

# Precise predictions: the importance of electroweak corrections



**Davide Pagani**

Particle-Physics Seminar

VUB

05-12-2019

# OUTLINE

Introduction: precision physics and EW corrections

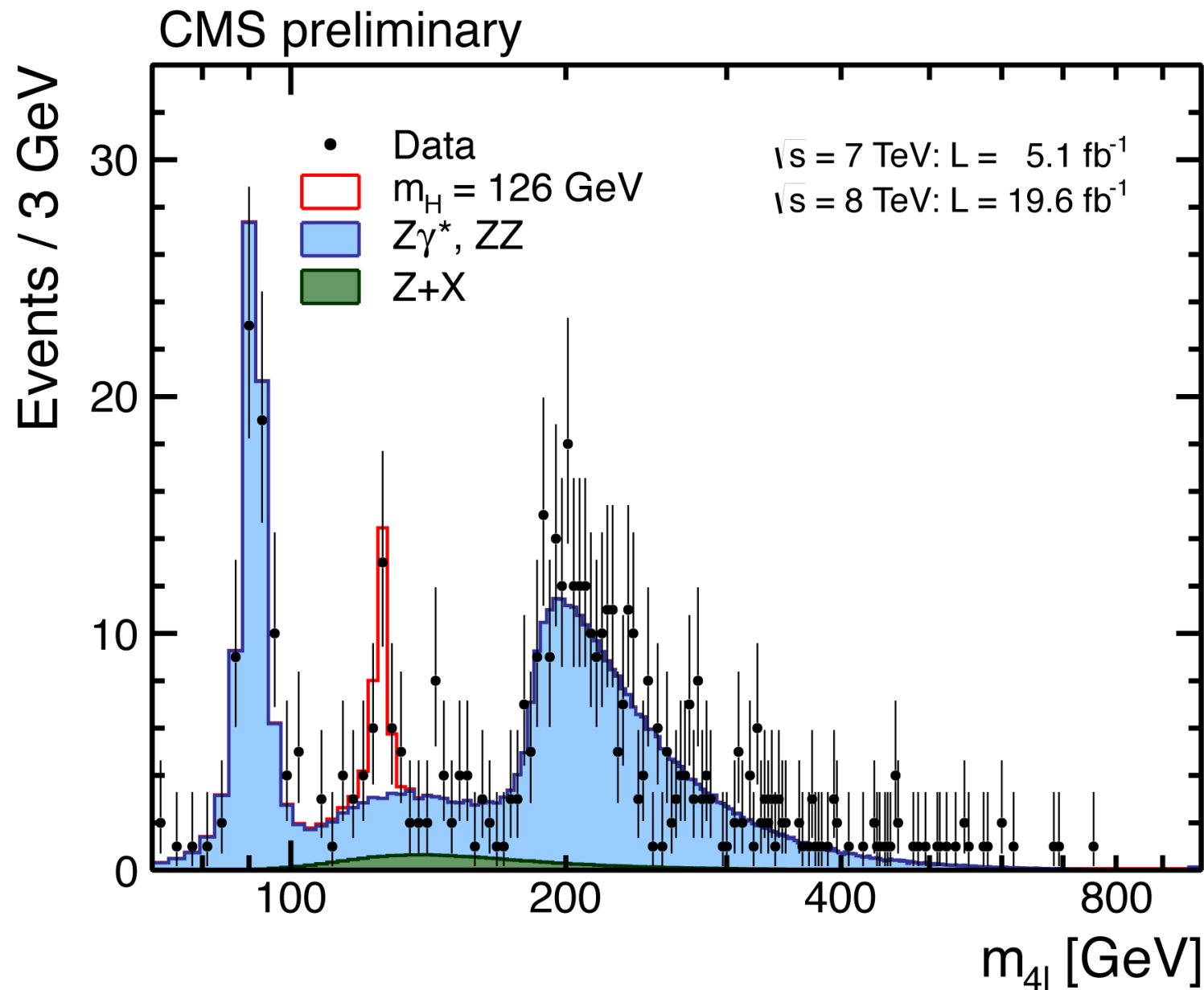
Automation of EW corrections in Madgraph5\_aMC@NLO

Phenomenological results in top-quark physics

Higgs-self couplings from single-Higgs production



# ! DISCLAIMER !



The topic of this talk is **not** very relevant for the identification of resonances from new physics.

**Precise predictions** are fundamental for correctly identifying **non-resonant** new physics effects, setting **exclusion limits** and **fully characterize** and understand both resonant and non-resonant new-physics dynamics.

# Predictions at the LHC

Every prediction at the LHC starts from here:

$$\sigma_{H_1, H_2}(p_1, p_2) = \sum_{i, j} \int dx_1 dx_2 \underbrace{f_i^{(H_1)}(x_1, \mu) f_j^{(H_2)}(x_2, \mu)}_{\text{PDFs}} \underbrace{\hat{\sigma}_{ij}(x_1 p_1, x_2 p_2, \alpha_S(\mu), \mu)}_{\text{Partonic cross sections}}$$

Renormalization/factorization scale

- PDFs are fitted from experimental measurements, only the dependence on  $\mu$  can be calculated in perturbation theory via DGLAP.
- Partonic cross sections can be calculated in perturbation theory via Feynman diagrams.

# Predictions at the LHC

Every prediction at the LHC starts from here:

$$\sigma_{H_1, H_2}(p_1, p_2) = \sum_{i,j} \int dx_1 dx_2 \underbrace{f_i^{(H_1)}(x_1, \mu) f_j^{(H_2)}(x_2, \mu)}_{\text{PDFs}} \underbrace{\hat{\sigma}_{ij}(x_1 p_1, x_2 p_2, \alpha_S(\mu), \mu)}_{\text{Partonic cross sections}}$$

Renormalization/factorization scale

- PDFs are fitted from experimental measurements, only the dependence on  $\mu$  can be calculated in perturbation theory via DGLAP.
- Partonic cross sections can be calculated in perturbation theory via Feynman diagrams.

## Precise predictions at the LHC: for what?

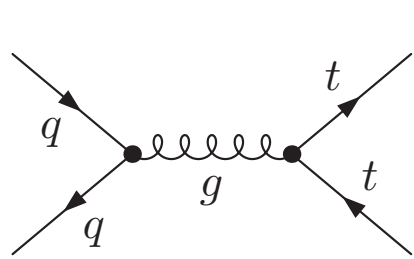
- More precise predictions for the total cross sections. (Total normalization)
- More precise differential distributions. (Kinematic-dependent corrections)
- Reduction of  $\mu$  dependence. (Theoretical accuracy)

Methods/  
Approximations

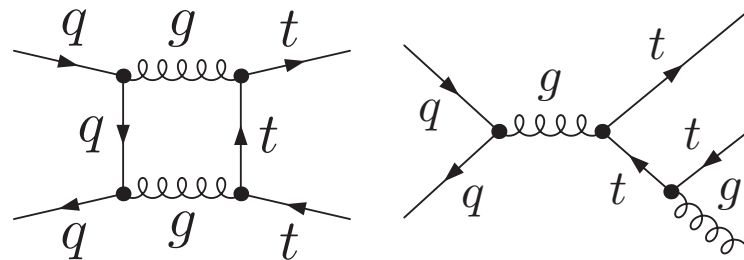
Fixed orders, Resummation, RGE, Parton Shower, Matching, Merging .....

# Fixed Order calculations

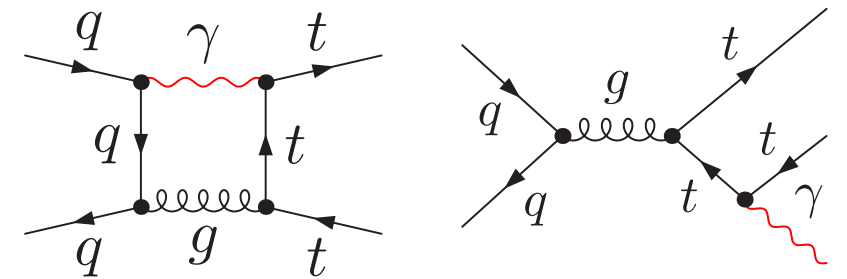
In the SM, contributions to the **partonic cross section** can be organized according to the powers of  $\alpha_s$  and  $\alpha$  (number of loop corrections and real emissions).



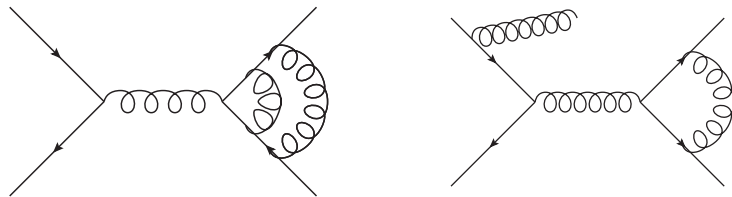
Born LO



NLO QCD  
 $\mathcal{O}(\alpha_s)$  corrections



NLO EW  
 $\mathcal{O}(\alpha)$  corrections



NNLO QCD  
 $\mathcal{O}(\alpha_s^2)$  corrections

NNLO EW,  
NNNLO QCD

.....

