

4321 gauge model for B-anomalies

CrossTalk Workshop: Flavour anomalies

Vrije Universiteit Brussel - 29.03.2018

Luca Di Luzio



[Based on:

LDL, Nardecchia 1706.01868

LDL, Greljo, Nardecchia, 1708.08450

LDL, Kirk, Lenz 1712.06572


LDL, Fuentes-Martin, Greljo, Nardecchia, Renner - work in progress]

Outline

1. Review of “B-anomalies”

- charged currents
- neutral currents

2. Combined explanations

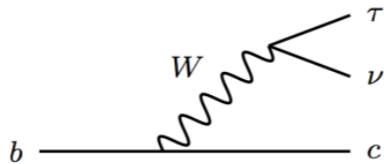
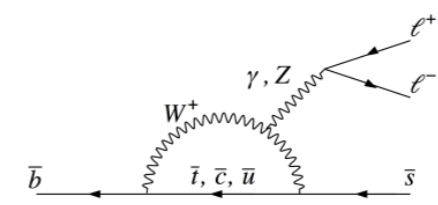
- EFT
- Simplified models
- UV completions  4321 model

Part-I

Review of “B-anomalies”

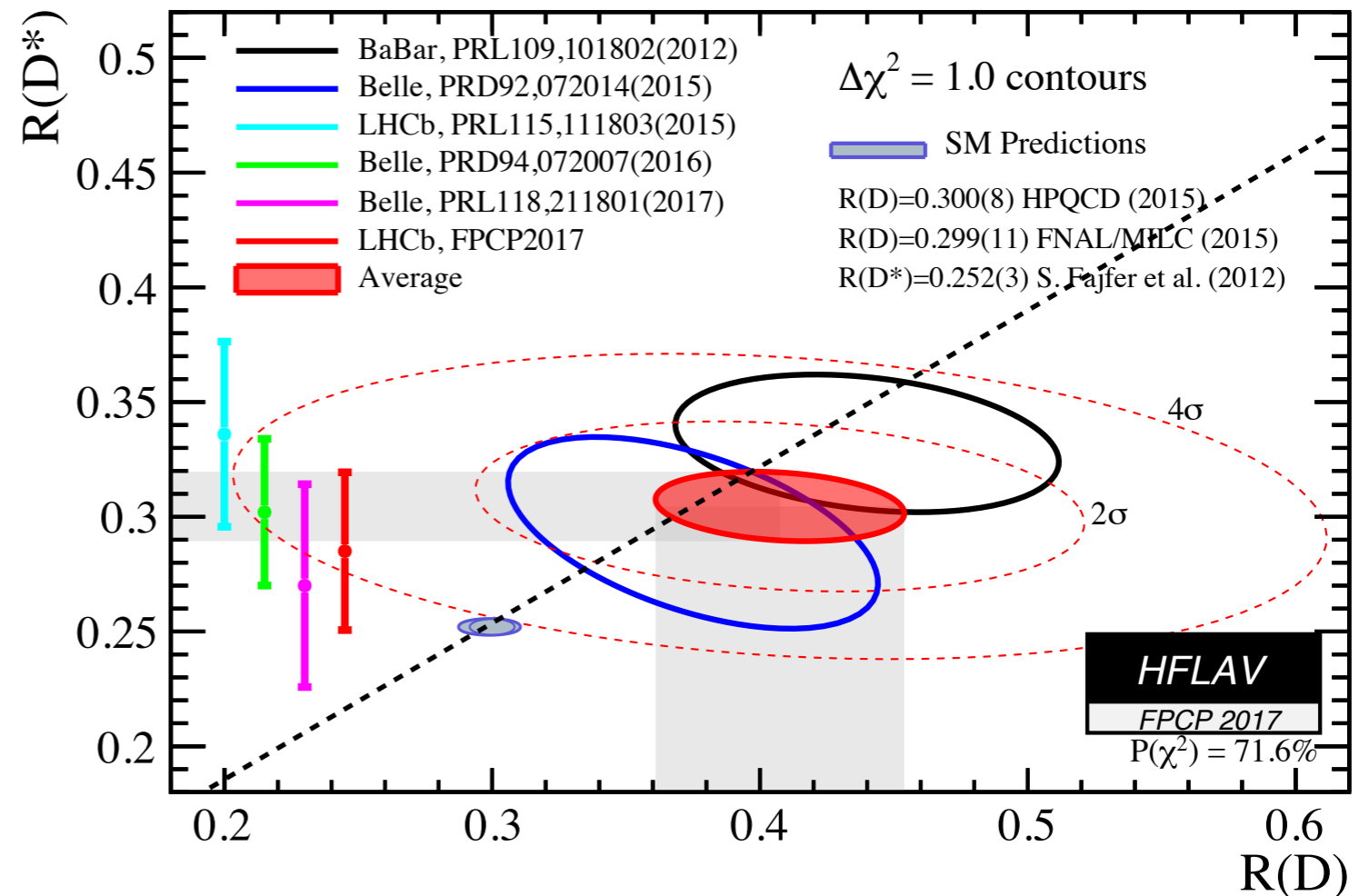
“B-anomalies”

- A seemingly coherent pattern of SM deviations building up since ~ 2013

	$b \rightarrow c\tau\nu$ 	$b \rightarrow s\mu\mu$ 
Lepton Universality	$R(D), R(D^*), R(J/\psi)$	$R(K), R(K^*)$
Angular Distributions		$B \rightarrow K^* \mu\mu (P'_5)$
Differential BR ($d\Gamma/dq^2$)		$B \rightarrow K^{(*)} \mu\mu$ $B_s \rightarrow \phi \mu\mu$ $\Lambda_b \rightarrow \Lambda \mu\mu$

Charged currents - $R(D)$ & $R(D^*)$

$$R(D^{(*)}) = \frac{\mathcal{B}(B \rightarrow D^{(*)} \tau \bar{\nu})}{\mathcal{B}(B \rightarrow D^{(*)} \ell \bar{\nu})}$$



- SM prediction quite robust
- Deviation seen in 3 exp. in a consistent way, **combined significance $\sim 4\sigma$**
- $R(D)$ and $R(D^*)$ point to constructive interference (+30%) with SM amplitude
- Suggests NP in LH tau currents (NP in e/mu and RH/scalar amplitudes disfavoured)

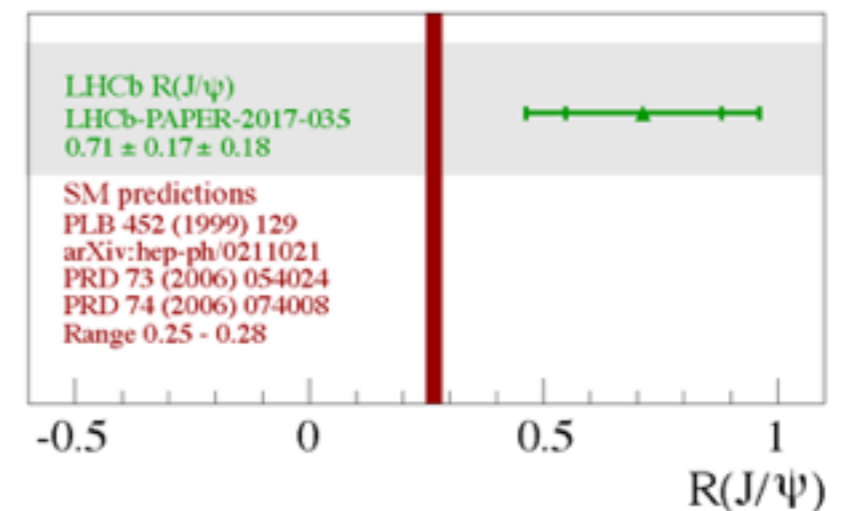
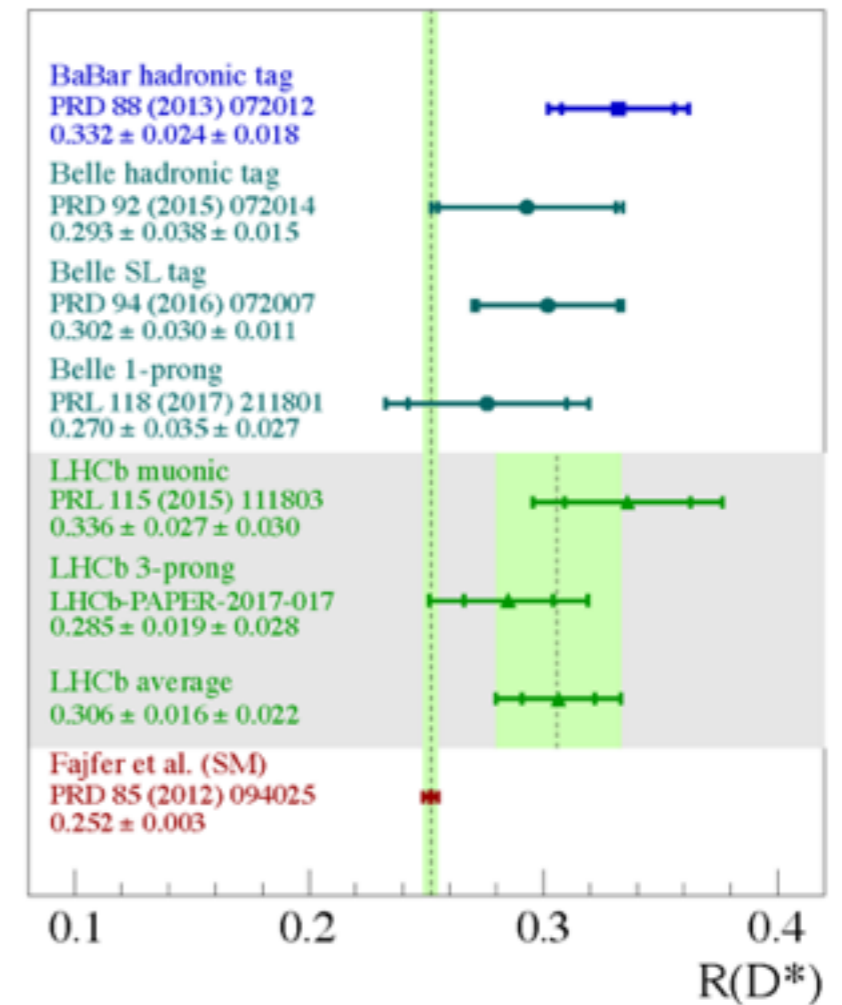
Charged currents - $R(D)$ & $R(D^*)$

$$R(D^{(*)}) = \frac{\mathcal{B}(B \rightarrow D^{(*)} \tau \bar{\nu})}{\mathcal{B}(B \rightarrow D^{(*)} \ell \bar{\nu})}$$

- Recently (as of Sept 2017):

$$R(J/\psi) = \frac{\mathcal{B}(B_c^+ \rightarrow J/\psi \tau^+ \nu_\tau)}{\mathcal{B}(B_c^+ \rightarrow J/\psi \mu^+ \nu_\mu)}$$

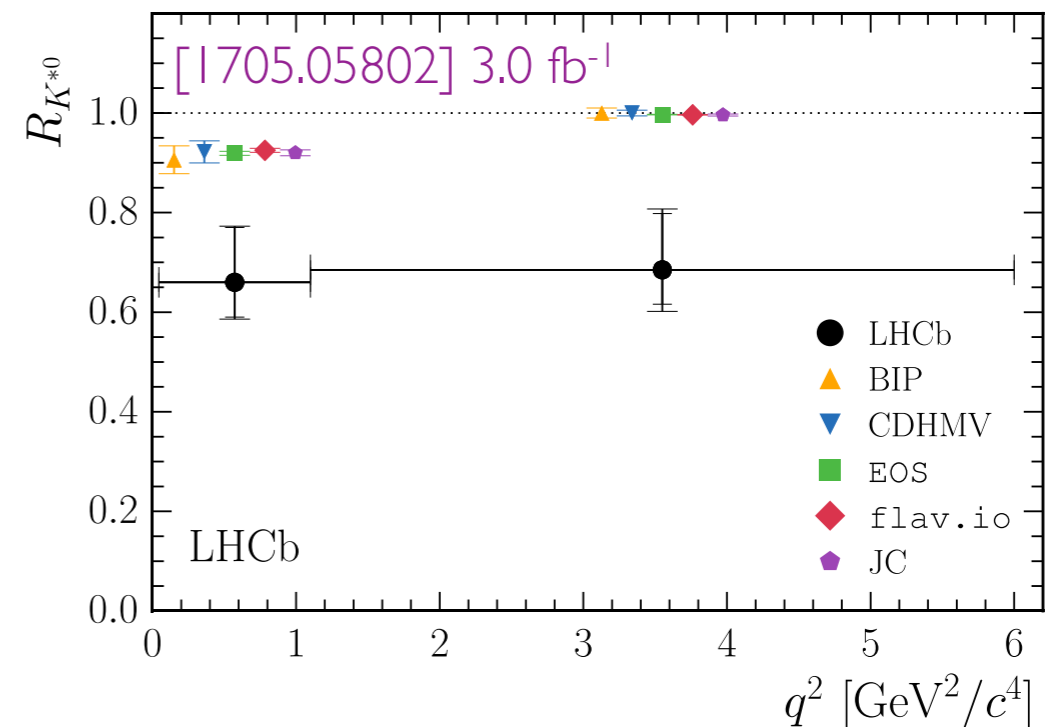
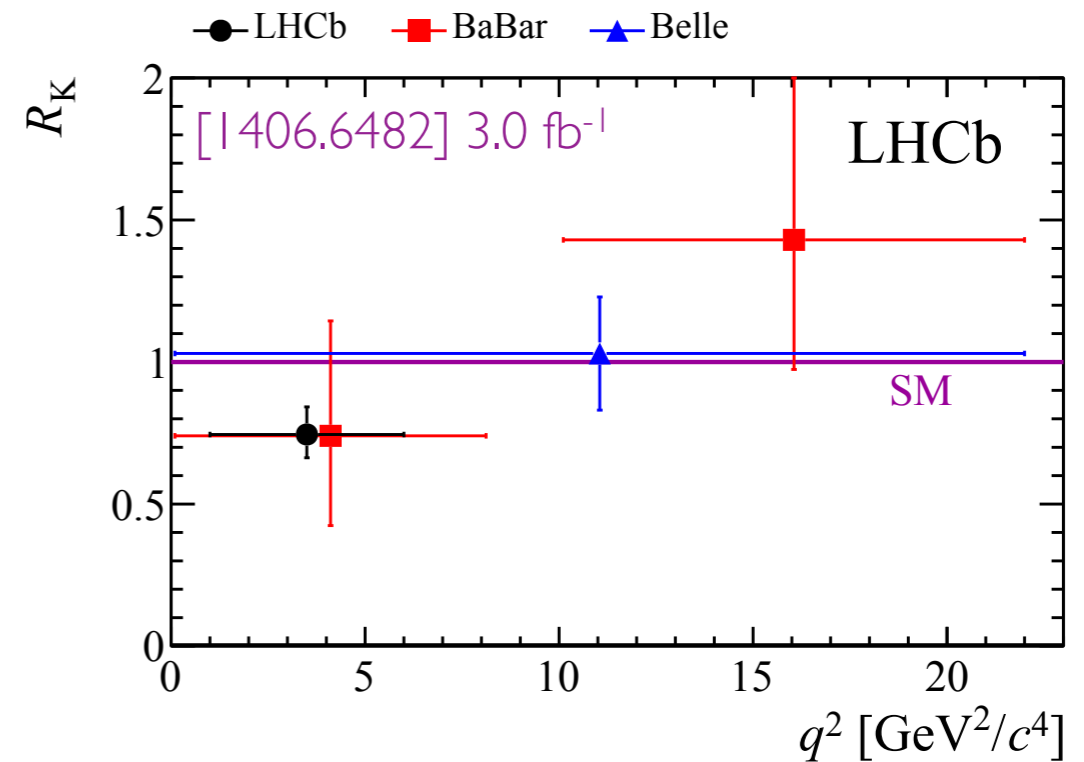
$\sim 2\sigma$ above the SM



Neutral currents - $R(K)$ & $R(K^*)$

$$R(K^{(*)}) = \frac{\mathcal{B}(B \rightarrow K^{(*)} \mu \bar{\mu})}{\mathcal{B}(B \rightarrow K^{(*)} e \bar{e})}$$

- SM prediction = $1 \pm O(1\%)$ [1406.6482]
- Combined significance $\sim 4\sigma$

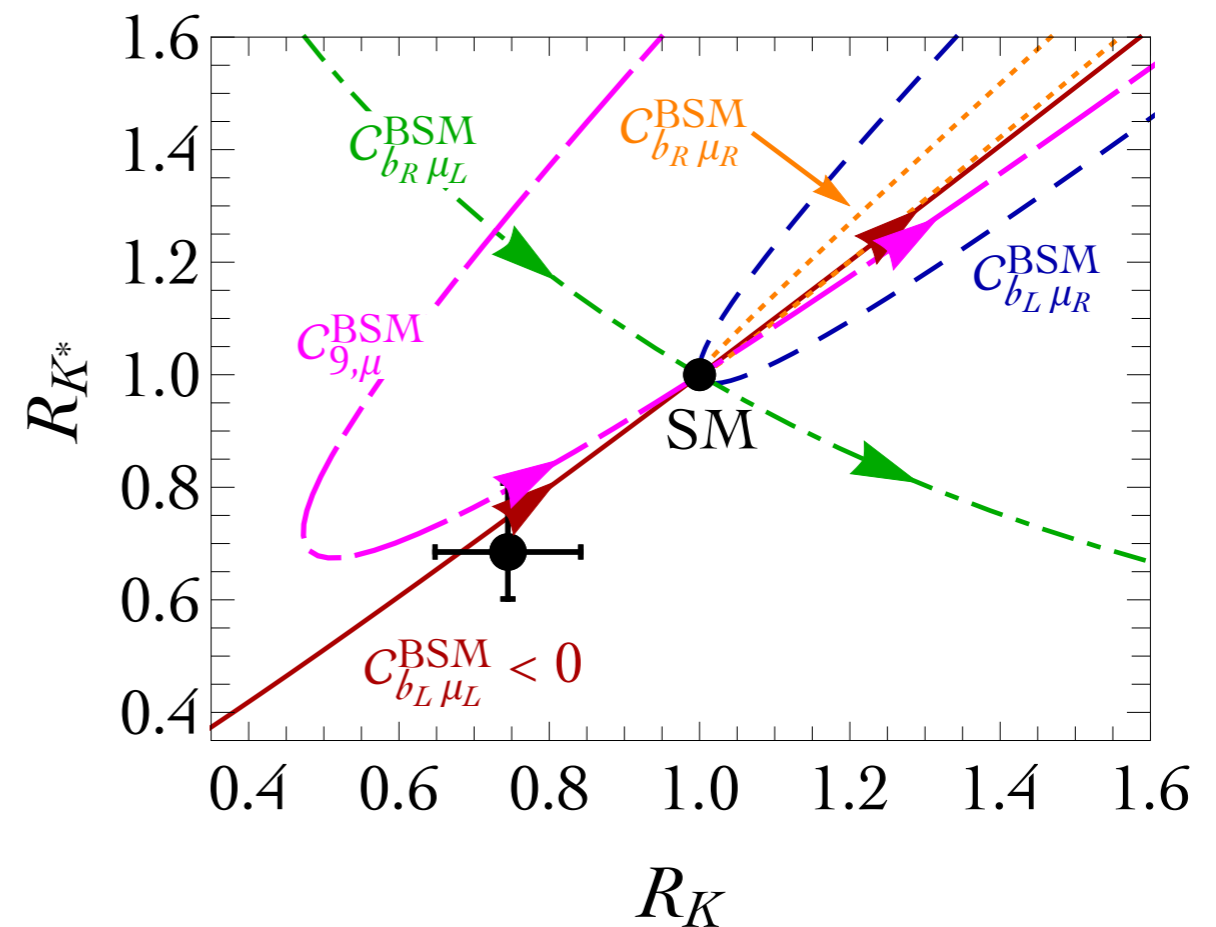


Neutral currents - $R(K)$ & $R(K^*)$

$$R(K^{(*)}) = \frac{\mathcal{B}(B \rightarrow K^{(*)} \mu \bar{\mu})}{\mathcal{B}(B \rightarrow K^{(*)} e \bar{e})}$$

$$R_{K^*} \simeq R_K - 4p \frac{\text{Re } C_{b_R(\mu-e)_L}^{\text{BSM}}}{C_{b_L\mu_L}^{\text{SM}}}$$

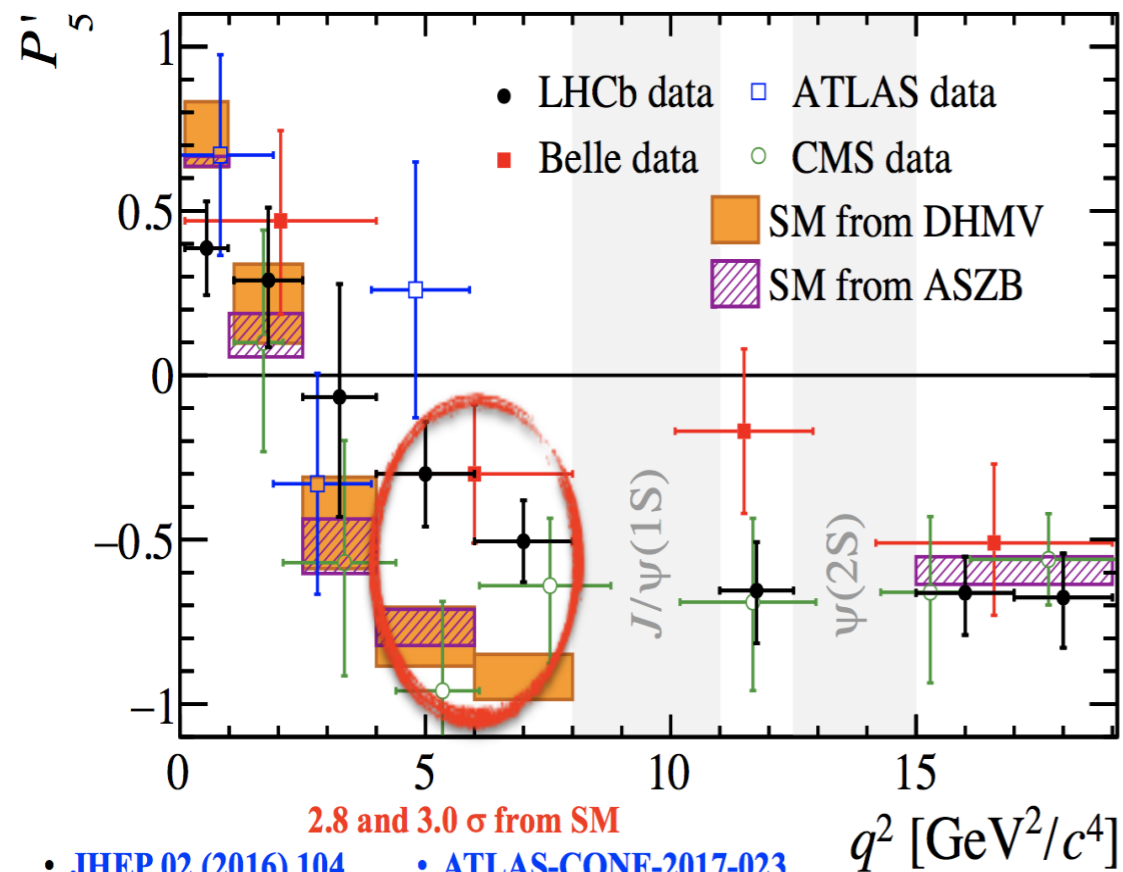
[D'Amico et al, 1704.05438]



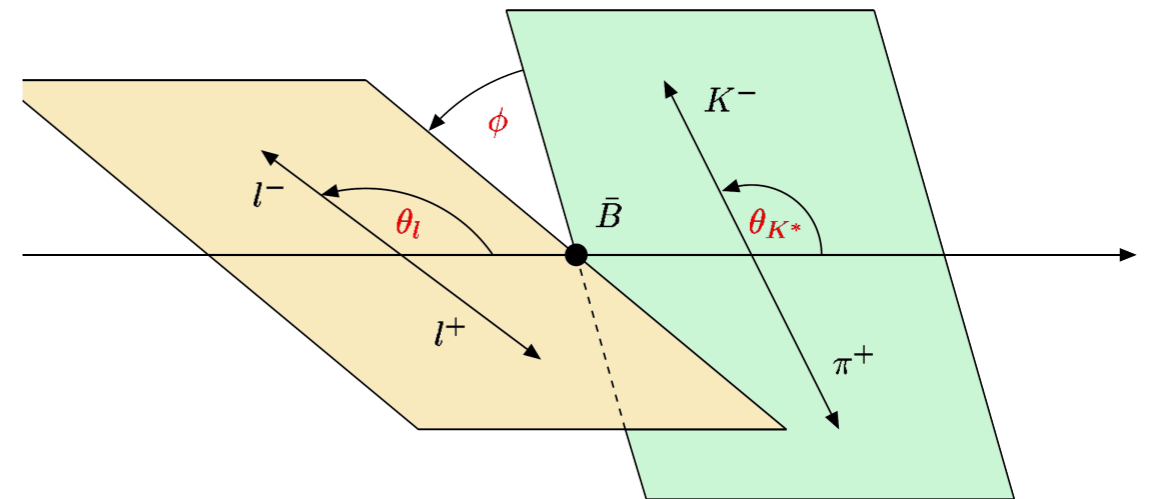
- NP in muons requires destructive interference with the SM (-15%)
- RH currents in quark sector disfavoured (predict wrong correlation)
- NP in electrons possible, but cannot explain anomalies in $b \rightarrow s \mu \mu$ angular observables

Neutral currents - P'5 et al

- Angular distributions in $B \rightarrow (K^* \rightarrow K\pi)\mu\mu$



- [JHEP 02 \(2016\) 104](#)
- [ATLAS-CONF-2017-023](#)
- [PRL 118 \(2017\)](#)
- [CMS-PAS-BPH-15-008](#)



$$P'_5 : \frac{d^4\Gamma}{dq^2 d\cos\theta_l d\cos\theta_{K^*} d\phi}$$

[Descotes-Genon, Matias, Ramon, Virto 1207.2753]

*Hadronic uncertainties potentially large

[See e.g. Chiuchini et al, 1512.07157]