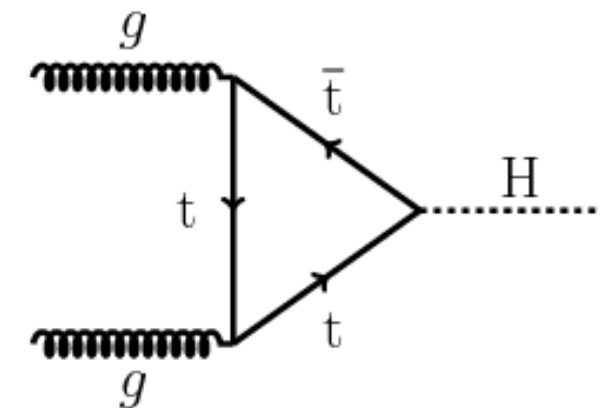
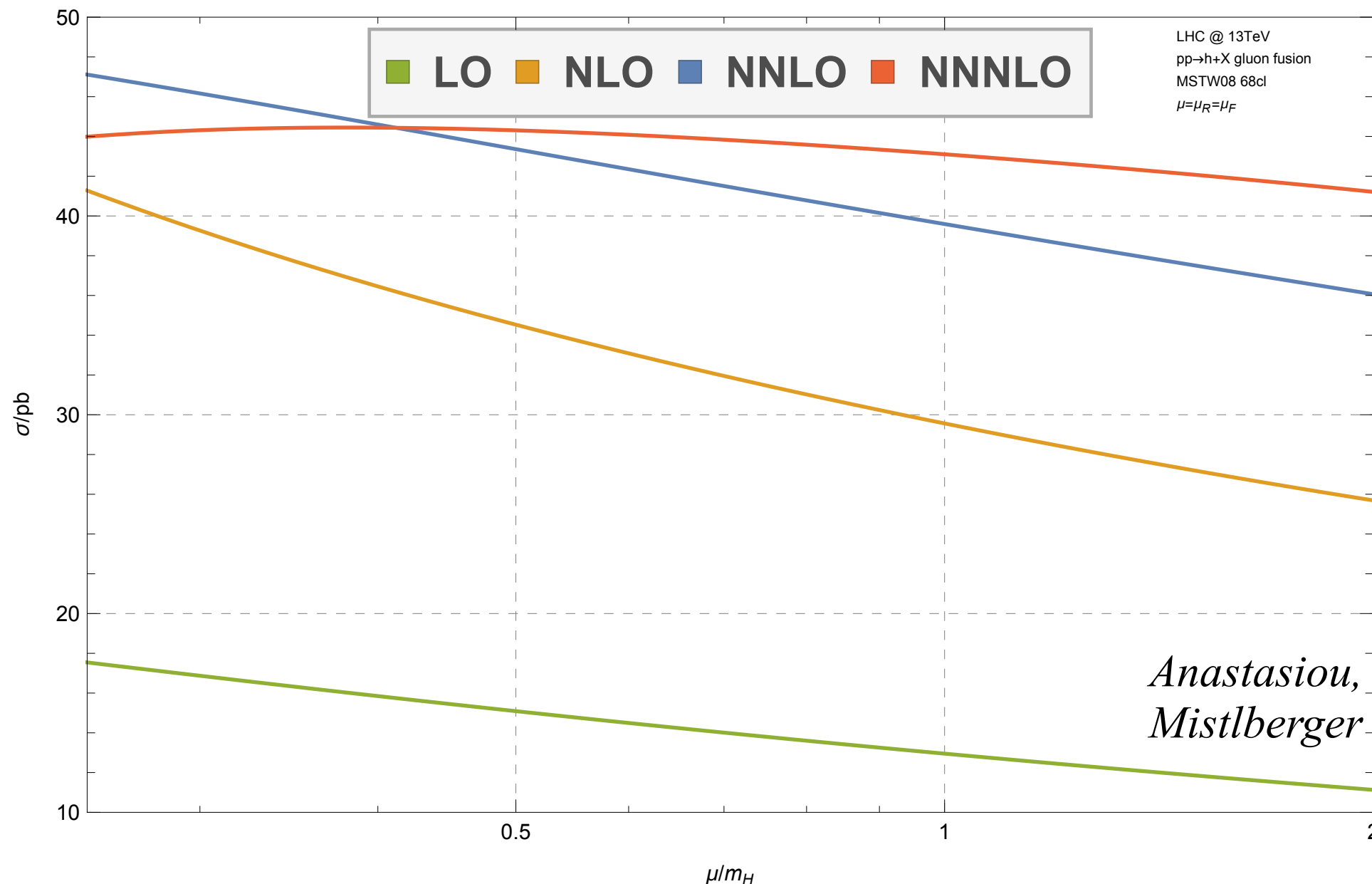
At the LHC, QCD is everywhere.  
Nowadays, a “standard” prediction in the SM is at NLO QCD accuracy.

NNLO QCD is expected to be of the same order of NLO EW  $\alpha_s^2 \sim \alpha$ .

EW corrections grow for large  $p_t$  (Sudakov logs), so they are not flat. Moreover they in general involve all the SM masses and couplings.

# Importance of NNLO (and NNNLO) QCD corrections

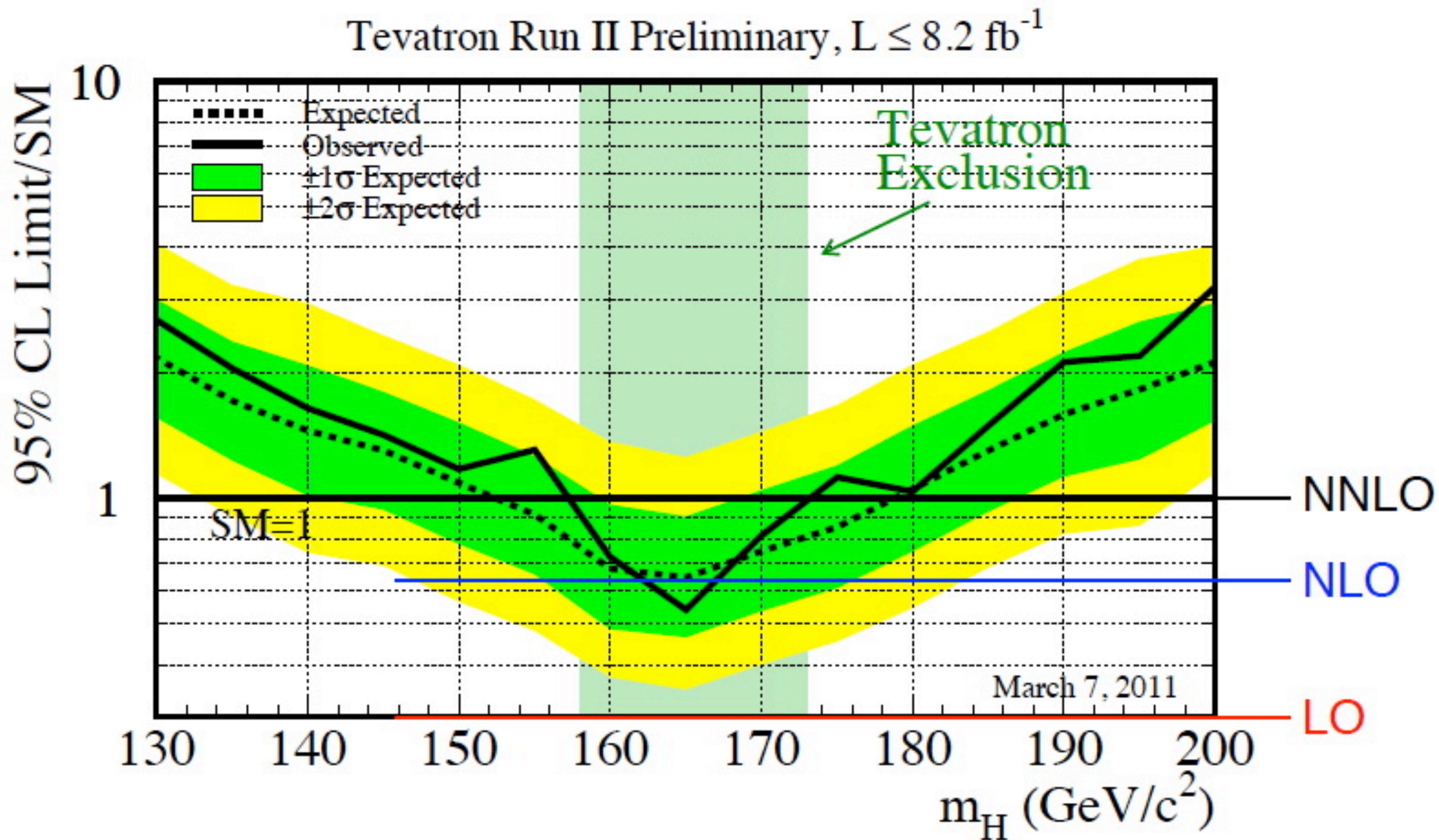
An example: H boson production via gluon fusion.



*Anastasiou, Duhr, Dulat, Herzog, Mistlberger '15*

NLO EW corrections are  $\sim 5\%$ , i.e., larger than the residual QCD scale uncertainty.