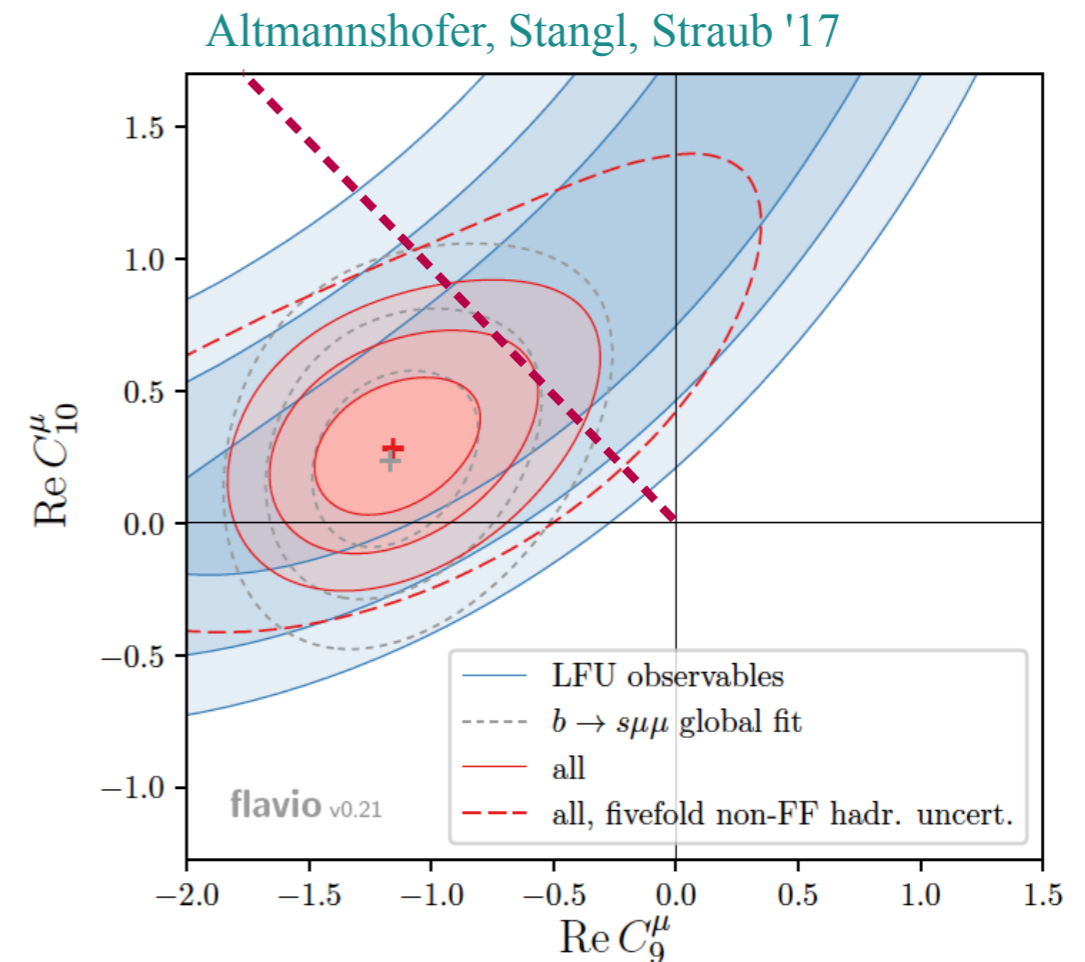
+ other low BR w.r.t. the SM ($B_S^0 \rightarrow \phi\mu^+\mu^-$)

Neutral currents - global fits

- Effects well-described by NP in $b \rightarrow s\mu\mu$ (explains also angular distributions, etc.)

$$O_9 \propto (\bar{s}_L \gamma_\mu b_L)(\bar{\ell}_L \gamma^\mu \ell)$$

$$O_{10} \propto (\bar{s}_L \gamma_\mu b_L)(\bar{\ell}_L \gamma^\mu \gamma_5 \ell)$$



Part-II

Combined explanations

EFT [general considerations]

- $SU(2)_L$ triplet operator (combined explanation in SMEFT)

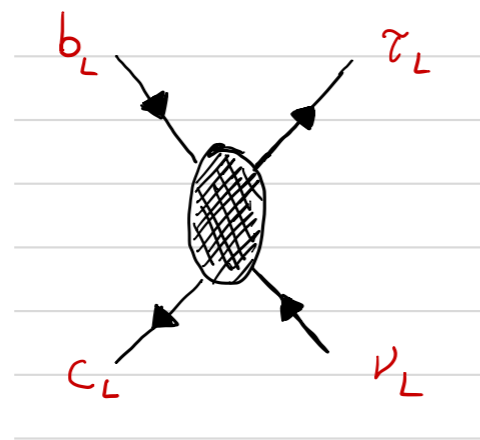
$$\frac{\lambda_{ij}^q \lambda_{kl}^\ell}{\Lambda^2} (\bar{Q}_L^i \sigma^a \gamma_\mu Q_L^j) (\bar{L}_L^k \sigma^a \gamma^\mu L_L^l)$$

[Bhattacharya et al 1412.7164
Alonso, Grinstein, Camalich 1505.05164,
Greljo, Isidori, Marzocca 1506.01705,
Calibbi, Crivellin, Ota 1506.02661, ...]

EFT [general considerations]

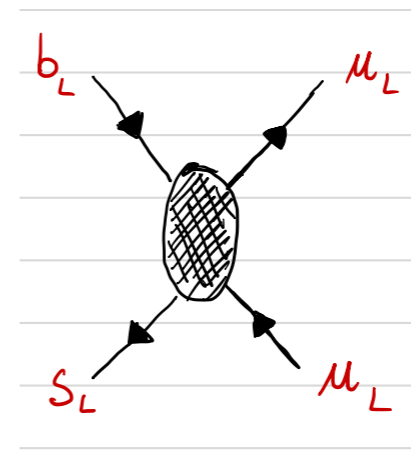
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$$\frac{\lambda_{ij}^q \lambda_{kl}^\ell}{\Lambda^2} (\bar{Q}_L^i \sigma^a \gamma_\mu Q_L^j) (\bar{L}_L^k \sigma^a \gamma^\mu L_L^l) \supset -\frac{1}{\Lambda_{RD}^2} 2 \bar{c}_L \gamma^\mu b_L \bar{\tau}_L \gamma_\mu \nu_L + \frac{1}{\Lambda_{RK}^2} \bar{s}_L \gamma^\mu b_L \bar{\mu}_L \gamma_\mu \mu_L$$



$$\Lambda_{RD} = 3.4 \text{ TeV}$$

\ll



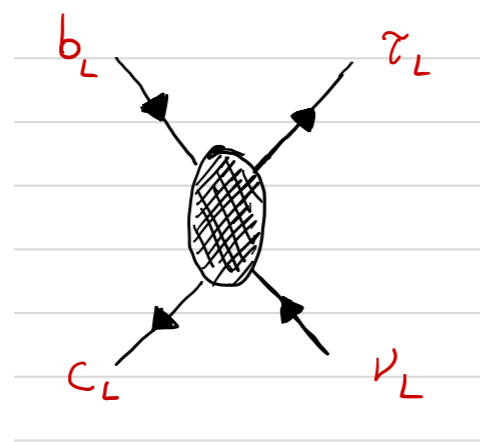
$$\Lambda_{RK} = 31 \text{ TeV}$$

what is the scale of NP ? (energy/coupling/mass ambiguity: $1/\Lambda^2 = g^2/M^2$)

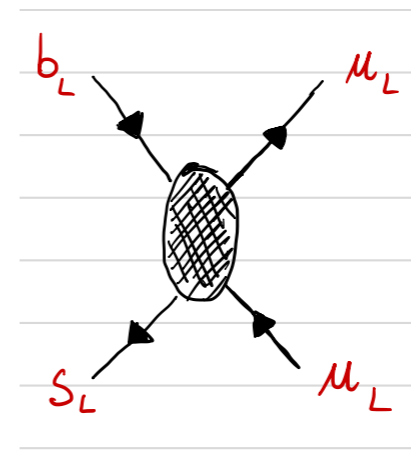
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$$\Lambda_{RD} = 3.4 \text{ TeV}$$



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\ll

- Perturbative unitarity bound from $2 \rightarrow 2$ fermion scatterings $a_{J=0} = \frac{\sqrt{3}}{8\pi} \frac{s}{\Lambda^2} < \frac{1}{2}$

$$\sqrt{s_{RD}} < 9.2 \text{ TeV (1.9 TeV)}$$

$$\sqrt{s_{RK}} < 84 \text{ TeV (17 TeV)}$$



no-loose theorem for HL/HE-LHC ?

[LDL, Nardecchia 1706.01868]

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- Flavour structure:

1. large couplings in taus (compete with SM tree level)
2. sizable couplings in muons (compete with SM one loop)
3. negligible couplings in electrons (well tested, not much room)

$$\lambda_{ij}^{q,\ell} = \delta_{i3} \delta_{j3} + \text{corrections} \quad U(2)_q \times U(2)_\ell \quad \text{approx flavor symmetry}$$

[Barbieri et al | 105.2296, 1512.01560]

$$Q_L^{(3)} \sim q_L^{(b)} = \begin{pmatrix} V_{ib}^* u_L^i \\ b_L \end{pmatrix}$$



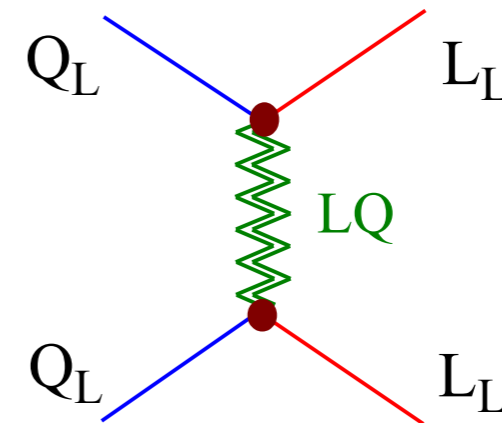
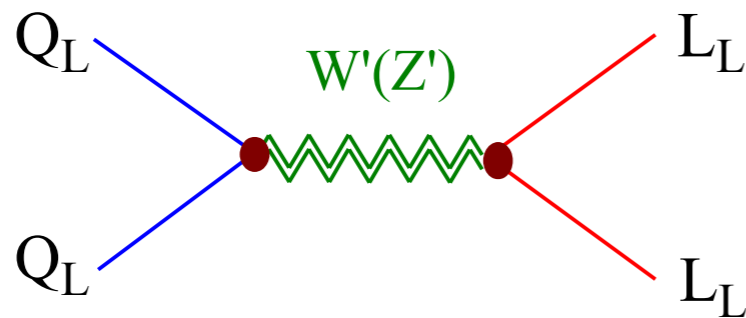
link to SM Yukawa pattern ?

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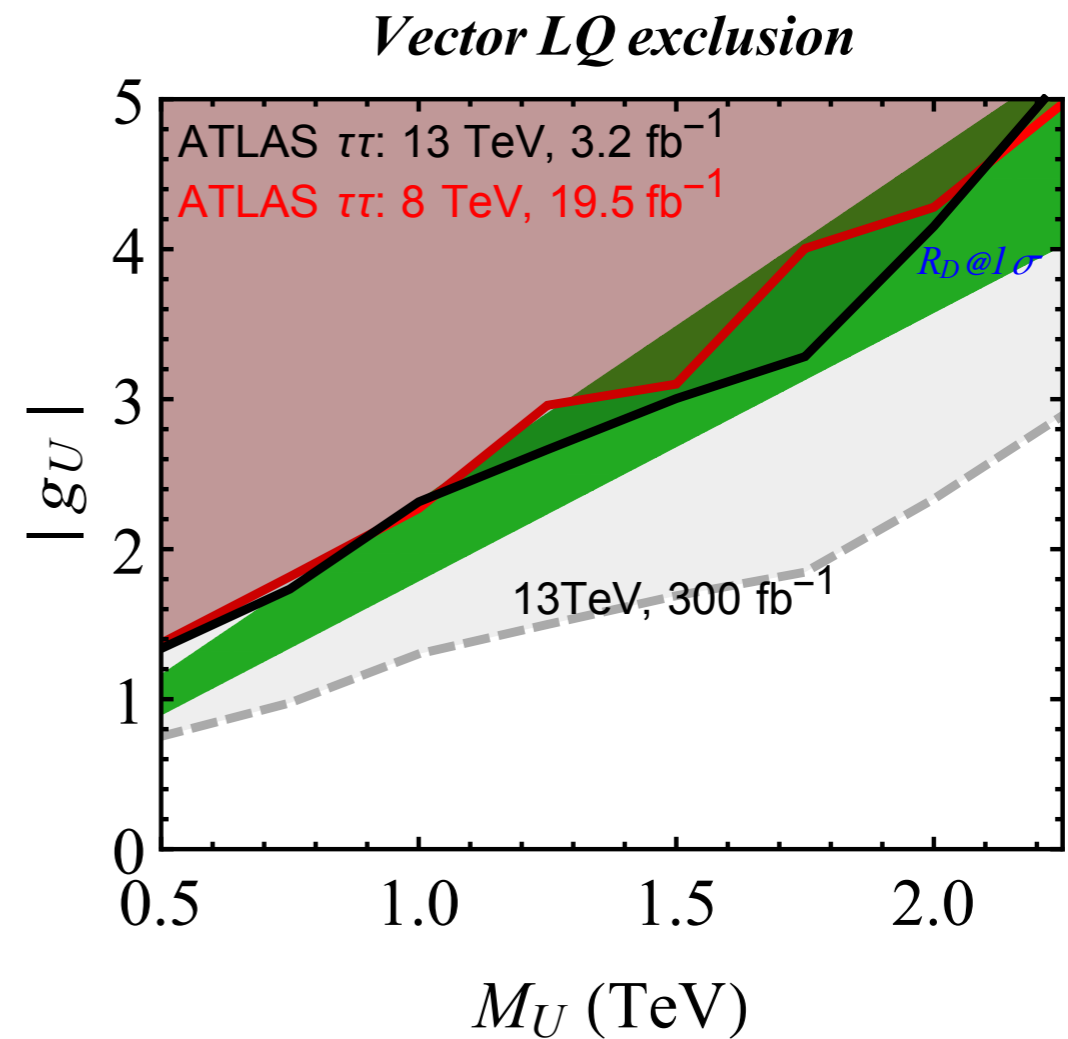
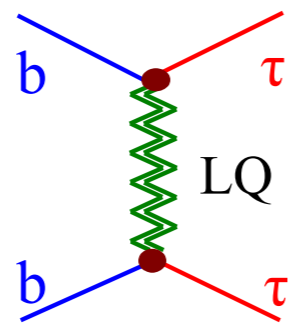
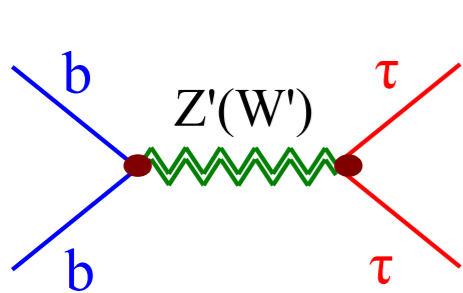
- Tree-level mediators:



EFT [problems]

- Three main problems mainly driven by R(D)

I. High- p_T constraints



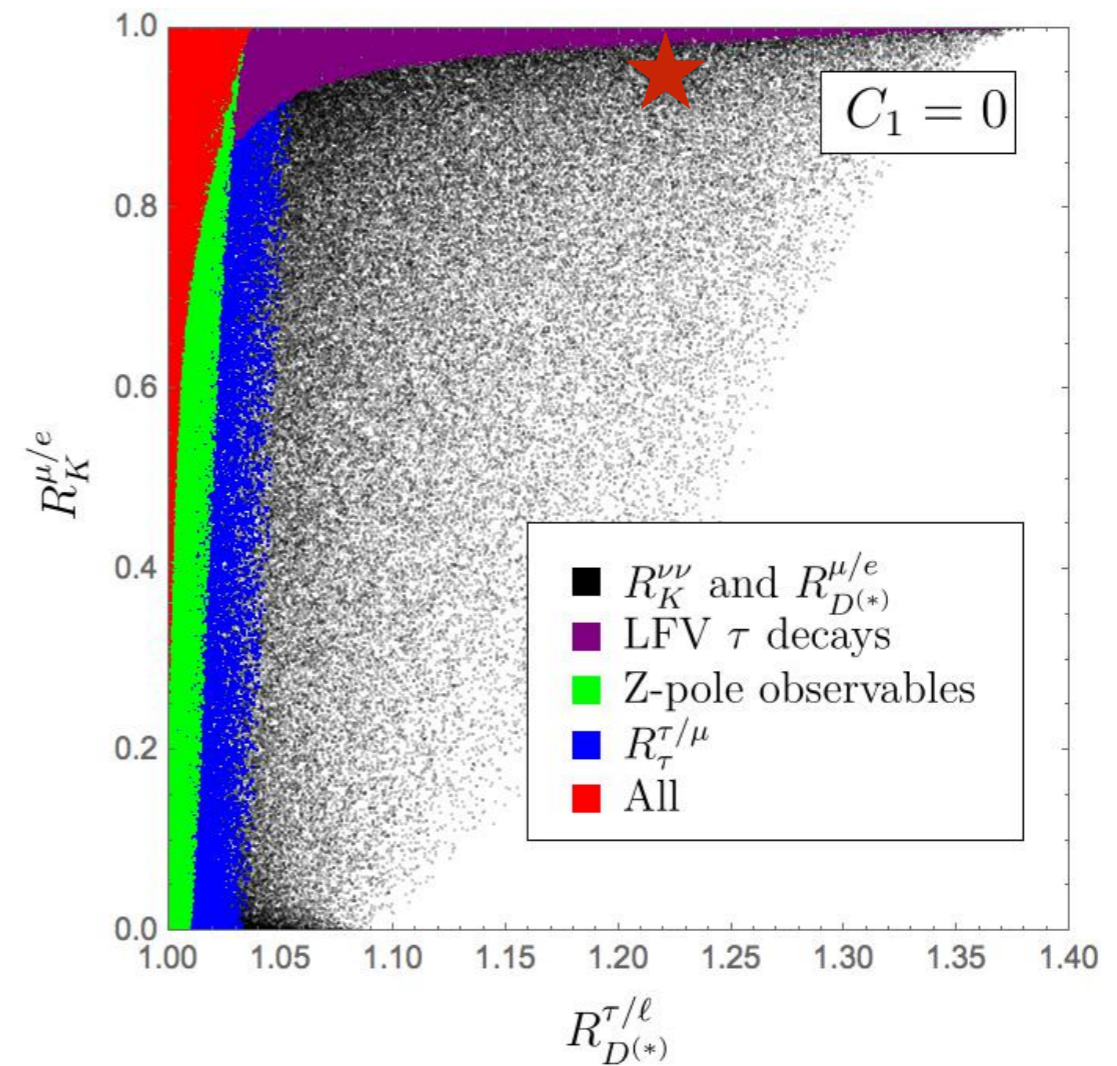
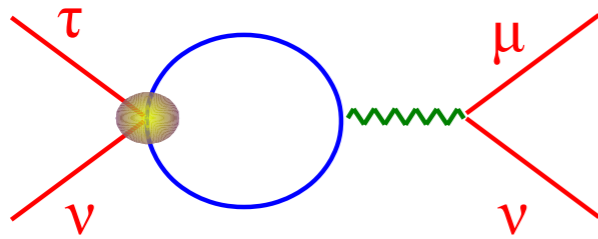
[Faroughy, Greljo, Kamenik | 609.07138]

EFT [problems]

- Three main problems mainly driven by R(D)

1. High- p_T constraints

2. Radiative constraints



[Feruglio, Paradisi, Pattori | 606.00524, | 705.00929]

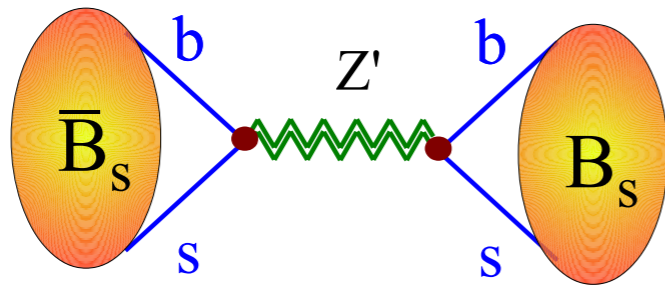
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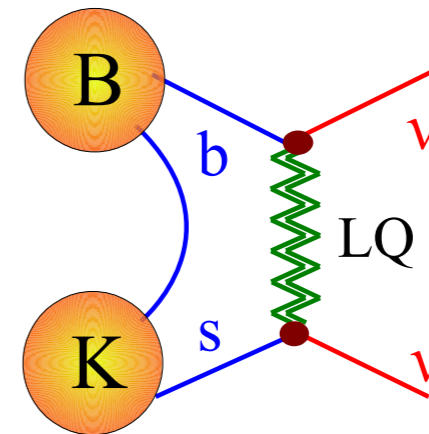
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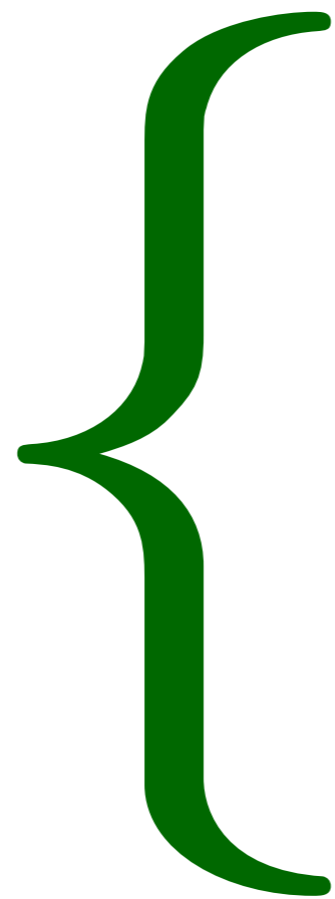
3. Flavour bounds



(absent at tree-level with LQ)



(consequence of $SU(2)_L$ invariance)



B_s-mixing

- Lattice results suggest a small discrepancy $\Delta M_s^{\text{SM}} > \Delta M_s^{\text{exp}} = (17.757 \pm 0.021) \text{ ps}^{-1}$ (1.8σ)

Source	$f_{B_s} \sqrt{\hat{B}}$	ΔM_s^{SM}
HPQCD14 [128]	$(247 \pm 12) \text{ MeV}$	$(16.2 \pm 1.7) \text{ ps}^{-1}$
ETMC13 [129]	$(262 \pm 10) \text{ MeV}$	$(18.3 \pm 1.5) \text{ ps}^{-1}$
HPQCD09 [130] = FLAG13 [131]	$(266 \pm 18) \text{ MeV}$	$(18.9 \pm 2.6) \text{ ps}^{-1}$
FLAG17 [69]	$(274 \pm 8) \text{ MeV}$	$(20.01 \pm 1.25) \text{ ps}^{-1}$
Fermilab16 [71]	$(274.6 \pm 8.8) \text{ MeV}$	$(20.1 \pm 1.5) \text{ ps}^{-1}$
HQET-SR [76, 132]	$(278_{-24}^{+28}) \text{ MeV}$	$(20.6_{-3.4}^{+4.4}) \text{ ps}^{-1}$
HPQCD06 [133]	$(281 \pm 20) \text{ MeV}$	$(21.0 \pm 3.0) \text{ ps}^{-1}$
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[LDL, Kirk, Lenz 1712.06572]

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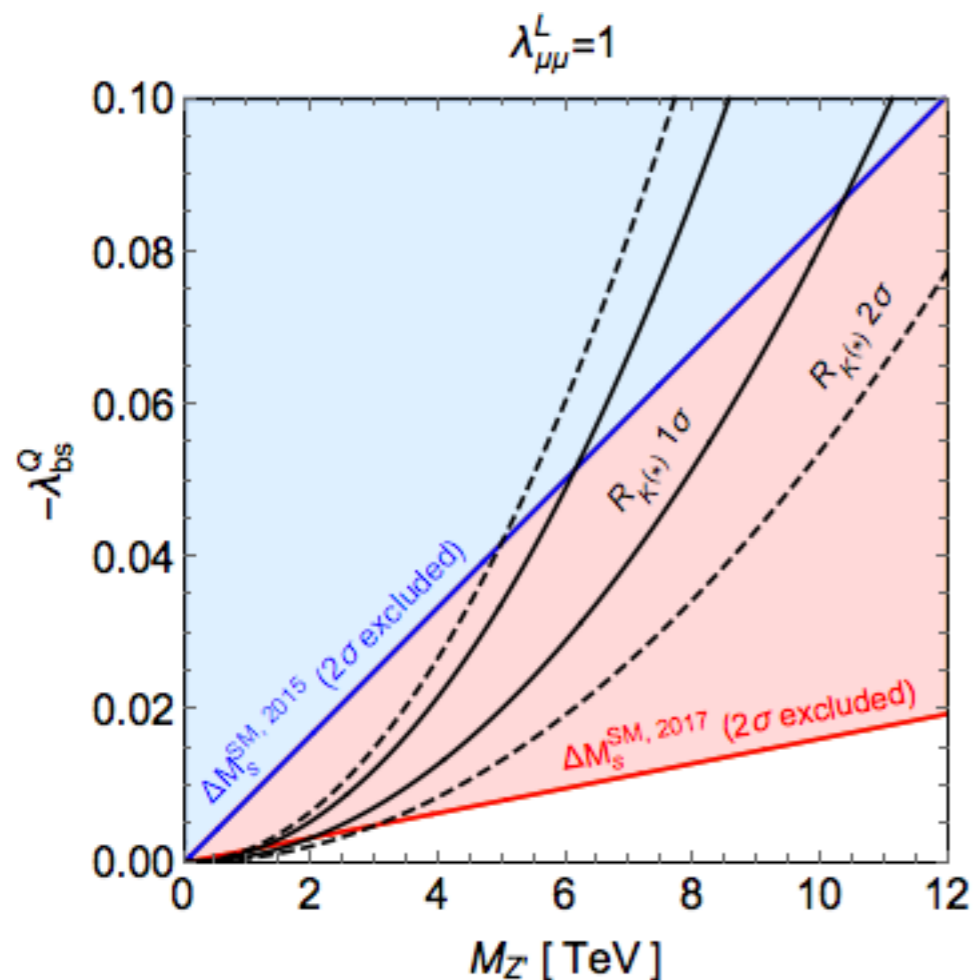
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[LDL, Kirk, Lenz 1712.06572]

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$$\frac{\Delta M_s^{\text{SM+NP}}}{\Delta M_s^{\text{SM}}} = \left| 1 + \frac{\kappa}{\Lambda_{\text{NP}}^2} \right| \quad \text{if } \kappa > 0 \quad \longrightarrow \quad \frac{\Lambda_{\text{NP}}^{2017}}{\Lambda_{\text{NP}}^{2015}} \simeq 5 \quad (2 \sigma \text{ bound})$$



$$\mathcal{L}_{Z'} = \frac{1}{2} M_{Z'}^2 (Z'_\mu)^2 + \left(\lambda_{ij}^Q \bar{d}_L^i \gamma^\mu d_L^j + \lambda_{\alpha\beta}^L \bar{\ell}_L^\alpha \gamma^\mu \ell_L^\beta \right) Z'_\mu$$