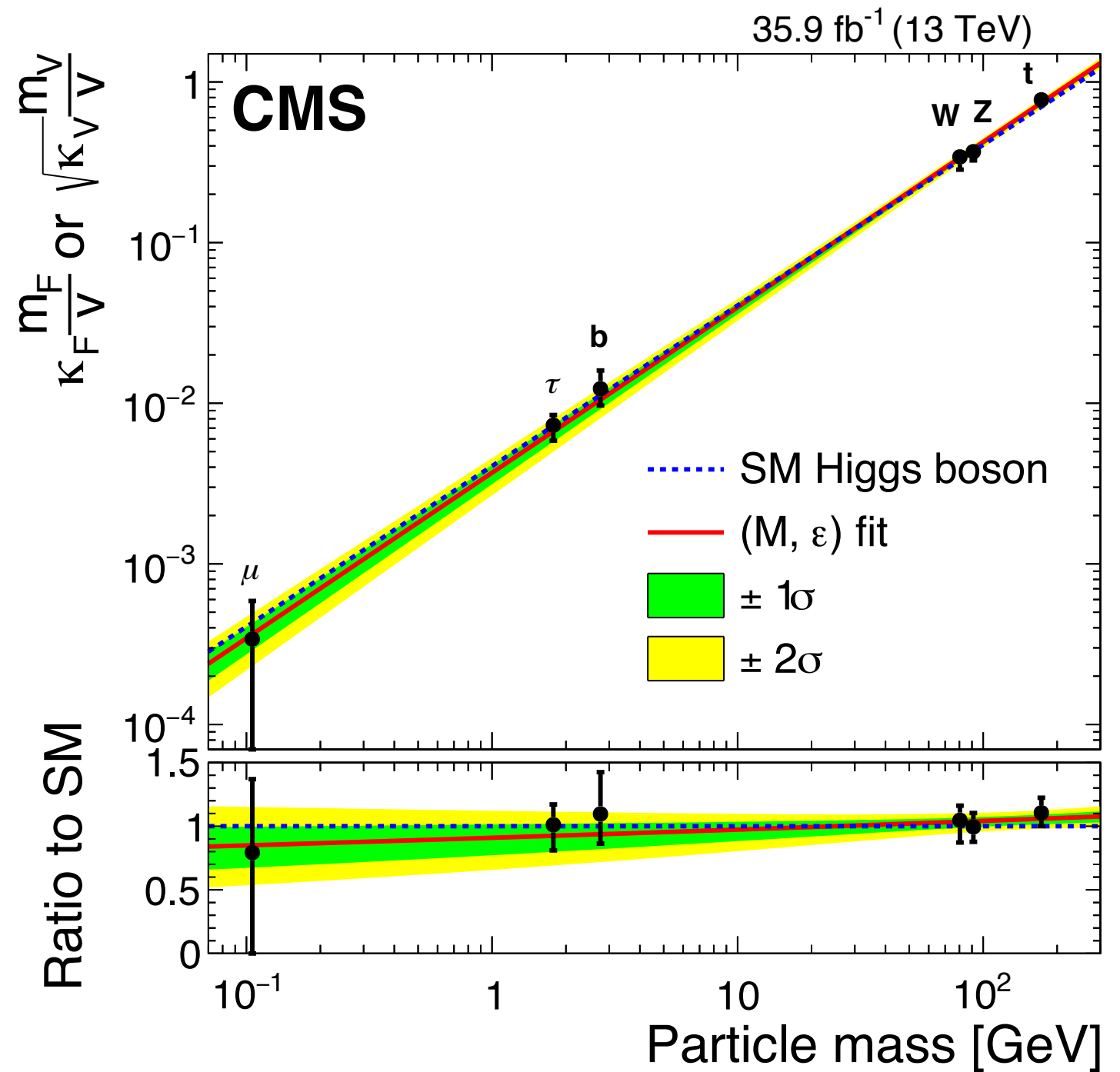
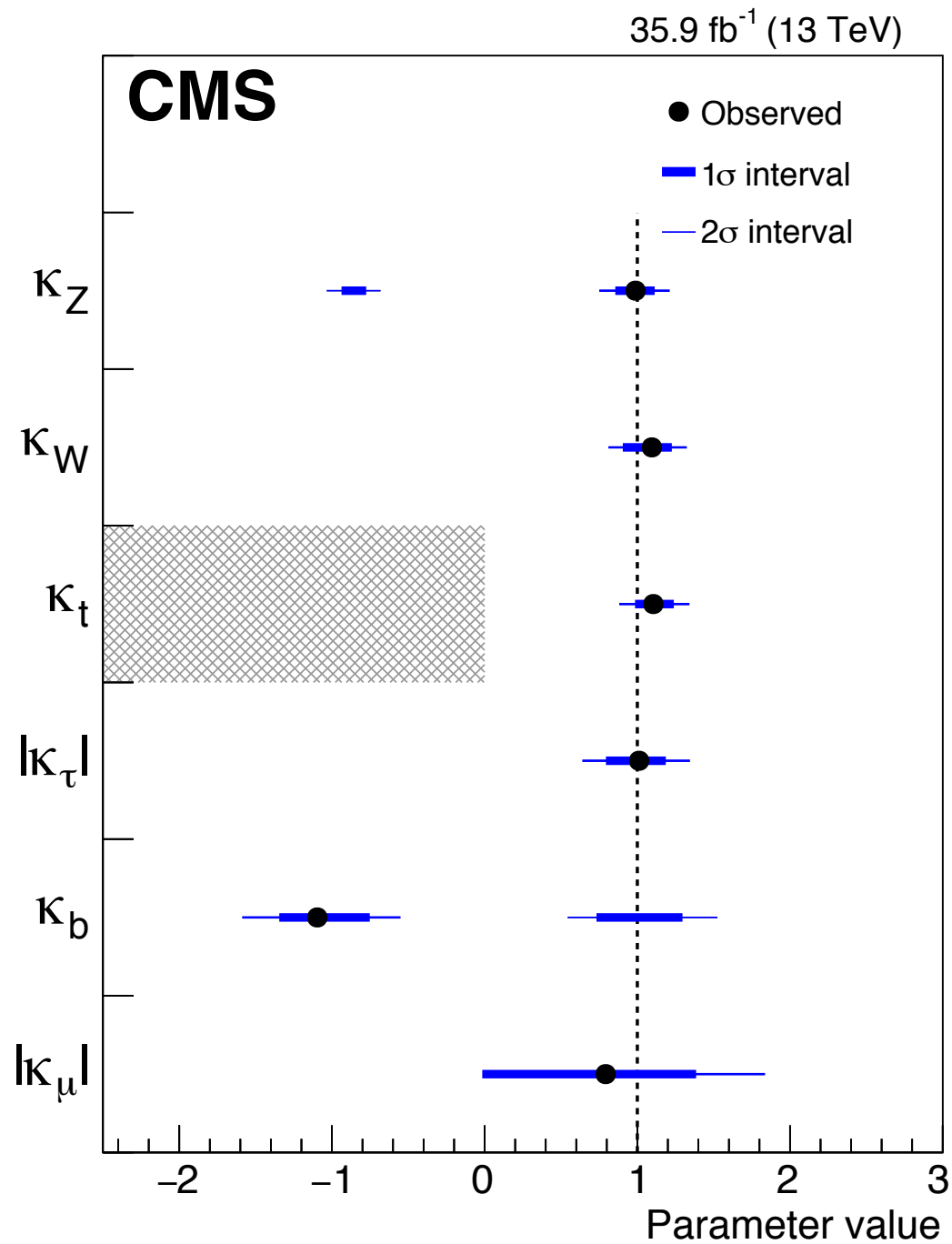
# Importance of NLO and NNLO QCD corrections



be careful : just illustrative example, not very precise



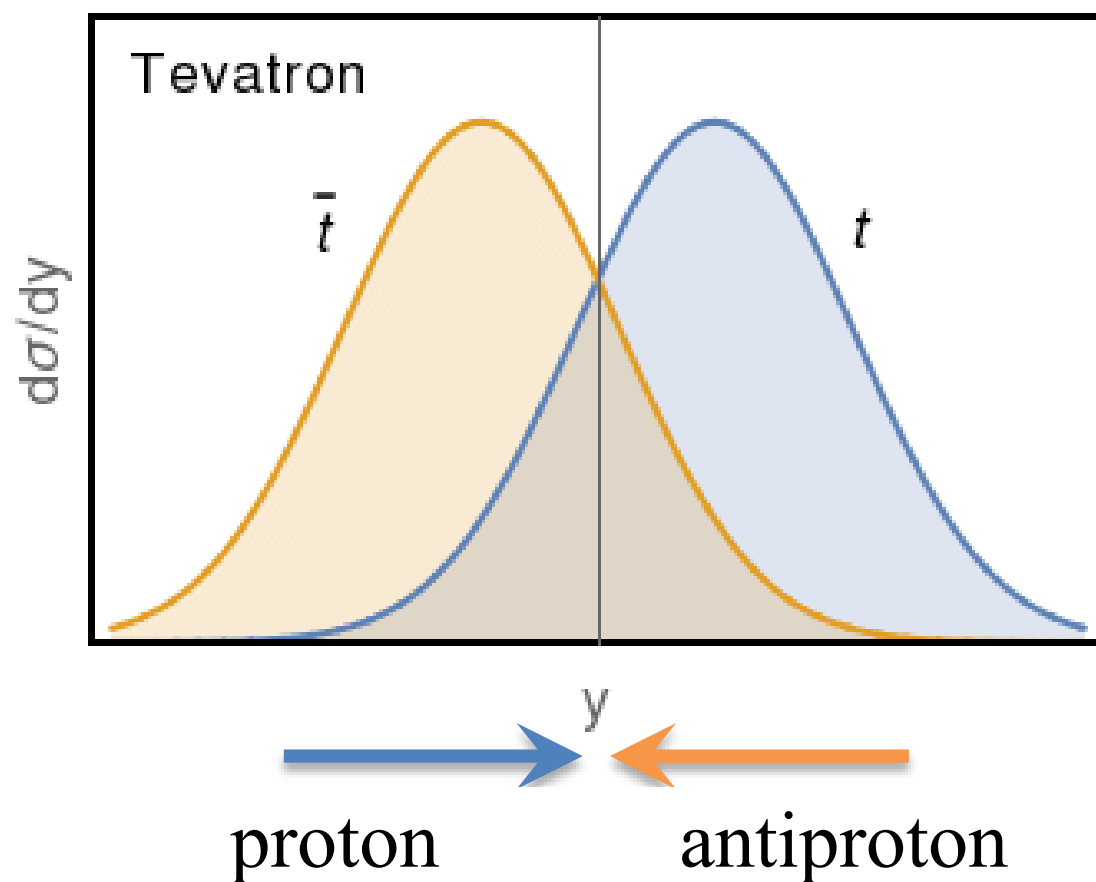
# Higgs boson today: precise measurements of couplings



CMS-HIG-17-031

# Correct interpretation of the (B)SM signal

A recent story from an other hadron collider: **the top-quark forward-backward asymmetry at the Tevatron.**



$$A_{FB}^{p\bar{p}} = \frac{\sigma(y_t > 0) - \sigma(y_t < 0)}{\sigma(y_t > 0) + \sigma(y_t < 0)}$$

D0 and especially CDF measured values for the forward-backward asymmetry that are larger than the SM prediction.

But which SM prediction?