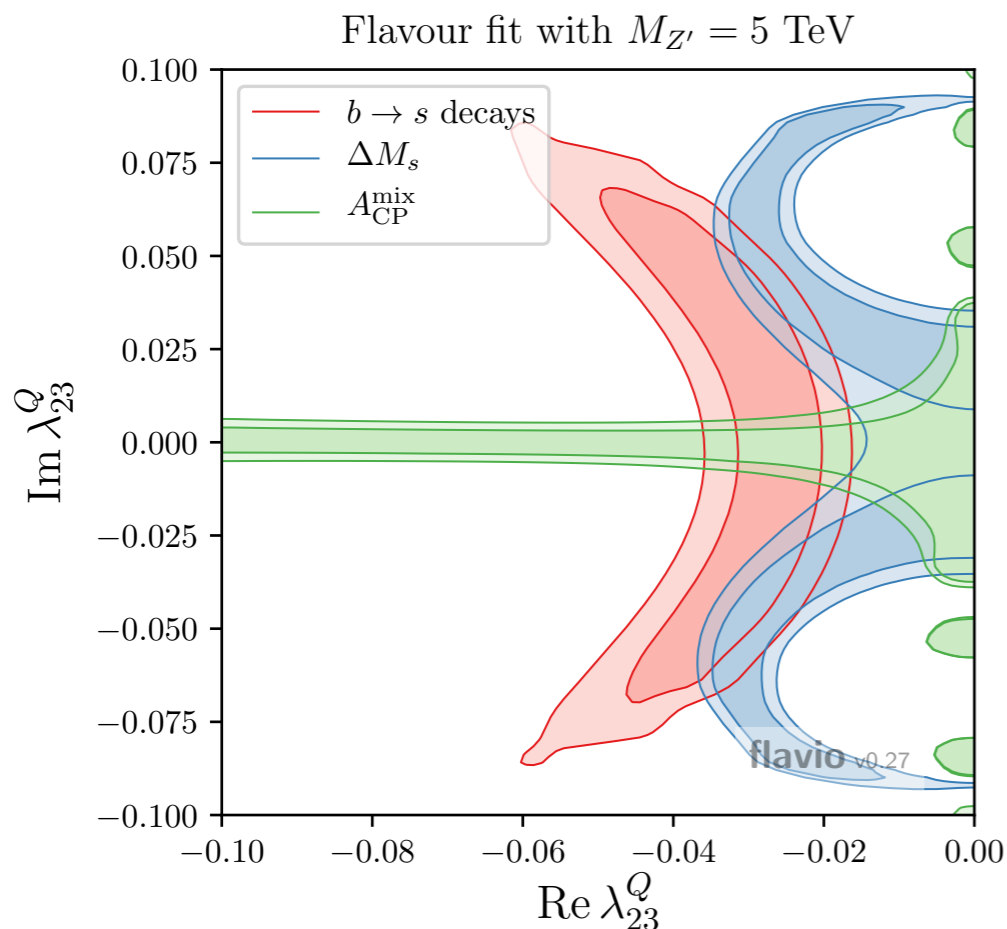
severe impact on Z' models for $b \rightarrow s\mu\mu$ anomalies

[LDL, Kirk, Lenz 1712.06572]

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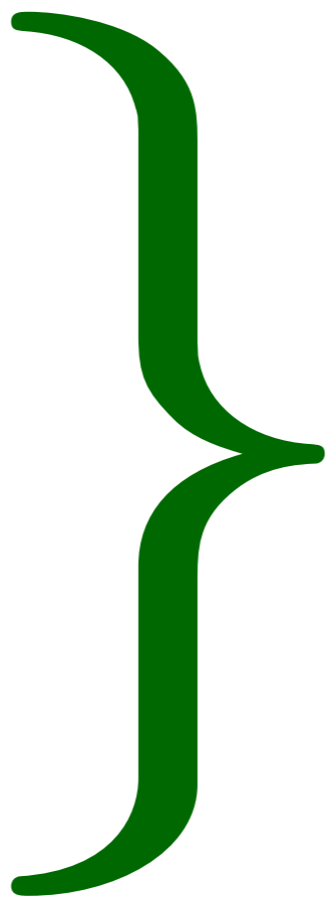
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Possible ways to obtain $\kappa < 0$:

- 1) Imaginary coupling $\kappa \sim (\lambda_{bs}^Q)^2$
- 2) RH currents contamination $\kappa \sim \lambda_{bs}^Q \lambda_{bs}^{d_R}$

- looking forward for lattice updates !

[LDL, Kirk, Lenz 1712.06572]



EFT [solutions]

- Tension gets drastically alleviated if

[Zürich's guide for combined explanations, 1706.07808]

1. Triplet + Singlet operator (more freedom in $SU(2)_L$ structure)

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{SM}} - \frac{1}{v^2} \lambda_{ij}^q \lambda_{\alpha\beta}^\ell \left[C_T (\bar{Q}_L^i \gamma_\mu \sigma^a Q_L^j) (\bar{L}_L^\alpha \gamma^\mu \sigma^a L_L^\beta) + C_S (\bar{Q}_L^i \gamma_\mu Q_L^j) (\bar{L}_L^\alpha \gamma^\mu L_L^\beta) \right]$$

2. Deviation from 'pure-mixing' scenario

$$\bar{Q}^i \lambda_{ij}^q Q^j = \left(\bar{u}^k V_{ki} \quad \bar{d}^i \right) \lambda_{ij}^q \begin{pmatrix} V_{jl}^\dagger u^l \\ d^j \end{pmatrix} \supset \bar{c} (V_{cb} \lambda_{bb}^q + V_{cs} \lambda_{sb}^q + \dots) b$$

$$R_{D^{(*)}}^{\tau\ell} \approx 1 + 2C_T \left(1 - \lambda_{sb}^q \frac{V_{tb}^*}{V_{ts}^*} \right) \quad \longrightarrow \quad \lambda_{sb}^q > \mathcal{O}(V_{cb}) \quad \text{allows for larger NP scale}$$

EFT [solutions]

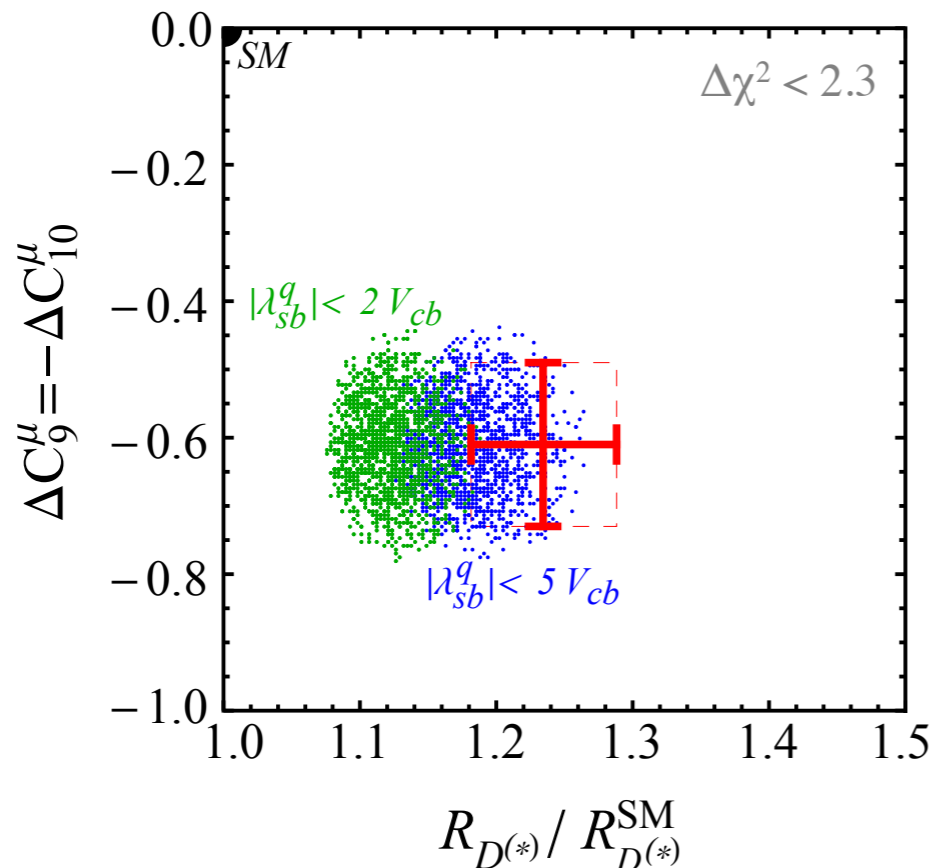
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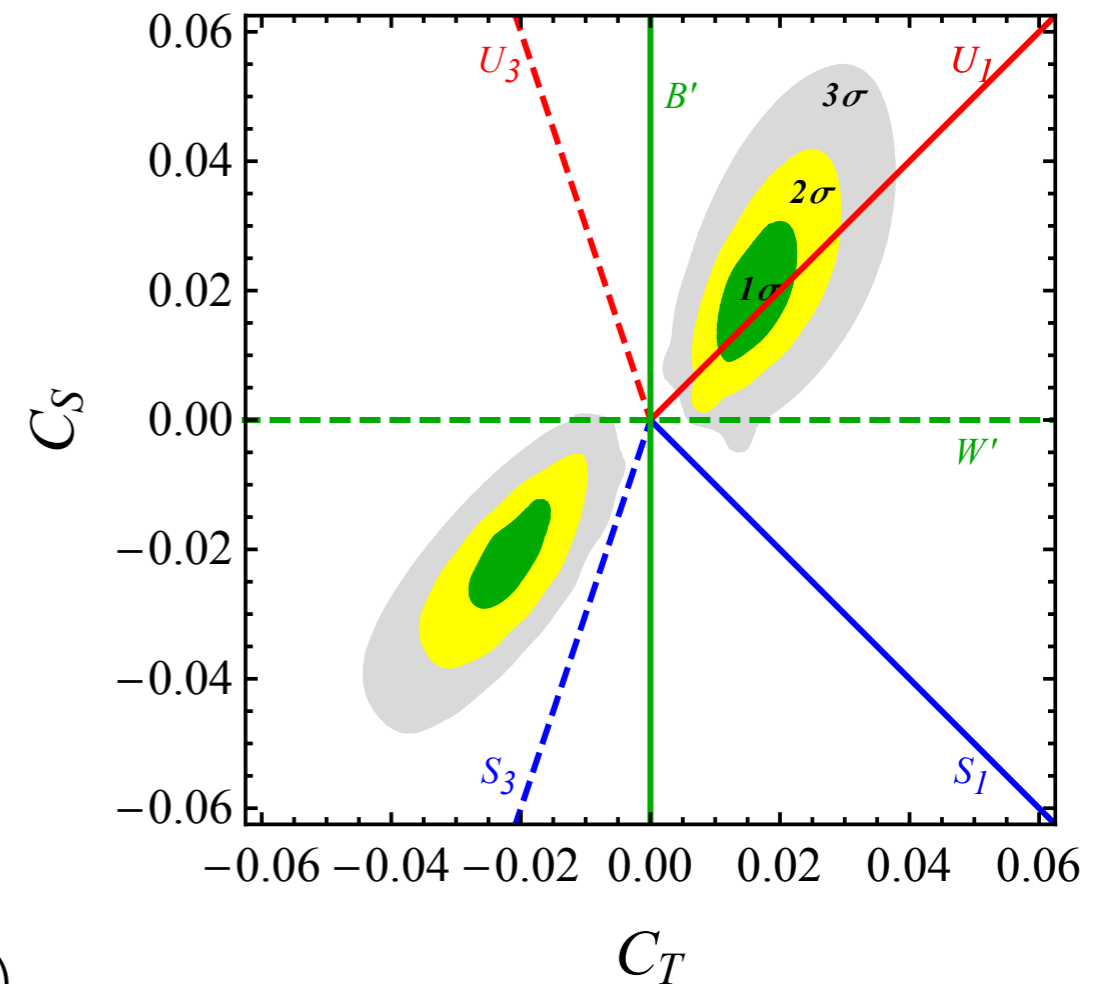
$\lambda_{sb}^q > \mathcal{O}(V_{cb})$ allows for larger NP scale

Simplified models

- Finite list of tree-level mediators

[Zürich's guide for combined explanations, 1706.07808]

Simplified Model	Spin	SM irrep	C_S/C_T	$R_{D^{(*)}}$	$R_{K^{(*)}}$
Z'	1	$(1, 1, 0)$	∞	×	✓
V'	1	$(1, 3, 0)$	0	✓	✓
S_1	0	$(\bar{3}, 1, 1/3)$	-1	✓	×
S_3	0	$(\bar{3}, 3, 1/3)$	3	✓	✓
U_1	1	$(3, 1, 2/3)$	1	✓	✓
U_3	1	$(3, 3, 2/3)$	-3	✓	✓



$$\mathcal{B}(B \rightarrow K^* \nu \nu) \propto (C_T - C_S)$$

A clear winner: U_1 \rightarrow $C_T = C_S$ (at threshold)

Linear combinations also possible (e.g. $S_1 + S_3$ or $Z' + V'$) \rightarrow tuning required

UV completion: $U_1 \sim (3, 1, 2/3)$

- Massive vectors point to UV dynamics at the TeV scale

composite resonance of
a new strong dynamics

gauge boson of an
extended gauge sector

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composite resonance of
a new strong dynamics

$$\frac{G}{H} = \frac{SU(4) \times SO(5) \times U(1)_X}{SU(4) \times SO(4) \times U(1)_X}$$

[Barbieri, Isidori, Pattori, Senia 1502.01560
Barbieri, Murphy, Senia 1611.0493
Buttazzo et al, 1706.07808
Barbieri, Tesi 1712.06844]

- Ambitious program: pNGB Higgs + U_1 as composite state of G
 - 😊 conceptual link with the naturalness issue of EW scale
 - 😞 light LQ lowers the whole resonances' spectrum: issue with direct searches + EWPTs
 - 😞 intrinsically non-calculable (e.g. divergent loop observables)

UV completion: $U_1 \sim (3, 1, 2/3)$

- An interesting option: minimal Pati-Salam (PS)

$$G_{PS} = SU(4)_{PS} \times SU(2)_L \times SU(2)_R$$

$$G_{PS}/G_{SM} = U_1 + Z' + W_R$$

gauge boson of an extended gauge sector

😊 hinted by SM chiral structure + everything's calculable

$$W_L \begin{array}{c} \updownarrow \\ \updownarrow \end{array} \begin{pmatrix} u_L & \nu_L \\ d_L & e_L \end{pmatrix} \quad U_1 \begin{array}{c} \leftarrow \rightleftarrows \rightarrow \\ \leftarrow \rightleftarrows \rightarrow \end{array}$$
$$W_R \begin{array}{c} \updownarrow \\ \updownarrow \end{array} \begin{pmatrix} u_R & \nu_R \\ d_R & e_R \end{pmatrix} \quad U_1 \begin{array}{c} \leftarrow \rightleftarrows \rightarrow \\ \leftarrow \rightleftarrows \rightarrow \end{array}$$

$$SU(4)_{PS} \supset SU(3)_C \times U(1)_{B-L}$$

$$Y = T_R^3 + (B - L)/2$$

UV completion: $U_1 \sim (3, 1, 2/3)$

- An interesting option: minimal Pati-Salam (PS)

$$G_{PS} = SU(4)_{PS} \times SU(2)_L \times SU(2)_R$$

$$G_{PS}/G_{SM} = U_1 + Z' + W_R$$

gauge boson of an extended gauge sector

😊 hinted by SM chiral structure + everything's calculable

😞 $M_{U_1} \gtrsim 86$ TeV from $K_L^0, B^0, B_s \rightarrow \ell \ell'$ decays (L \times R couplings)

[Kutznetsov et al 1203.0196
+ update from A. D. Smirnov
1801.02895]

mass basis

$$\mathcal{L}_{PS} \supset \frac{g_4}{\sqrt{2}} \left(\bar{d}_L^i \delta_{ij} \gamma_\mu e_L^j + \bar{d}_R^i \delta_{ij} \gamma_\mu e_R^j \right) U_1^\mu \quad \longrightarrow \quad \frac{g_4}{\sqrt{2}} \left(\bar{d}_L^i \beta_{ij}^L \gamma_\mu e_L^j + \bar{d}_R^i \beta_{ij}^R \gamma_\mu e_R^j \right) U_1^\mu$$

$$\beta^{L,R} = U_{d_{L,R}}^\dagger U_{e_{L,R}} \quad (\text{unitary matrices})$$

UV completion: $U_1 \sim (3, 1, 2/3)$

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gauge boson of an extended gauge sector

- 😊 hinted by SM chiral structure + everything's calculable
- 😞 $M_{U_1} \gtrsim 86 \text{ TeV}$ from $K_L^0, B^0, B_s \rightarrow \ell \ell'$ decays (L \times R couplings)
- 😞 Z' direct searches ($M_{U_1} \sim M_{Z'} \sim \text{TeV} + \mathcal{O}(g_s)$ Z' couplings to valence quarks)
- 😞 neutrino masses also suggest $M_{U_1} \gg \text{TeV}$ ($y_{\text{top}} \sim y_{\nu_3\text{-Dirac}}$)

➔ Minimal PS cannot explain B-anomalies

Beyond minimal PS

- We want something like

$$\beta^L \sim \begin{pmatrix} \epsilon & \epsilon & \epsilon \\ \epsilon & 0.02 & 0.2 \\ \epsilon & 0.06 & 1 \end{pmatrix} \quad \beta^R \sim \epsilon \quad (\beta^\dagger \beta \neq 1)$$

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l): non-minimal **matter** content (mixing with heavy fermions)

[Calibbi, Crivellin, Li 1709.00692]

$$\frac{g_4}{\sqrt{2}} \overline{D}^A \hat{\beta}_{AB} \gamma_\mu \mathcal{E}^B U_1^\mu \quad \hat{\beta} = \begin{pmatrix} \beta_{LL} & \beta_{LH} \\ \beta_{HL} & \beta_{HH} \end{pmatrix} \quad \begin{aligned} \hat{\beta}^\dagger \hat{\beta} &= 1 \\ \beta_{LL}^\dagger \beta_{LL} &\neq 1 \end{aligned}$$

☹️ Z' direct searches

☹️ neutrino masses

Beyond minimal PS

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$$\beta^L \sim \begin{pmatrix} \epsilon & \epsilon & \epsilon \\ \epsilon & 0.02 & 0.2 \\ \epsilon & 0.06 & 1 \end{pmatrix} \quad \beta^R \sim \epsilon \quad (\beta^\dagger \beta \neq 1)$$

1): non-minimal **matter** content (mixing with heavy fermions)

[Calibbi, Crivellin, Li 1709.00692]

2): non-universal **gauge** interactions

[Bordone, Cornella, Fuentes-Martin, Isidori 1712.01368]

$$(422)^3 \quad \sum_{i=1,2,3} \frac{g_4^i}{\sqrt{2}} \bar{Q}^i \gamma^\mu L^i U_\mu^i \quad \xrightarrow{m_{U_1} \gg m_{U_2} \gg m_{U_3}} \quad \beta^{LO} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

😊 flavour hierarchies

😞 neutrino masses [Greljo, Stefanek 1802.04274]

😊 low-energy effective theory similar to 4321 model

Beyond minimal PS

- We want something like

$$\beta^L \sim \begin{pmatrix} \epsilon & \epsilon & \epsilon \\ \epsilon & 0.02 & 0.2 \\ \epsilon & 0.06 & 1 \end{pmatrix} \quad \beta^R \sim \epsilon \quad (\beta^\dagger \beta \neq 1)$$

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3): non-minimal **matter** and **gauge** content (4321 model) [LDL, Greljo, Nardecchia 1708.08450]

$$G = SU(4) \times SU(3)' \times SU(2)_L \times U(1)' \quad + \text{heavy fermions}$$



The '4321' model

[LDL, Greljo, Nardecchia | 708.08450. Inspired by Diaz, Schmaltz, Zhong | 706.05033, Georgi, Nakai | 606.05865]

$$G = SU(4) \times SU(3)' \times SU(2)_L \times U(1)' \longrightarrow G_{SM} = SU(3)_C \times SU(2)_L \times U(1)_Y$$

$\langle \Omega_{1,3} \rangle$

Embedding:

$$SU(3)_C = (SU(3)_4 \times SU(3)')_{diag}$$

$$g_s = \frac{g_4 g_3}{\sqrt{g_4^2 + g_3^2}} \simeq g_3$$

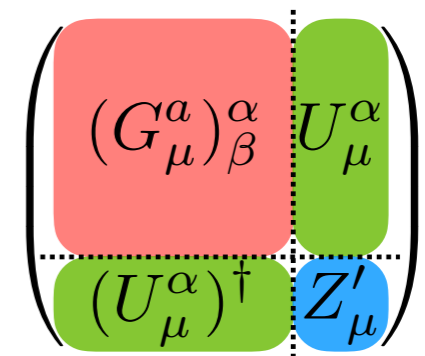
$$U(1)_Y = (U(1)_4 \times U(1)')_{diag}$$

$$g_Y = \frac{g_4 g_1}{\sqrt{g_4^2 + \frac{2}{3} g_1^2}} \simeq g_1$$

Gauge boson spectrum:

$$G/G_{SM} = U + Z' + g'$$

$$M_{g'} \simeq \sqrt{2} M_U \quad M_{Z'} \simeq \sqrt{\frac{3}{2}} M_U$$



→ Structure of gauge symmetry breaking does not allow to decouple g' and Z'

The '4321' model

[LDL, Greljo, Nardecchia | 708.08450. Inspired by Diaz, Schmaltz, Zhong | 706.05033, Georgi, Nakai | 606.05865]

$$G = SU(4) \times SU(3)' \times SU(2)_L \times U(1)' \xrightarrow{\langle \Omega_{1,3} \rangle} G_{SM} = SU(3)_C \times SU(2)_L \times U(1)_Y$$

Matter content:

Field	$SU(4)$	$SU(3)'$	$SU(2)_L$	$U(1)'$
q_L^i	1	3	2	1/6
u_R^i	1	3	1	2/3
d_R^i	1	3	1	-1/3
ℓ_L^i	1	1	2	-1/2
e_R^i	1	1	1	-1
Ψ_L^i	4	1	2	0
Ψ_R^i	4	1	2	0
H	1	1	2	1/2
Ω_3	$\bar{4}$	3	1	1/6
Ω_1	$\bar{4}$	1	1	-1/2

Would-be SM fields

Vector-like fermions (Q'+L')

SSB



mix after SSB

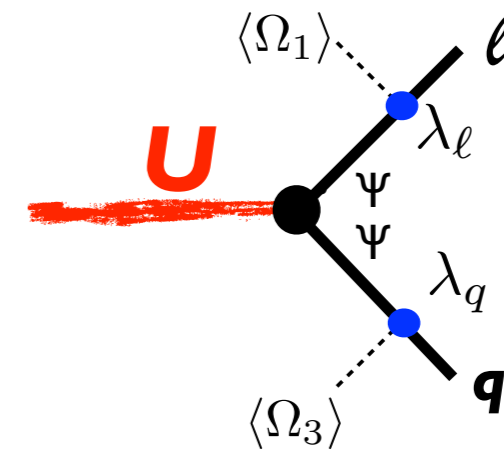
Yukawa sector:

$$\begin{aligned} \mathcal{L}_Y = & - \bar{q}'_L Y_d H d'_R - \bar{q}'_L Y_u \tilde{H} u'_R - \bar{\ell}'_L Y_e H e'_R \\ & - \bar{q}'_L \lambda_q \Omega_3^T \Psi_R - \bar{\ell}'_L \lambda_\ell \Omega_1^T \Psi_R - \bar{\Psi}_L M \Psi_R \end{aligned}$$

Key phenomenological features

I. LQ couples dominantly to 3rd generation LH fields (can satisfy Zürich's EFT criteria)

Field	$SU(4)$	$SU(3)'$	$SU(2)_L$	$U(1)'$
q_L^i	1	3	2	1/6
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d_R^i	1	3	1	-1/3
ℓ_L^i	1	1	2	-1/2
e_R^i	1	1	1	-1
Ψ_L^i	4	1	2	0
Ψ_R^i	4	1	2	0
H	1	1	2	1/2
Ω_3	$\bar{4}$	3	1	1/6
Ω_1	$\bar{4}$	1	1	-1/2



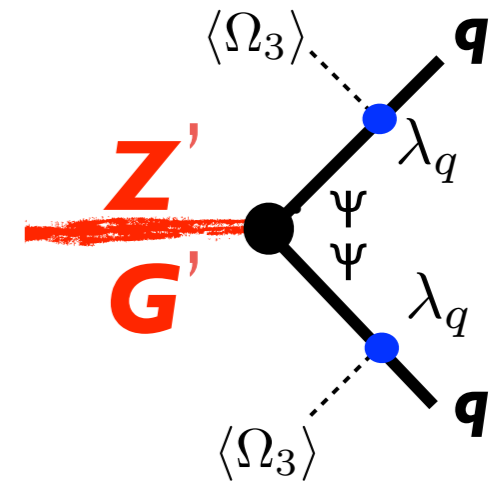
$$\mathcal{L}_Y = -\bar{q}'_L Y_d H d'_R - \bar{q}'_L Y_u \tilde{H} u'_R - \bar{\ell}'_L Y_e H e'_R \\ - \bar{q}'_L \lambda_q \Omega_3^T \Psi_R - \bar{\ell}'_L \lambda_\ell \Omega_1^T \Psi_R - \bar{\Psi}_L M \Psi_R$$

Key phenomenological features

1. LQ couples dominantly to 3rd generation LH fields (can satisfy Zürich's EFT criteria)
2. Down-alignment to avoid tree-level FCNC in the down sector

$$\mathcal{M}_d = \begin{pmatrix} \frac{v}{\sqrt{2}} Y_d^{\text{diag}} & \frac{v_3}{\sqrt{2}} \lambda_q \\ 0 & M^{\text{diag}} \end{pmatrix} \quad \lambda_q = \begin{pmatrix} \lambda_q^d & 0 & 0 \\ 0 & \lambda_q^s & 0 \\ 0 & 0 & \lambda_q^b \end{pmatrix}$$

$$\mathcal{M}_u = \begin{pmatrix} \frac{v}{\sqrt{2}} V^\dagger Y_u^{\text{diag}} & \frac{v_3}{\sqrt{2}} \lambda_q \\ 0 & M^{\text{diag}} \end{pmatrix} \quad \longrightarrow \quad \text{CKM-induced D-mixing}$$



$$\begin{aligned} \mathcal{L}_Y = & -\bar{q}'_L Y_d H d'_R - \bar{q}'_L Y_u \tilde{H} u'_R - \bar{\ell}'_L Y_e H e'_R \\ & - \bar{q}'_L \lambda_q \Omega_3^T \Psi_R - \bar{\ell}'_L \lambda_\ell \Omega_1^T \Psi_R - \bar{\Psi}_L M \Psi_R \end{aligned}$$