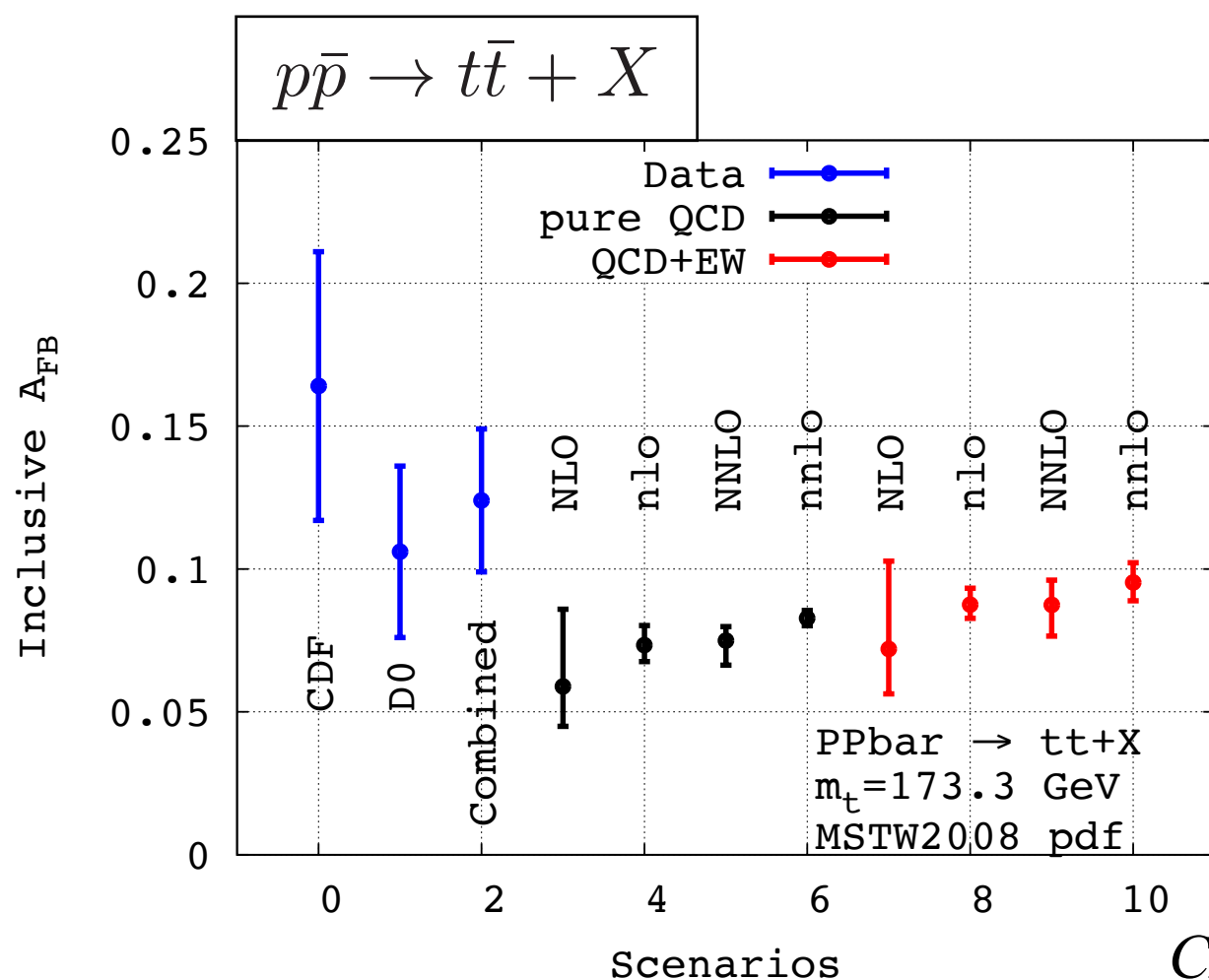
# Correct interpretation of the (B)SM signal

A recent story from an other hadron collider: **the top-quark forward-backward asymmetry at the Tevatron.**

**Surprisingly** (No Sudakov enhancement), the NLO EW induces corrections of order 20-25%.

$$R_{QED}(Q_q) = \frac{\alpha \tilde{N}_1^{QED}}{\alpha_s N_1} = Q_q Q_t \frac{36}{5} \frac{\alpha}{\alpha_s}$$

*DP, Hollik '11*



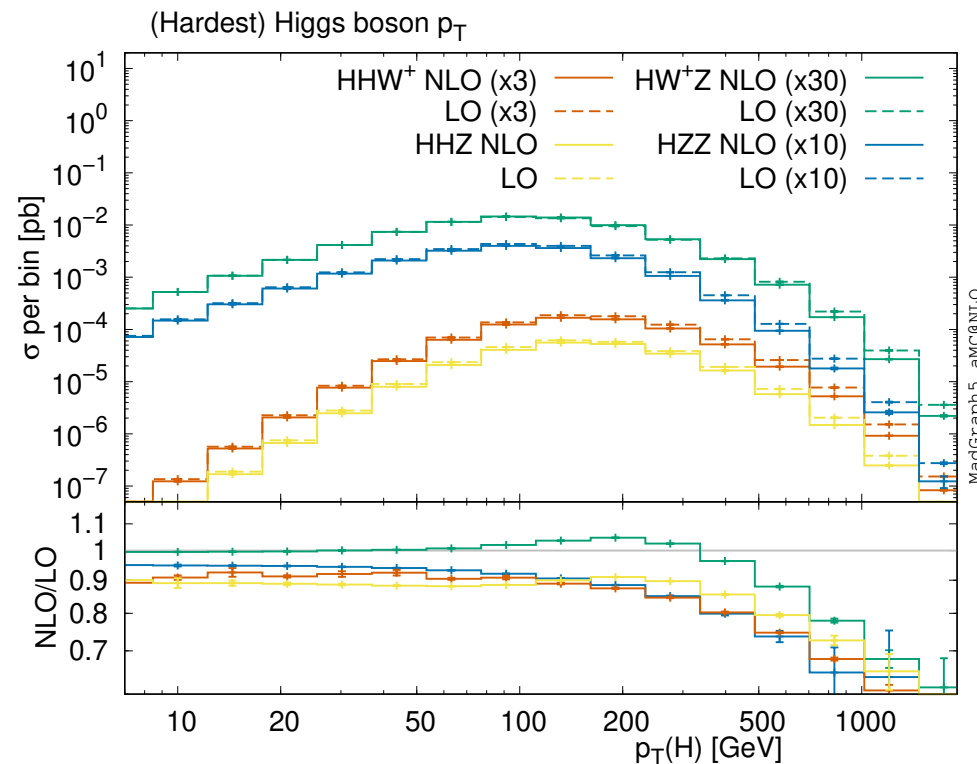
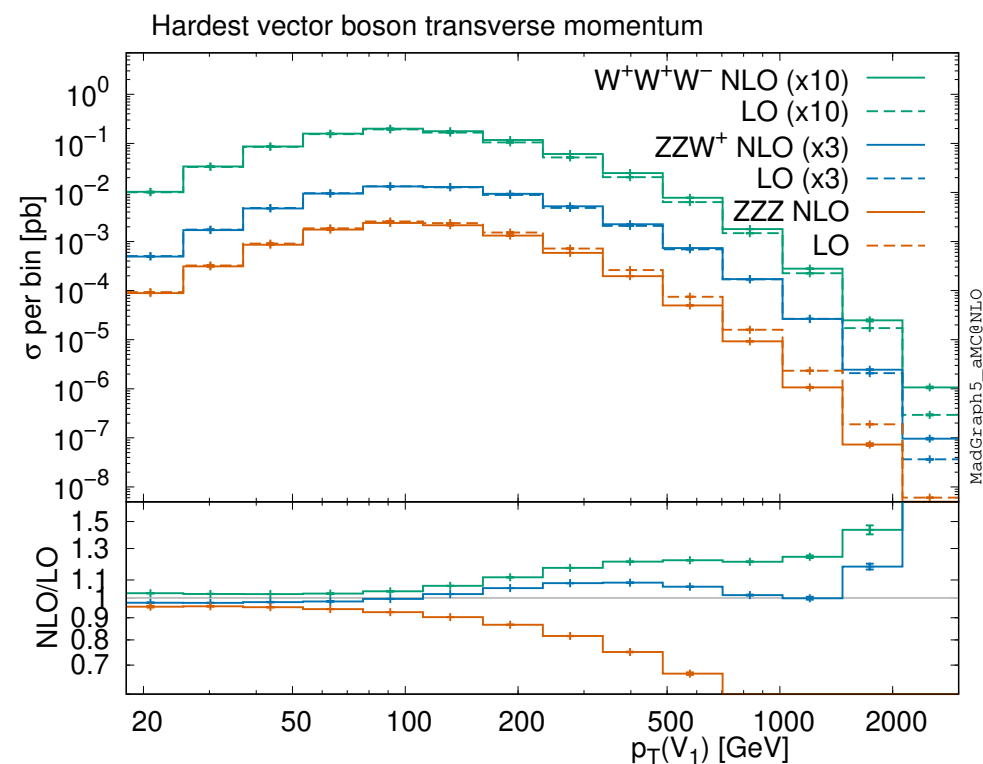
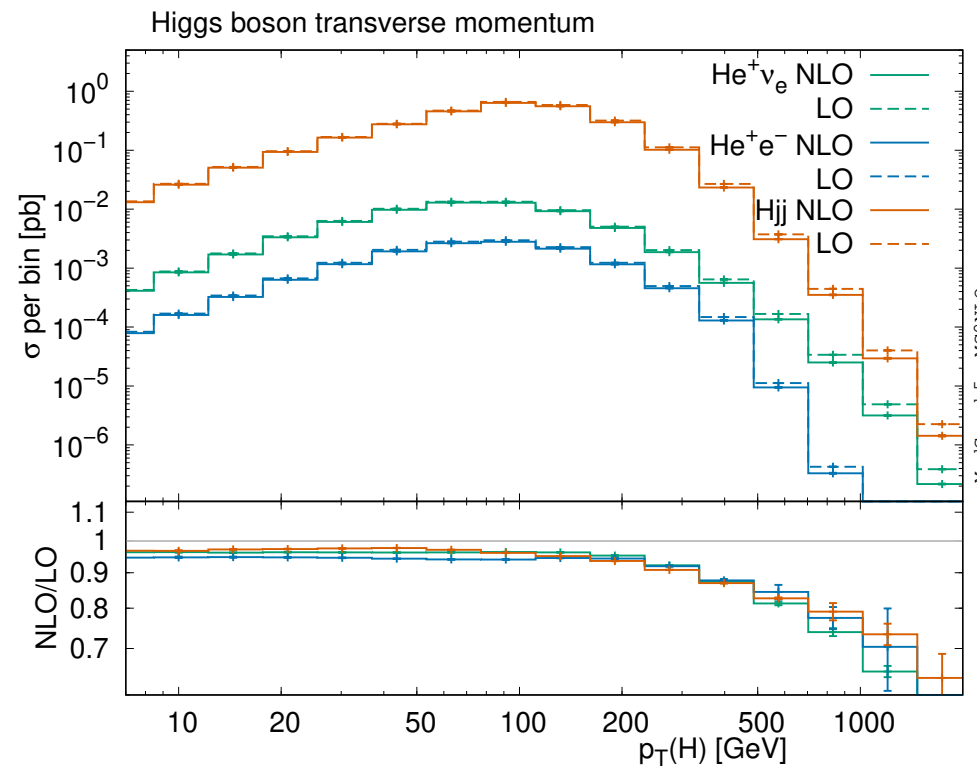
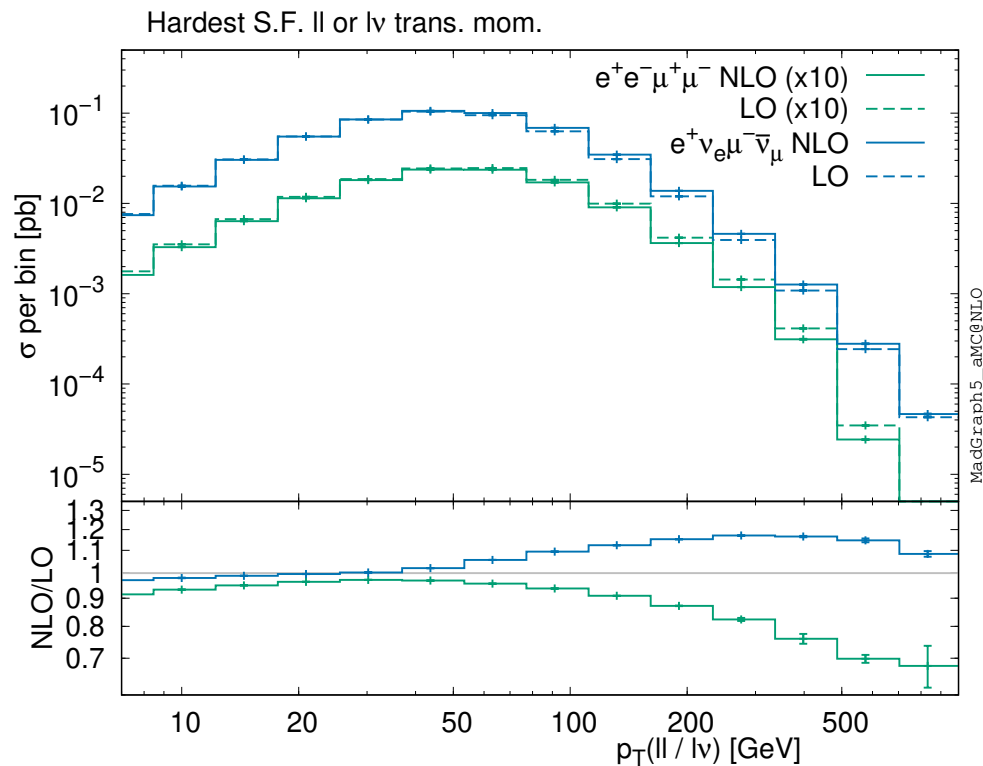
NNLO QCD and NLO EW are essential for a reliable theoretical prediction.

Missing higher-orders in the theoretical predictions may be misinterpreted as BSM signals.

*Czakon, Fiedler, Mitov '14*

# Sudakov enhancement

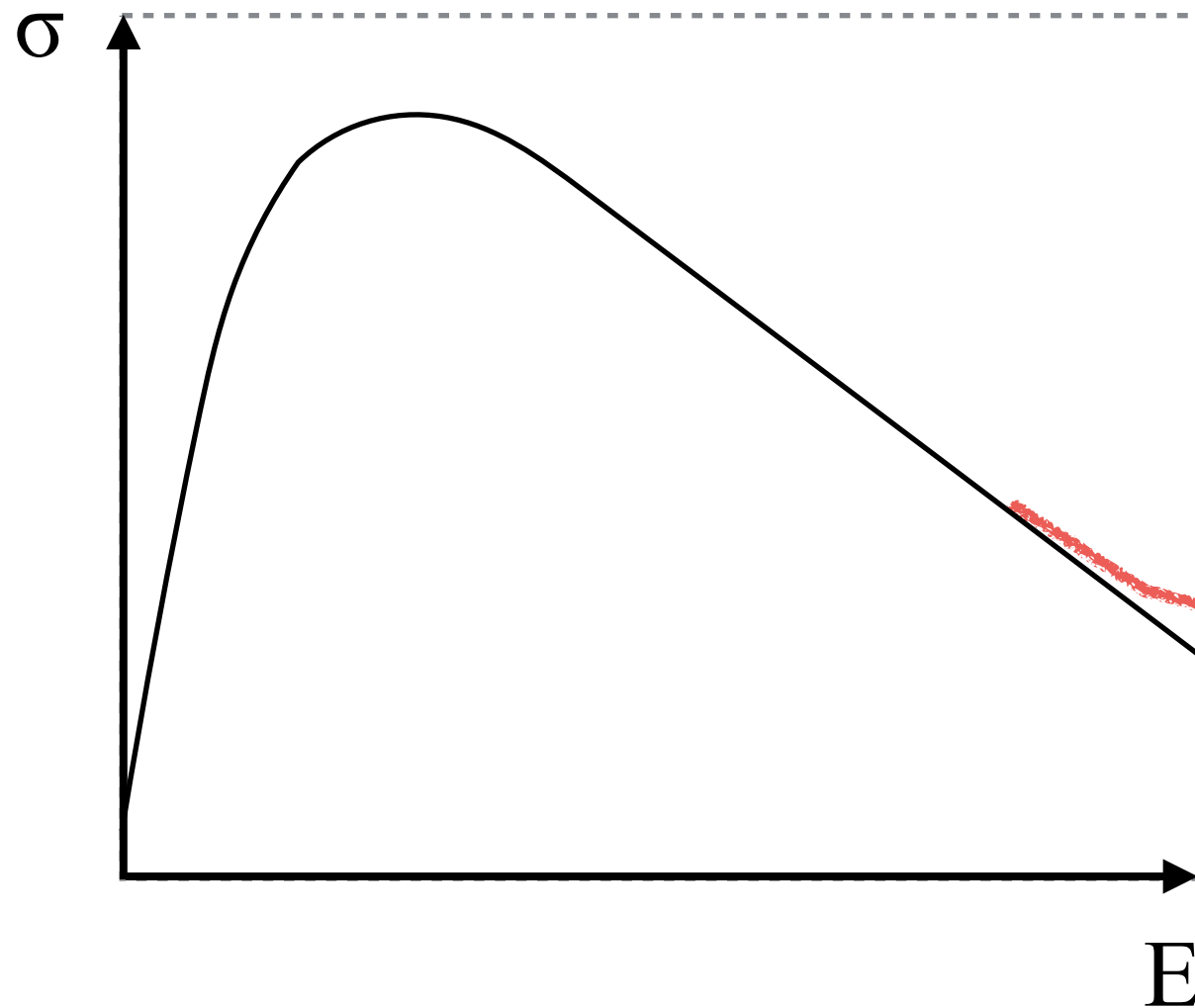
Not surprisingly, weak corrections at large scales are not negligible for a general process due to the Sudakov Logarithms  $\sim \alpha \ln^2 \left( \frac{s}{M_W^2} \right)$ .



*Frederix, Frixione,  
Hirschi, DP, Shao,  
Zaro '18*

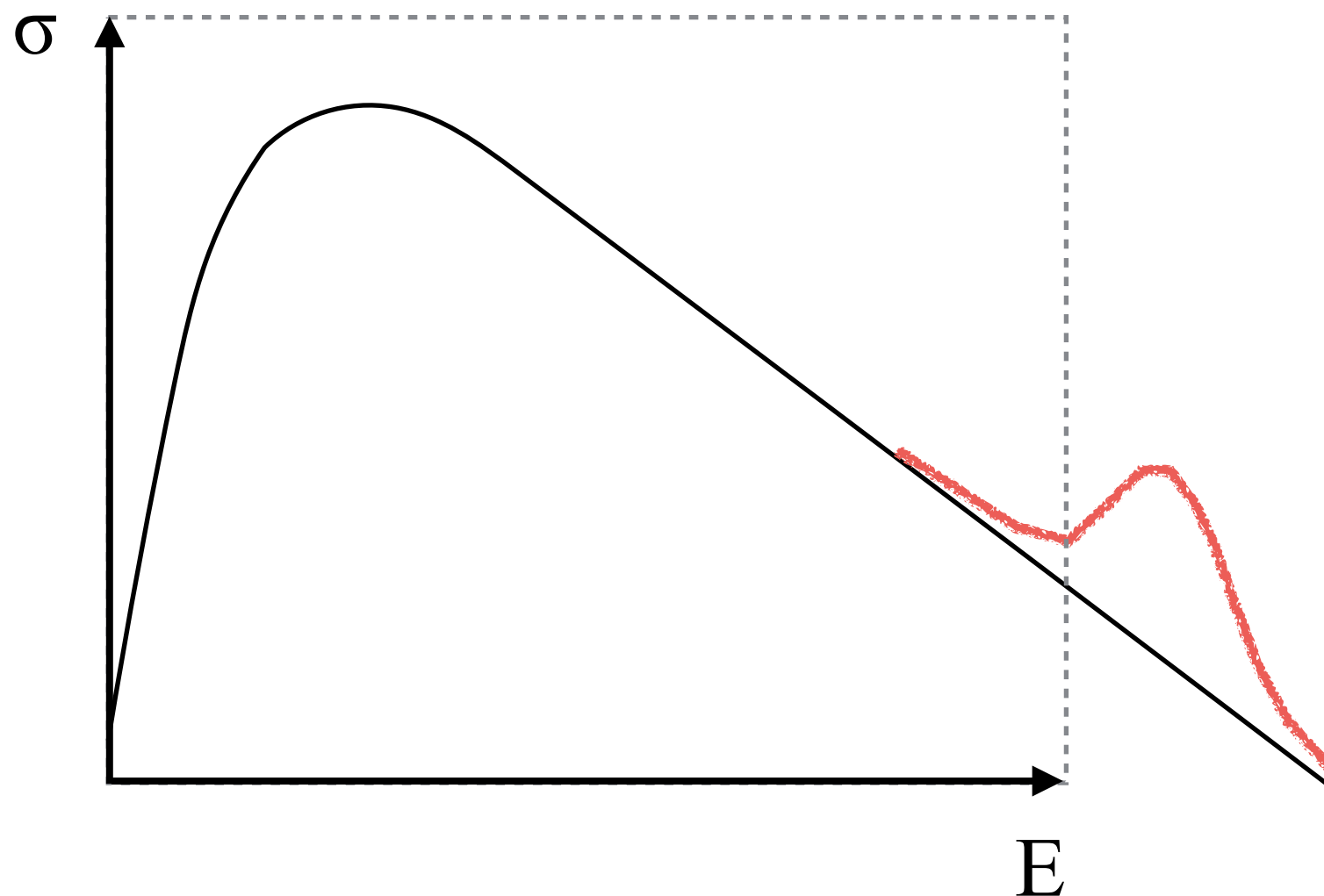


# New Physics from differential distributions



With higher luminosity (and higher energy), at the LHC the accuracy of all measurements will in general increase, especially in the tail of distributions.

# New Physics from differential distributions



With higher luminosity (and higher energy), at the LHC the accuracy of all measurements will in general increase, especially in the tail of distributions.