Key phenomenological features

1. LQ couples dominantly to 3rd generation LH fields (can satisfy Zürich's EFT criteria)
2. Down-alignment to avoid tree-level FCNC in the down sector
3. Suppressed Z' and g' couplings to light generations

$$\begin{aligned}\mathcal{L}_L \supset & \frac{g_4}{\sqrt{2}} \bar{Q}'_L \gamma^\mu L'_L U_\mu + \text{h.c.} \\ & + \frac{g_4 g_s}{g_3} \left(\bar{Q}'_L \gamma^\mu T^a Q'_L - \frac{g_3^2}{g_4^2} \bar{q}'_L \gamma^\mu T^a q'_L \right) g'_a \\ & + \frac{1}{6} \frac{\sqrt{3} g_4 g_Y}{\sqrt{2} g_1} \left(\bar{Q}'_L \gamma^\mu Q'_L - \frac{2g_1^2}{3g_4^2} \bar{q}'_L \gamma^\mu q'_L \right) Z'_\mu \\ & - \frac{1}{2} \frac{\sqrt{3} g_4 g_Y}{\sqrt{2} g_1} \left(\bar{L}'_L \gamma^\mu L'_L - \frac{2g_1^2}{3g_4^2} \bar{\ell}'_L \gamma^\mu \ell'_L \right) Z'_\mu\end{aligned}$$

Key phenomenological features

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 & - \frac{1}{2} \frac{\sqrt{3} g_4 g_Y}{\sqrt{2} g_1} \left(\bar{L}'_L \gamma^\mu L'_L - \frac{2g_1^2}{3g_4^2} \bar{\ell}'_L \gamma^\mu \ell'_L \right) Z'_\mu
 \end{aligned}$$



requires the phenomenological limit
 $g_4 \gg g_3 \simeq g_s \gg g_1 \simeq g_Y$

Key phenomenological features

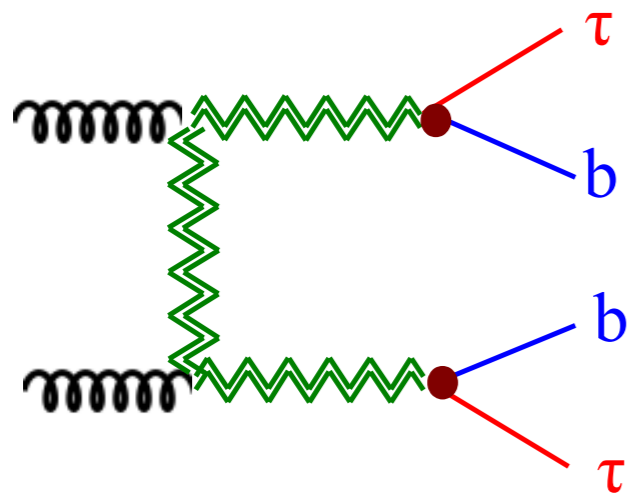
1. LQ couples dominantly to 3rd generation LH fields (can satisfy Zürich's EFT criteria)
2. Down-alignment to avoid tree-level FCNC in the down sector
3. Suppressed Z' and g' couplings to light generations
4. B and L accidental global symmetries as in the SM ($m_\nu = 0$)

$$\mathcal{O}_5 = \frac{1}{\Lambda_L} \ell' \ell' H H \quad \Lambda_L \gg v$$

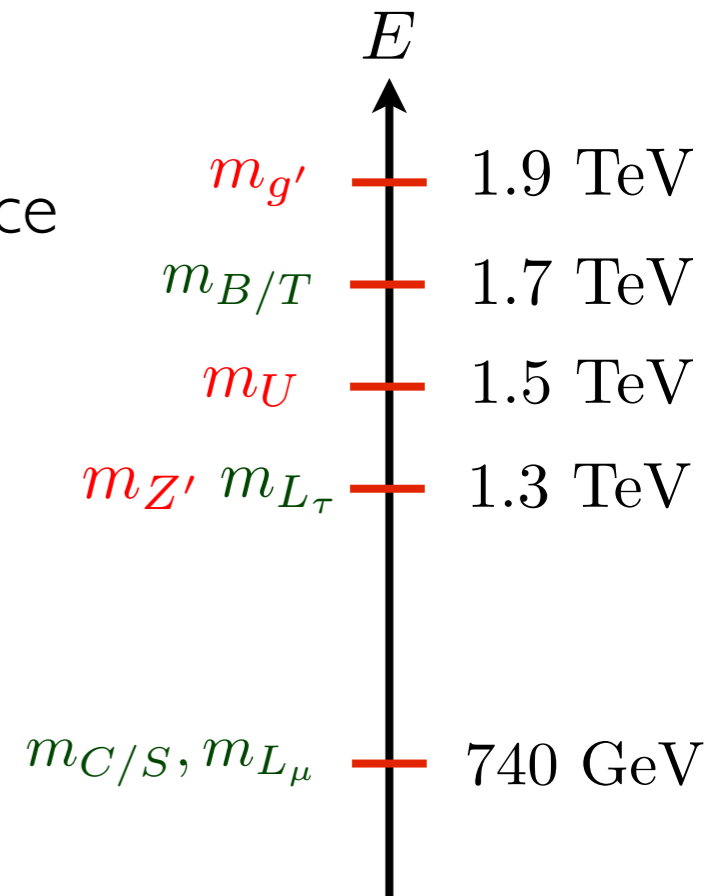
High- p_T searches

- LQ pair production via QCD

- 3rd generation final states, fixed by anomaly and $SU(2)_L$ invariance



$$\begin{cases} U \rightarrow b\tau^+, & \text{BR} = 50\% \\ U \rightarrow t\bar{\nu}, & \text{BR} = 50\% \end{cases}$$



[CMS search for spin-0, 1703.03995

recast for spin-1 1706.01868 (see also 1706.05033) + Moriond EW update]

$$m_U \gtrsim 1.5 \text{ TeV}$$



LQ mass sets the overall scale: $M_{g'} \simeq \sqrt{2} M_U$ $M_{Z'} \simeq \sqrt{\frac{3}{2}} M_U$

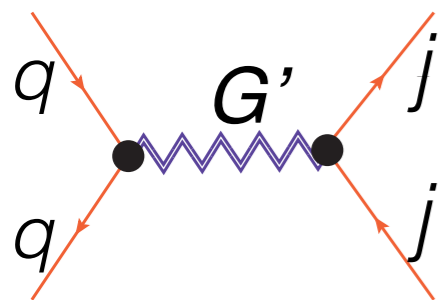
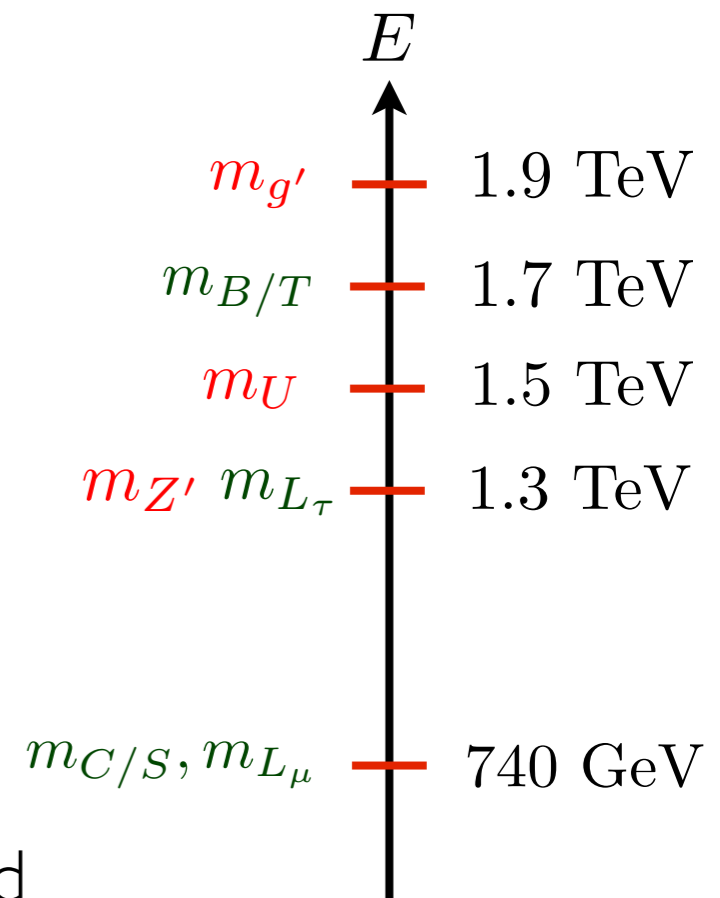
High- p_T searches

- LQ pair production via QCD
- Z' Drell-Yan production enough suppressed

$$\sin \theta_{Z'} = \sqrt{\frac{3}{2}} \frac{g_Y}{g_4} \simeq 0.09 \quad \longrightarrow \quad \text{requires } g_4 \gtrsim 3$$

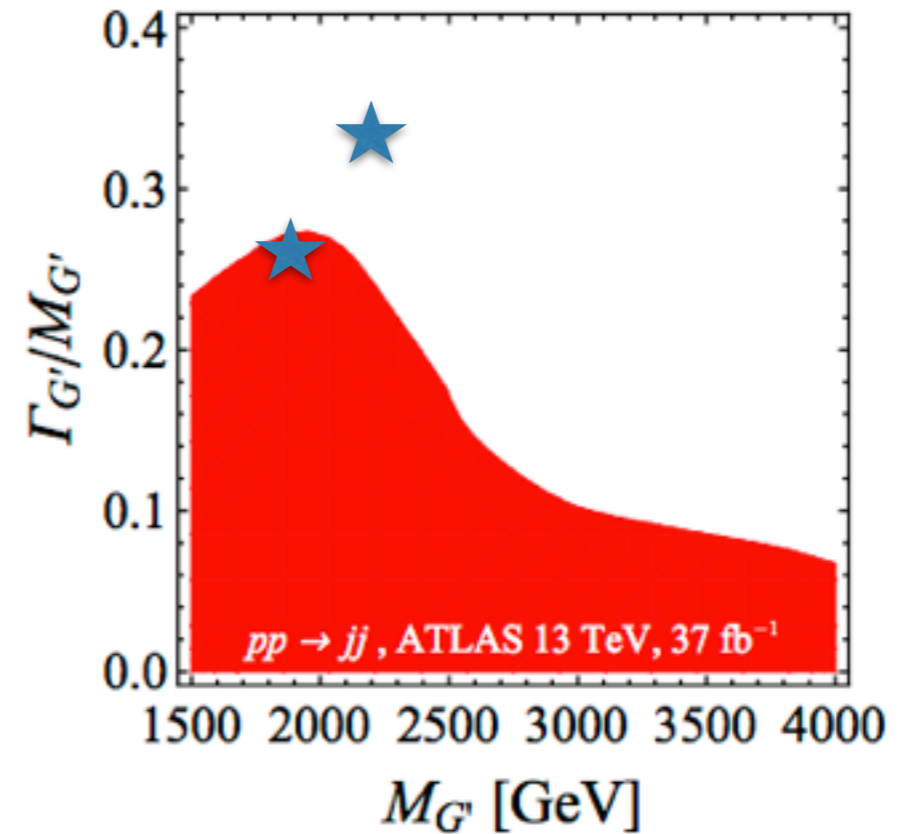
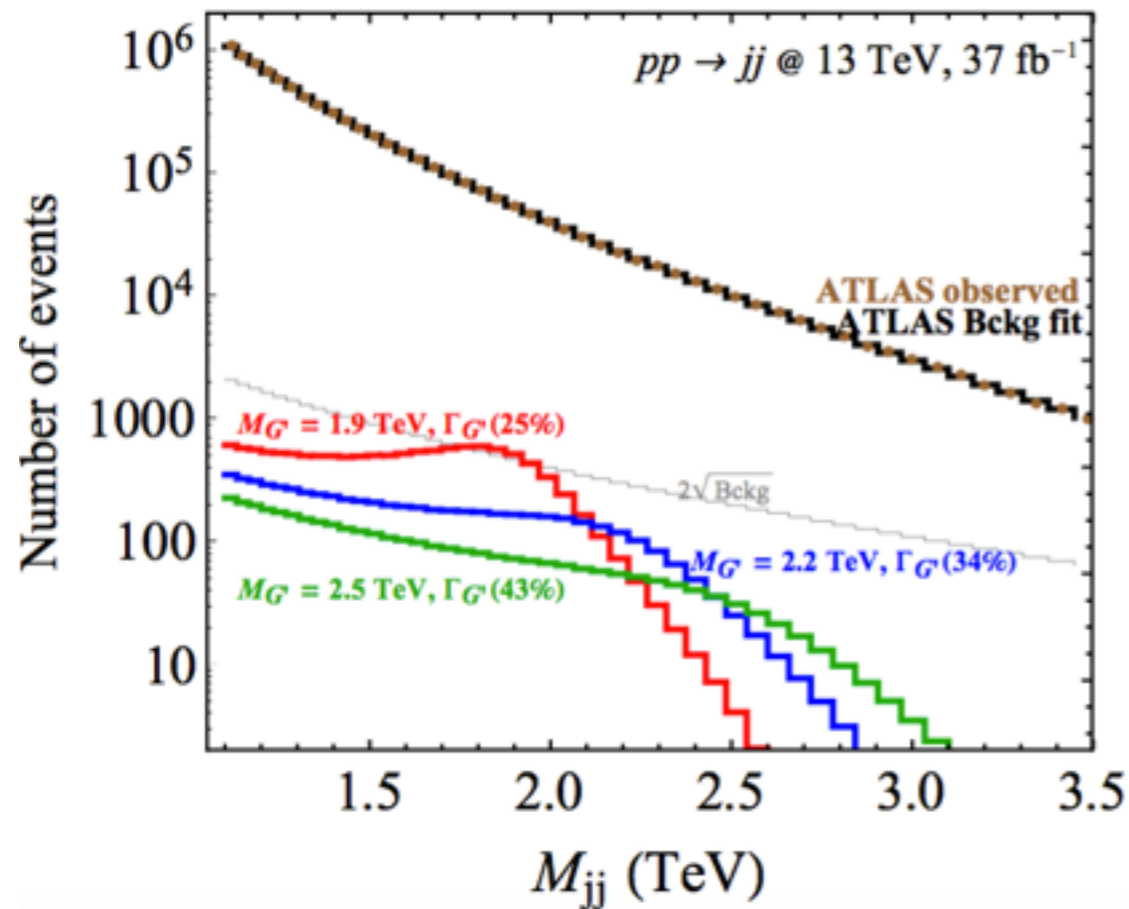
- g' resonant di-jet searches [ATLAS, 1703.09127]

$$\sin \theta_{g'} = \frac{g_s}{g_4} \simeq 0.3 \quad \longrightarrow \quad 2 \text{ TeV coloron naively excluded}$$



High- p_T searches

[LDL, Fuentes-Martin, Greljo, Nardecchia, Renner (work in progress)]



- However, bump-searches loose in sensitivity for large width/mass

$$\frac{\Gamma}{m} \lesssim 15\% \quad (\text{exp. analysis})$$

$$\frac{\Gamma_{g'}}{m_{g'}} \simeq 25\%$$

(unavoidable in our scenario:
large g_4 + extra channel in VLF)

Conclusions

1. We will know much more by ~ 2020 (LHCb + Belle II)
2. Early speculations point to TeV-scale vector leptoquark (R(D)+R(K) explanation)

 who ordered that ?