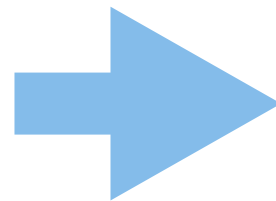
Precise predictions are necessary for the current and future measurements at the LHC, especially if no clear sign of new physics will appear. In order to match the experimental precision, NLO EW corrections are essential.

# Automation of NLO corrections in Madgraph5\_aMC@NLO

What do we mean with automation of EW corrections?

The possibility of calculating **QCD** and **EW** corrections for SM processes (matched to shower effects) with a process-independent approach.

```
generate process [QCD]
output process_QCD
```



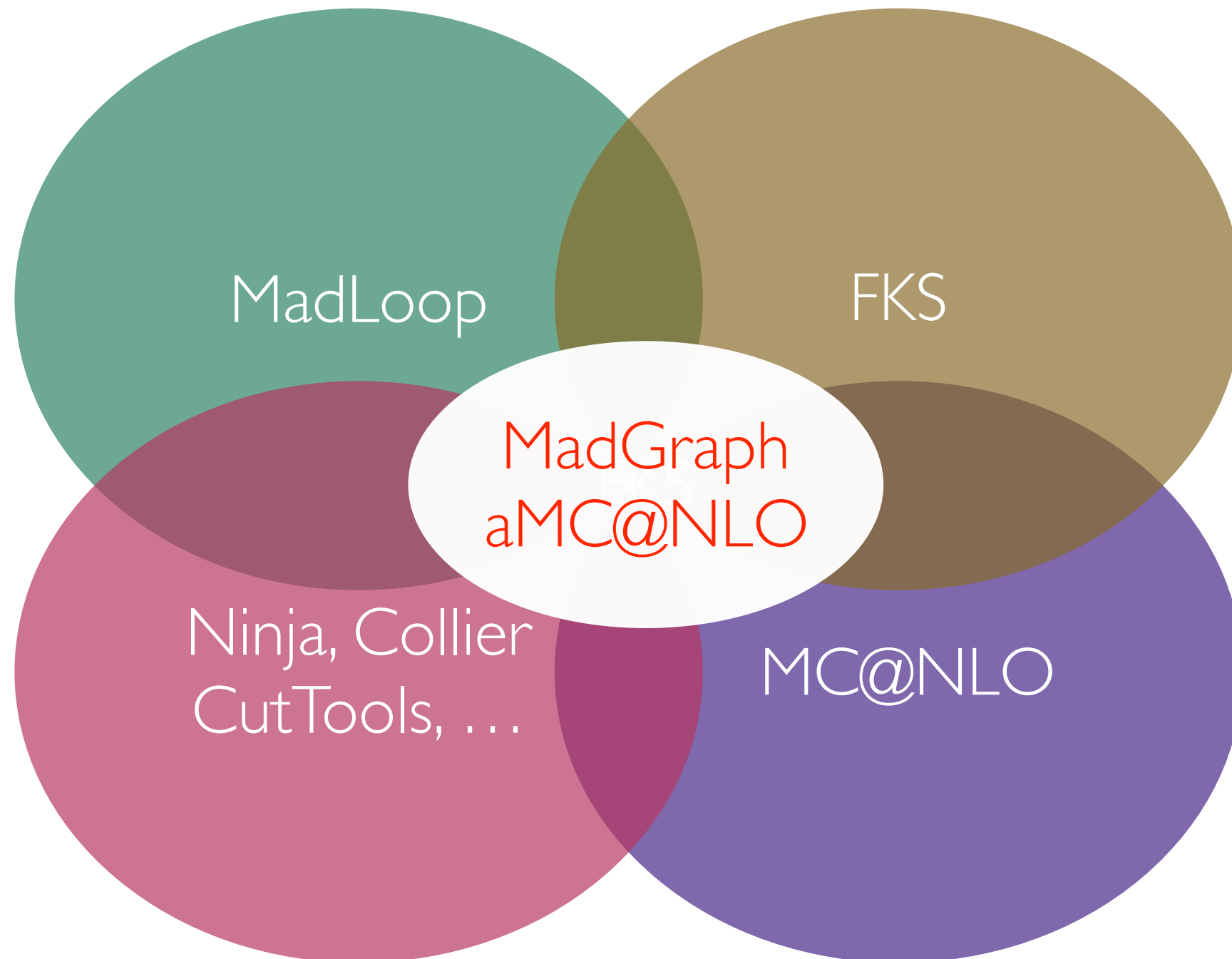
```
generate process [QCD EW]
output process_QCD_EW
```

The automation of NLO QCD has already been achieved, but we need higher precision to match the experimental accuracy at the LHC and future colliders.

- NNLO QCD complete automation is out of our theoretical capabilities at the moment.
- NLO EW and NNLO QCD corrections are of the same order ( $\alpha_s^2 \sim \alpha$ ), but NLO EW corrections **can be automated**. Moreover effects such as Sudakov logarithms or photon FSR can enhance their size.

# Automation of NLO corrections in Madgraph5\_aMC@NLO

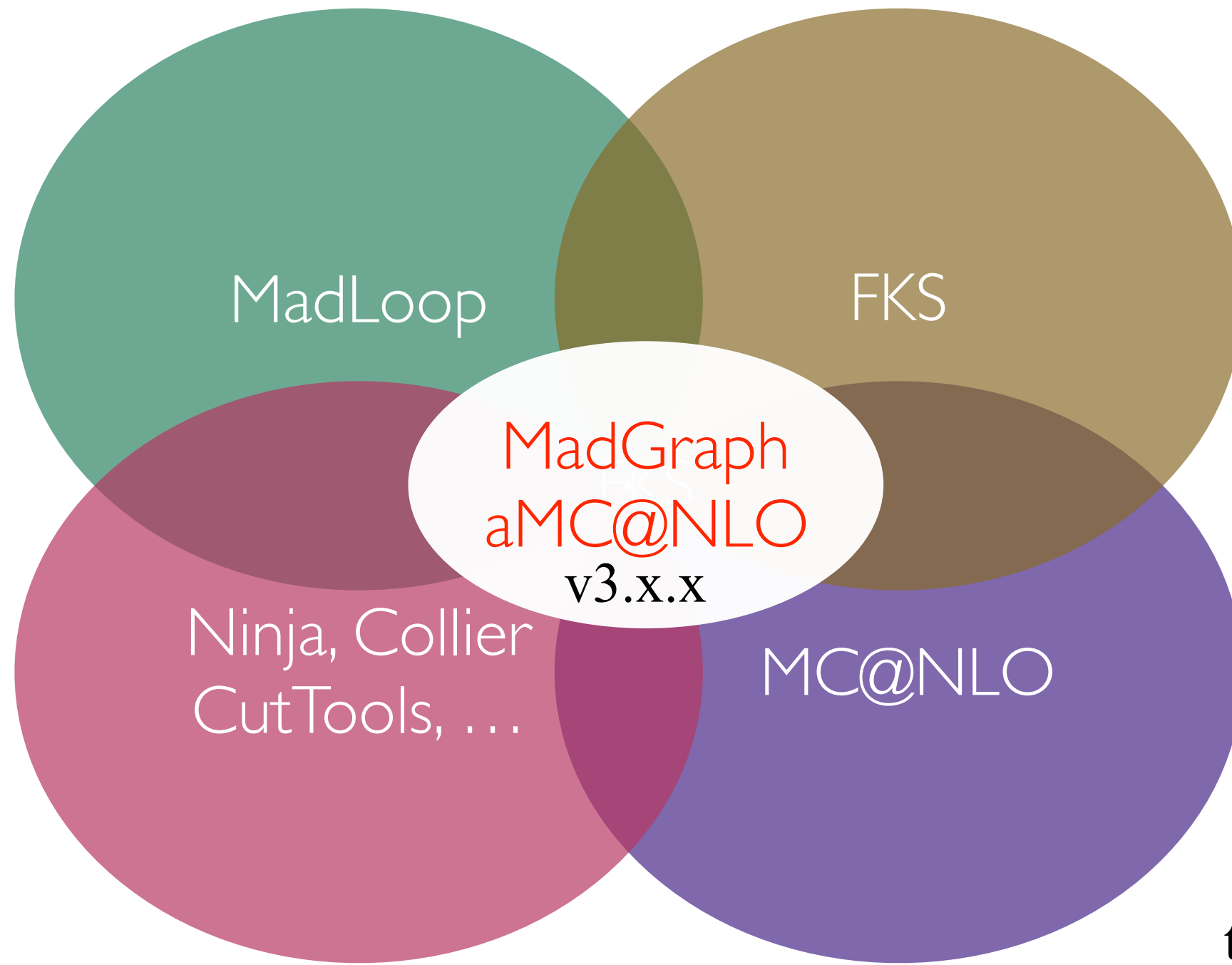
The **complete automation** had already been achieved for **QCD**.



*Alwall, Frederix, Frixione, Hirschi, Maltoni, Mattelaer, Shao, Stelzer, Torrielli, Zaro '14*

# Automation of NLO corrections in Madgraph5\_aMC@NLO

The **complete automation** is now available also for combined **QCD and EW**.



Matching with  
the shower is in  
progress

*Frederix, Frixione, Hirschi, DP, Shao, Zaro '18*



## What is new from QCD to EW?

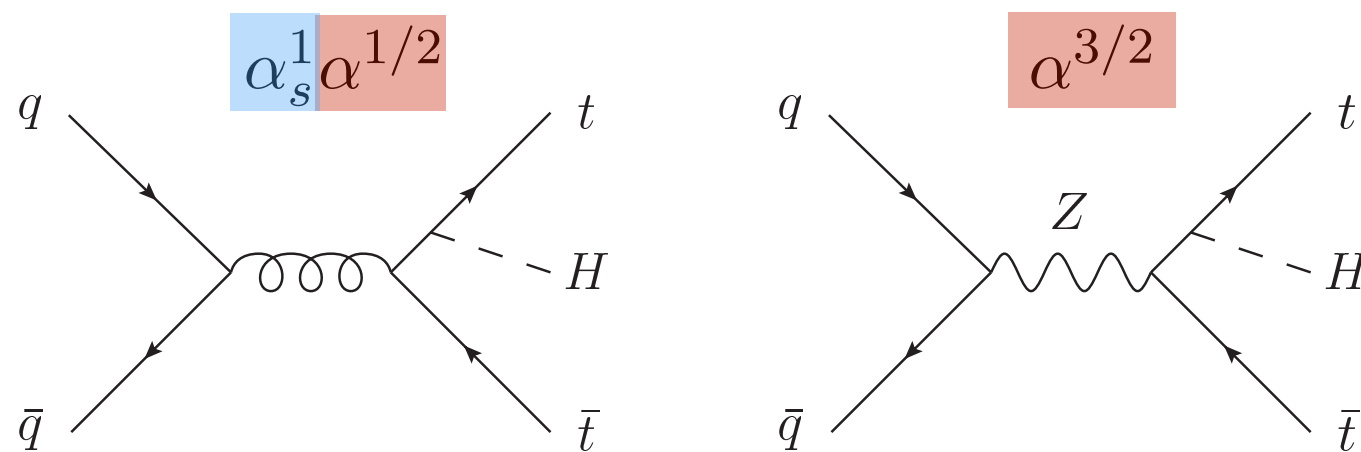
- Many more loop diagrams, involving the photon and the W, Z and H bosons.
- Z, W bosons and top quark intermediate resonances are often involved in a generic process. Complex mass scheme is necessary.
- New R2 and UV counterterms are necessary.
- A richer structure of interferences of tree and one-loop diagrams due to different possible perturbative orders combinations. Same situation for real radiations
- FKS subtractions of singularities has to be extended in order to account for singularities due to photons and the aforementioned richer structure of interferences.
- Jets definitions have to be modified in order to be IR safe.

All these problems have been solved and implemented in the new version (v3) of Madgraph5\_aMC@NLO

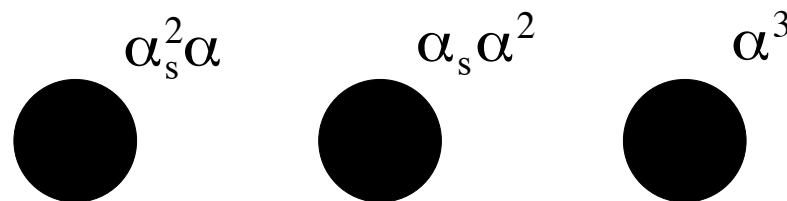
We also provided FKS formulas for fragmentation functions, but they have not been implemented yet. At the moment, NLO EW to FS photons not available.