3. Are flavour anomalies part of a bigger picture ?

 EW naturalness / SM Yukawa puzzle / DM / ...

4. Lesson from UV complete models

 unexpected experimental signatures (coloron, D-mixing, ...)
+ playground to compute correlations

[More pheno to come: LDL, Fuentes-Martin, Greljo, Nardecchia, Renner (work in progress)]


Backup slides

Down-alignment (flavour symmetry)

- Down-alignment to avoid tree-level FCNC in the down sector

- Identify d'_R, Ψ_L, Ψ_R as triplets of the flavour group $U(3)_{d'_R} \equiv U(3)_{\Psi_L} \equiv U(3)_{\Psi_R}$

- $M \propto$ identity

- Y_d and $\lambda_q \propto$ to the same spurion $(\bar{3}, 3)$ of $U(3)_{q'_L} \times U(3)_{d'_R}$  simultaneously diagonalizable

$$\mathcal{M}_d = \begin{pmatrix} \frac{v}{\sqrt{2}} Y_d^{\text{diag}} & \frac{v_3}{\sqrt{2}} \lambda_q \\ 0 & M^{\text{diag}} \end{pmatrix} \quad \lambda_q = \begin{pmatrix} \lambda_q^d & 0 & 0 \\ 0 & \lambda_q^s & 0 \\ 0 & 0 & \lambda_q^b \end{pmatrix} \quad |\lambda_q^{d,s}| \ll |\lambda_q^b|$$

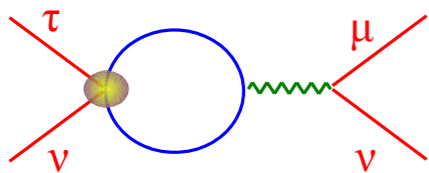
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EFT [details fit]

- 4 parameters fit: $C_S, C_T, \lambda_{bs}^q, \lambda_{\mu\mu}^\ell$ ($\lambda_{bb}^q = \lambda_{\tau\tau}^\ell = 1$) [Zürich's guide for combined explanations, 1706.07808]

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{SM}} - \frac{1}{v^2} \lambda_{ij}^q \lambda_{\alpha\beta}^\ell \left[C_T (\bar{Q}_L^i \gamma_\mu \sigma^a Q_L^j) (\bar{L}_L^\alpha \gamma^\mu \sigma^a L_L^\beta) + C_S (\bar{Q}_L^i \gamma_\mu Q_L^j) (\bar{L}_L^\alpha \gamma^\mu L_L^\beta) \right]$$



LH Z- τ - τ coupling

LH Z- ν - ν coupling

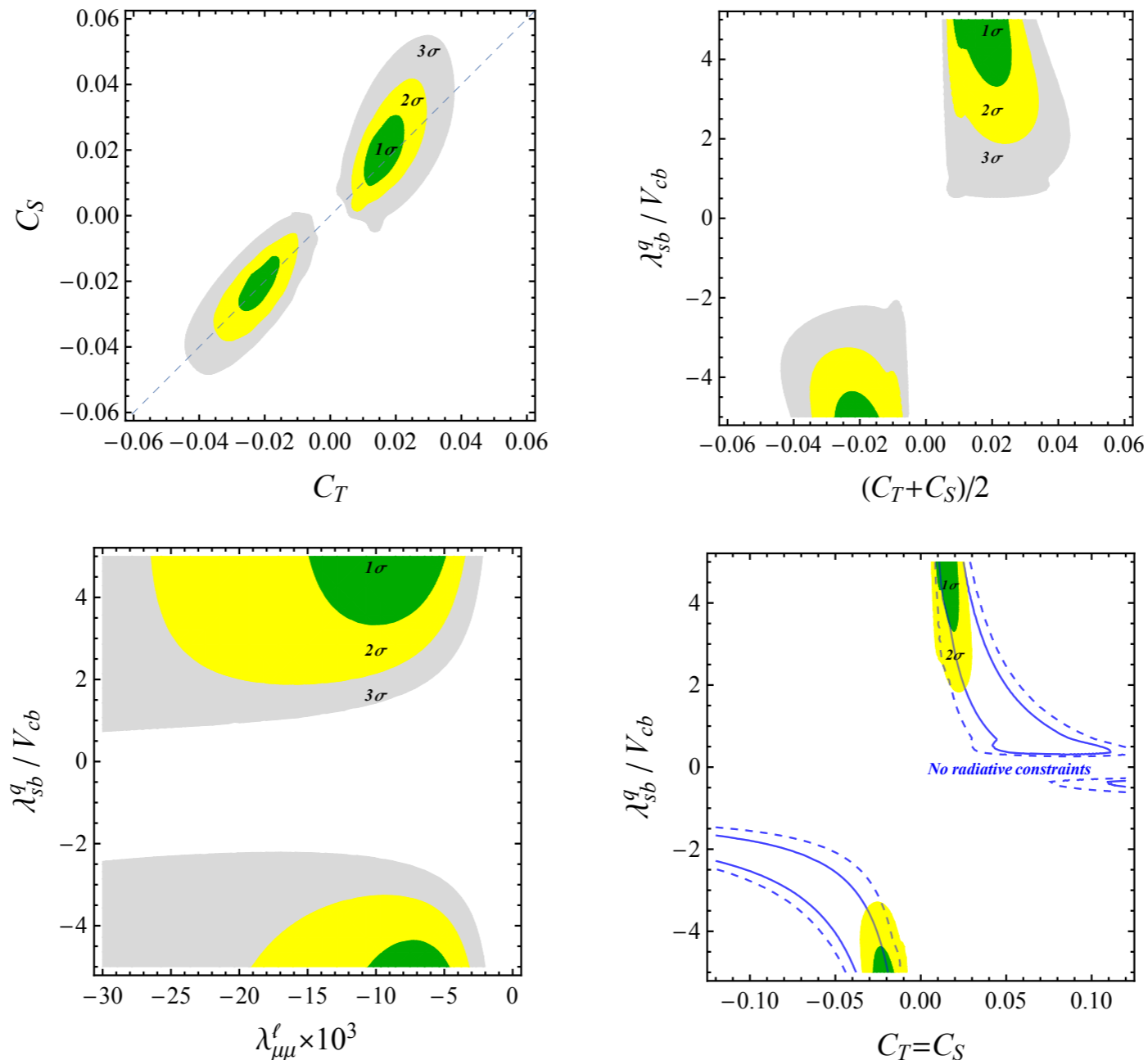
LFUV in τ decays

LFV in τ decays

Observable	Experimental bound	Linearised expression
$R_{D^{(*)}}^{\tau\ell}$	1.237 ± 0.053	$1 + 2C_T(1 - \lambda_{sb}^q V_{tb}^*/V_{ts}^*)(1 - \lambda_{\mu\mu}^\ell/2)$
$\Delta C_9^\mu = -\Delta C_{10}^\mu$	-0.61 ± 0.12 [36]	$-\frac{\pi}{\alpha_{\text{em}} V_{tb} V_{ts}^*} \lambda_{\mu\mu}^\ell \lambda_{sb}^q (C_T + C_S)$
$R_{b \rightarrow c}^{\mu e} - 1$	0.00 ± 0.02	$2C_T(1 - \lambda_{sb}^q V_{tb}^*/V_{ts}^*) \lambda_{\mu\mu}^\ell$
$B_{K^{(*)}\nu\bar{\nu}}$	0.0 ± 2.6	$1 + \frac{2}{3} \frac{\pi}{\alpha_{\text{em}} V_{tb} V_{ts}^* C_\nu^{\text{SM}}} (C_T - C_S) \lambda_{sb}^q (1 + \lambda_{\mu\mu}^\ell)$
$\delta g_{\tau_L}^Z$	-0.0002 ± 0.0006	$0.033C_T - 0.043C_S$
$\delta g_{\nu_\tau}^Z$	-0.0040 ± 0.0021	$-0.033C_T - 0.043C_S$
$ g_\tau^W / g_\ell^W $	1.00097 ± 0.00098	$1 - 0.084C_T$
$\mathcal{B}(\tau \rightarrow 3\mu)$	$(0.0 \pm 0.6) \times 10^{-8}$	$2.5 \times 10^{-4} (C_S - C_T)^2 (\lambda_{\tau\mu}^\ell)^2$

EFT [details fit]

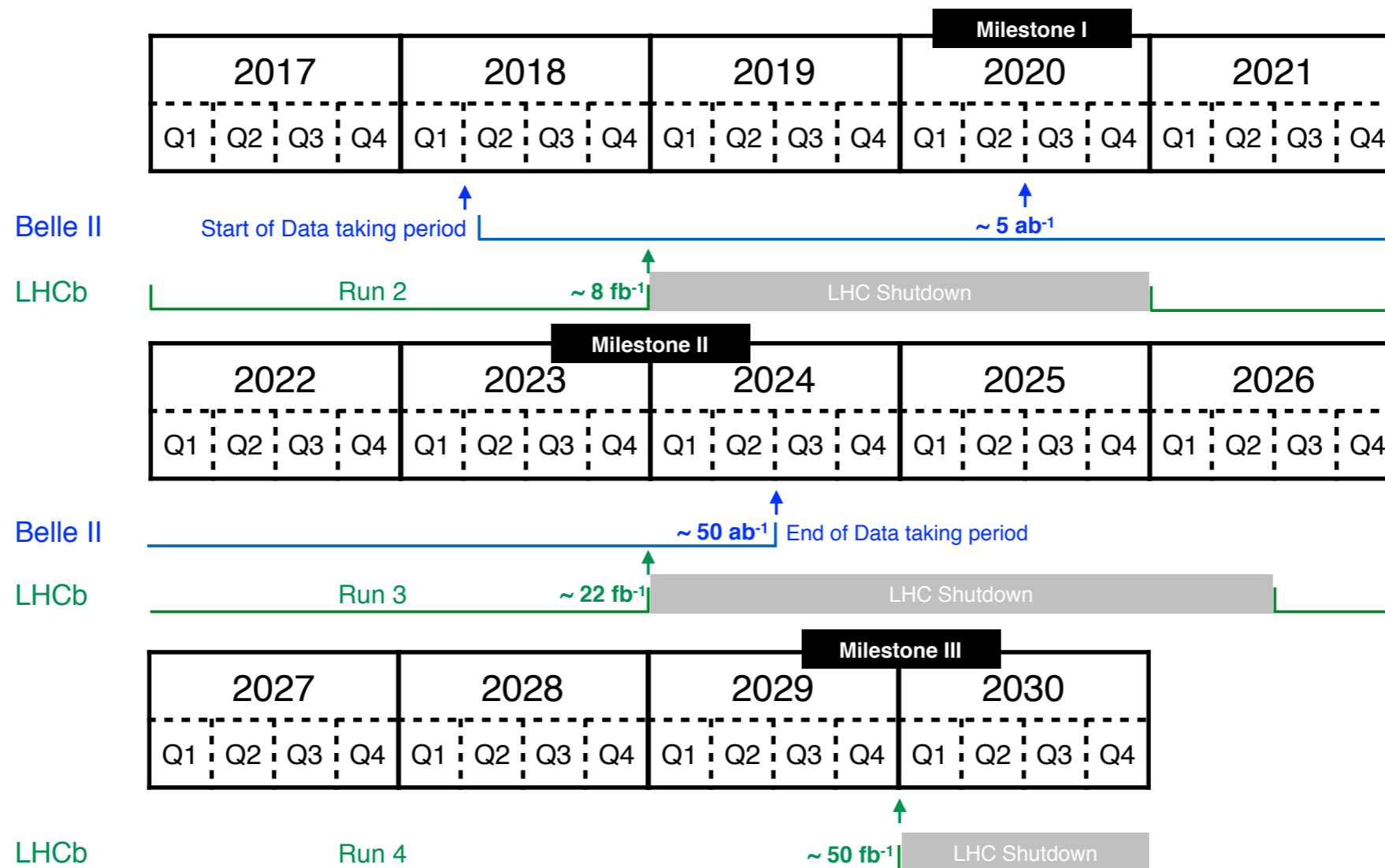
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Future prospects

- LHCb + Belle-II have the potential to fully establish NP in B-anomalies

[Albrecht et al, 1709.10308]



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Belle II		LHCb		
5 ab ⁻¹	50 ab ⁻¹	8 fb ⁻¹	22 fb ⁻¹	50 fb ⁻¹
2020	2024	2019	2024	2030