# Structure of NLO EW-QCD corrections

$t\bar{t}H$   
as example



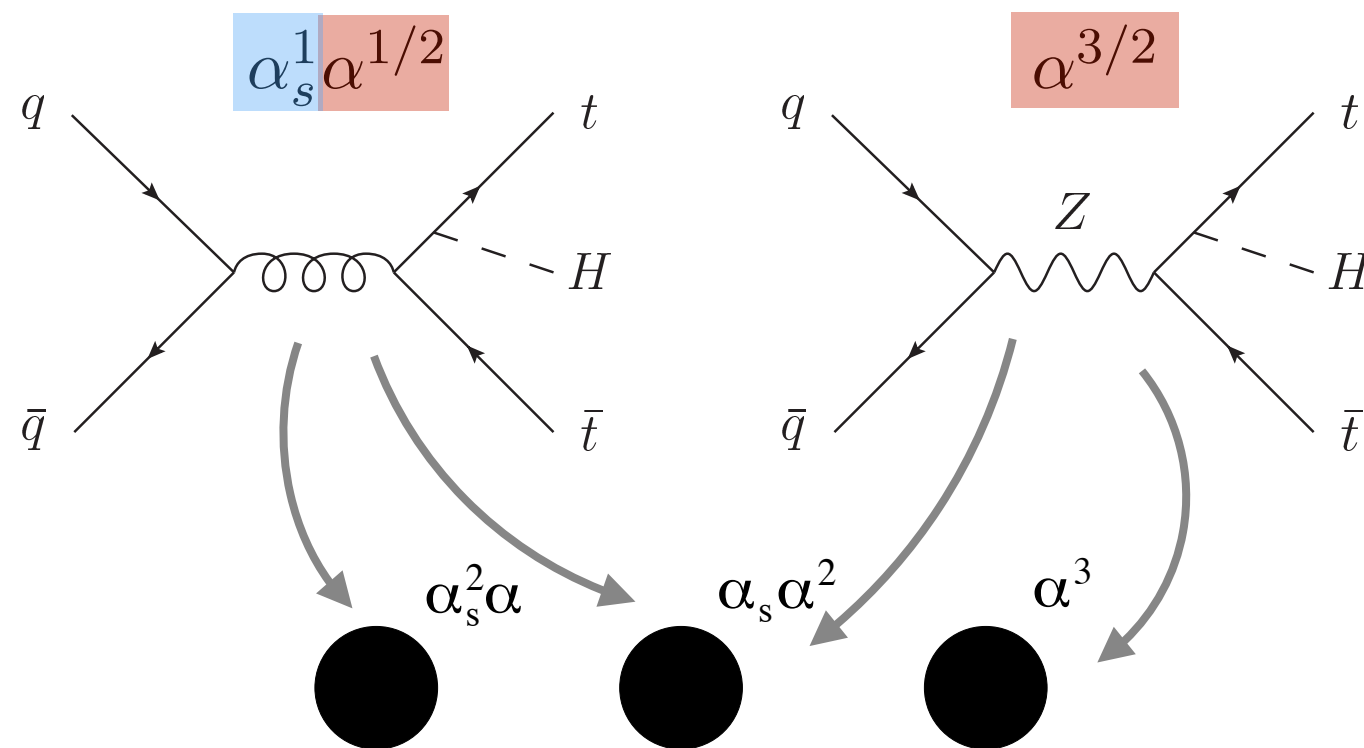
LO



# Structure of NLO EW-QCD corrections

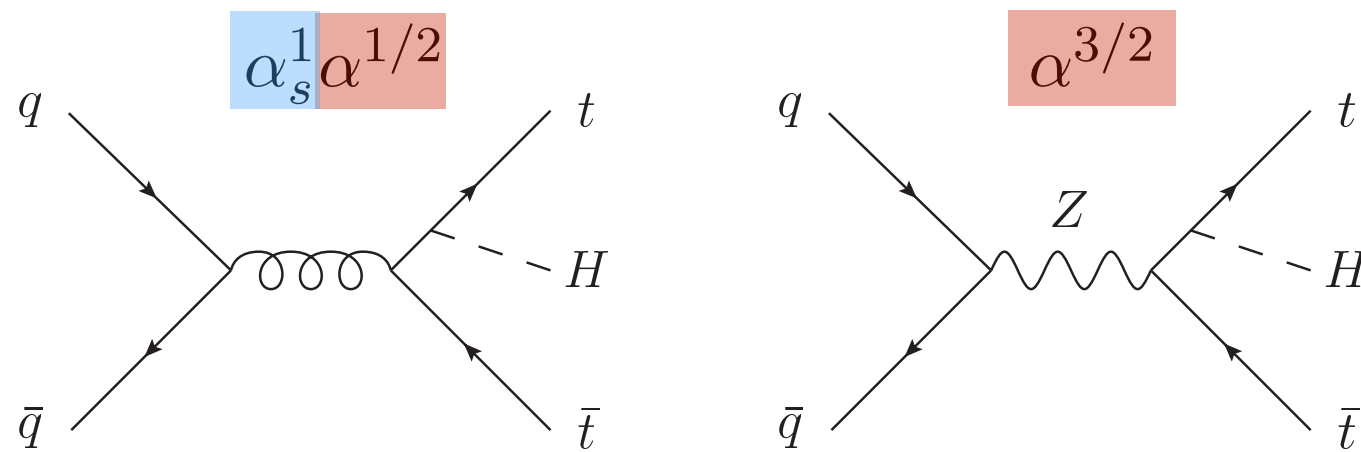
$t\bar{t}H$   
as example

LO

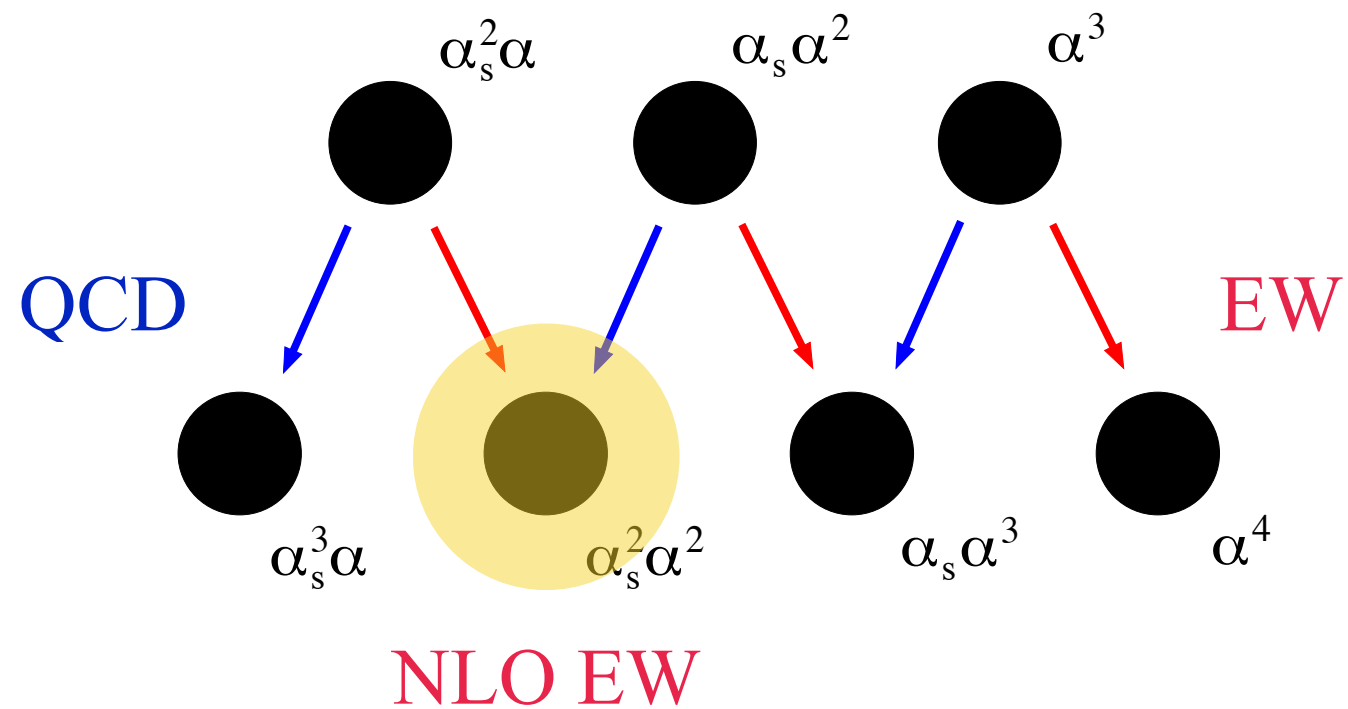


# Structure of NLO EW-QCD corrections

$t\bar{t}H$   
as example



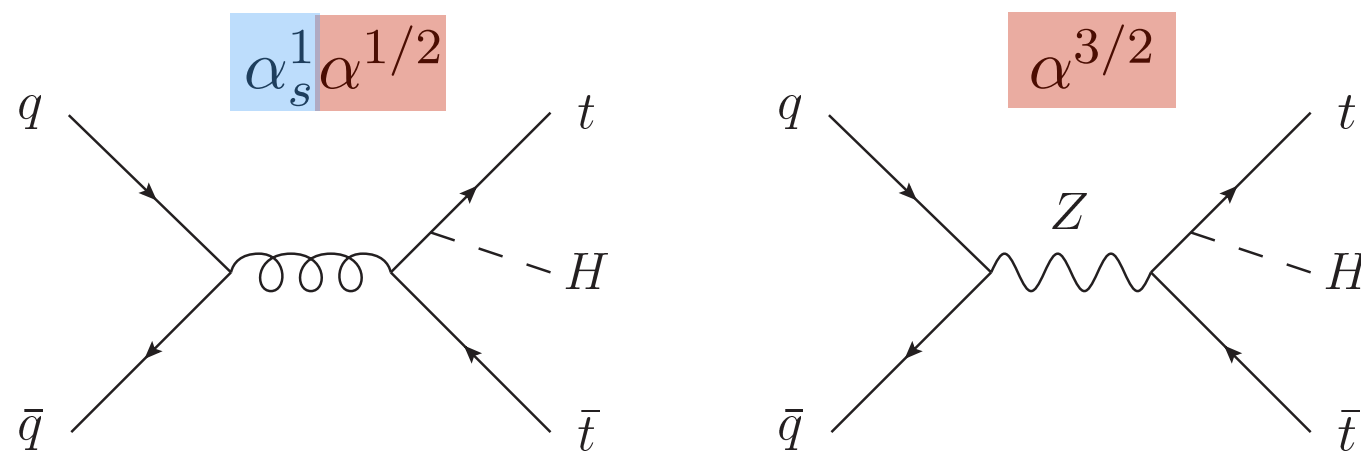
LO



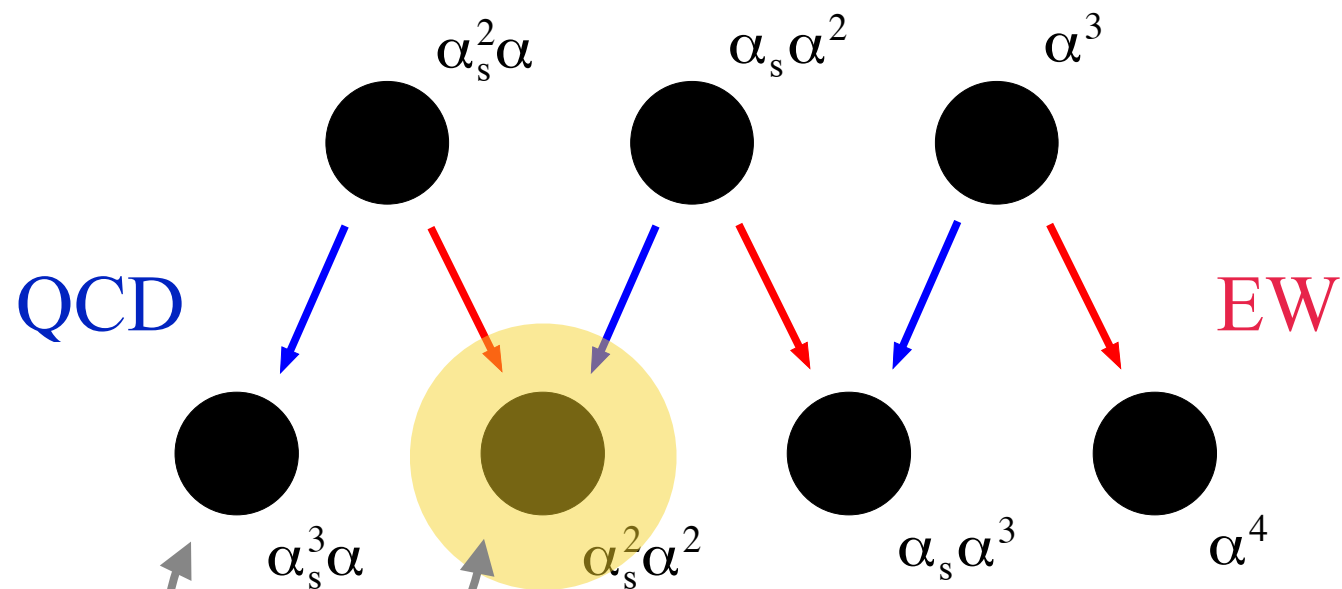
NLO

# Structure of NLO EW-QCD corrections

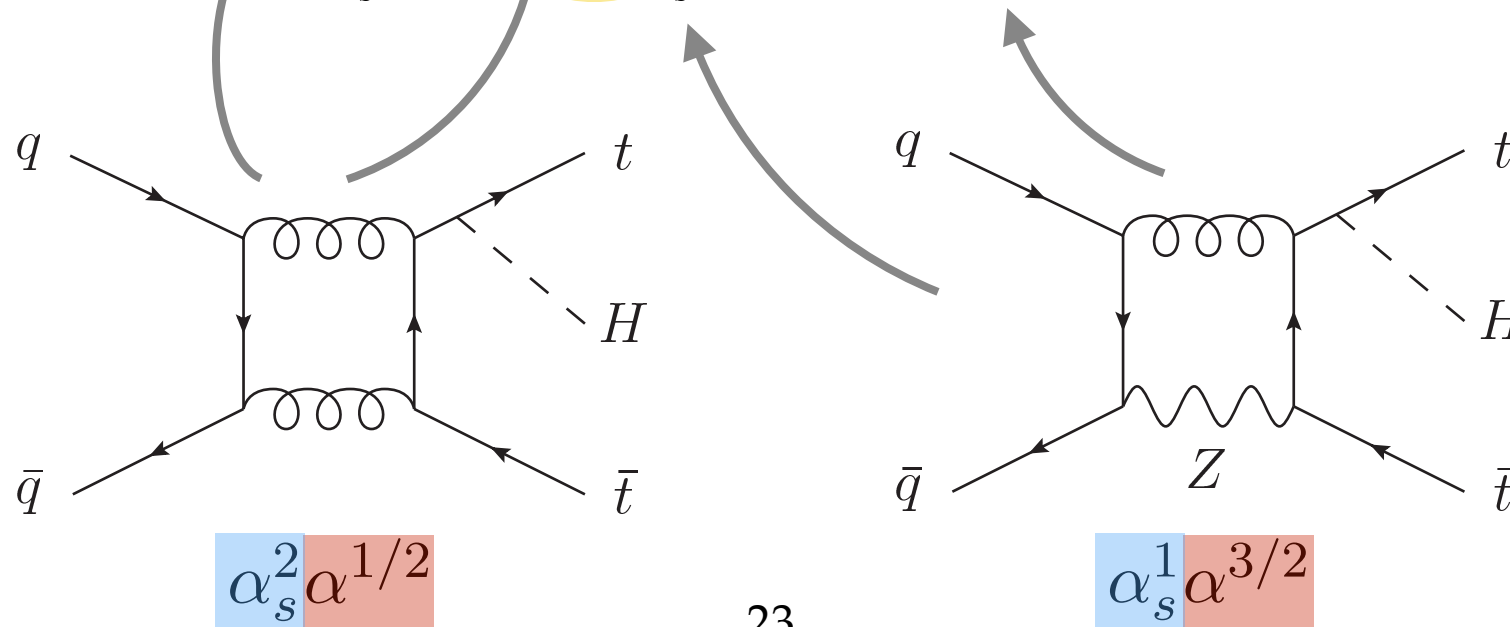
$t\bar{t}H$   
as example



LO

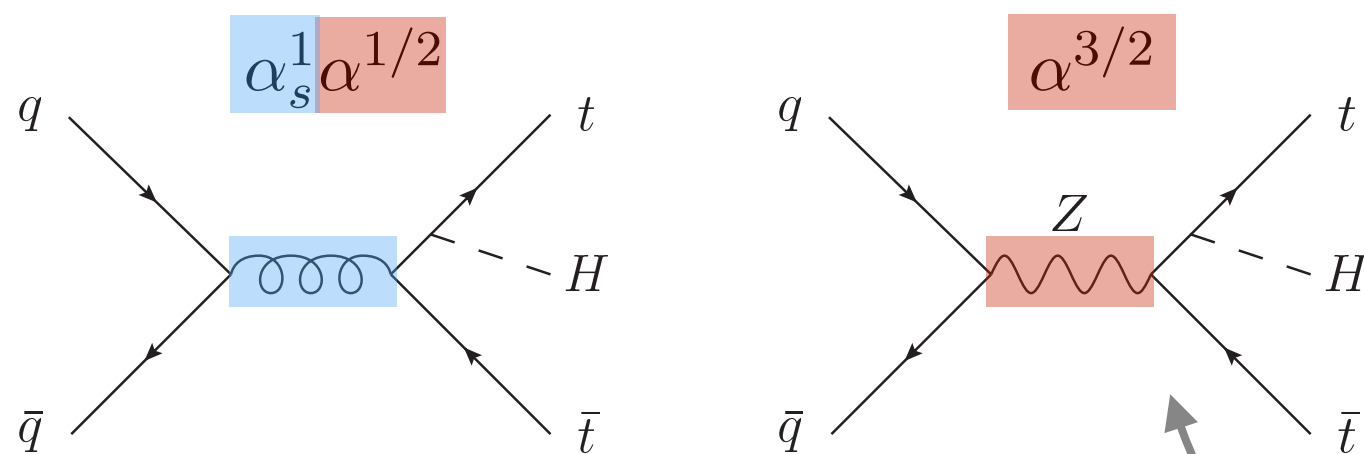


NLO

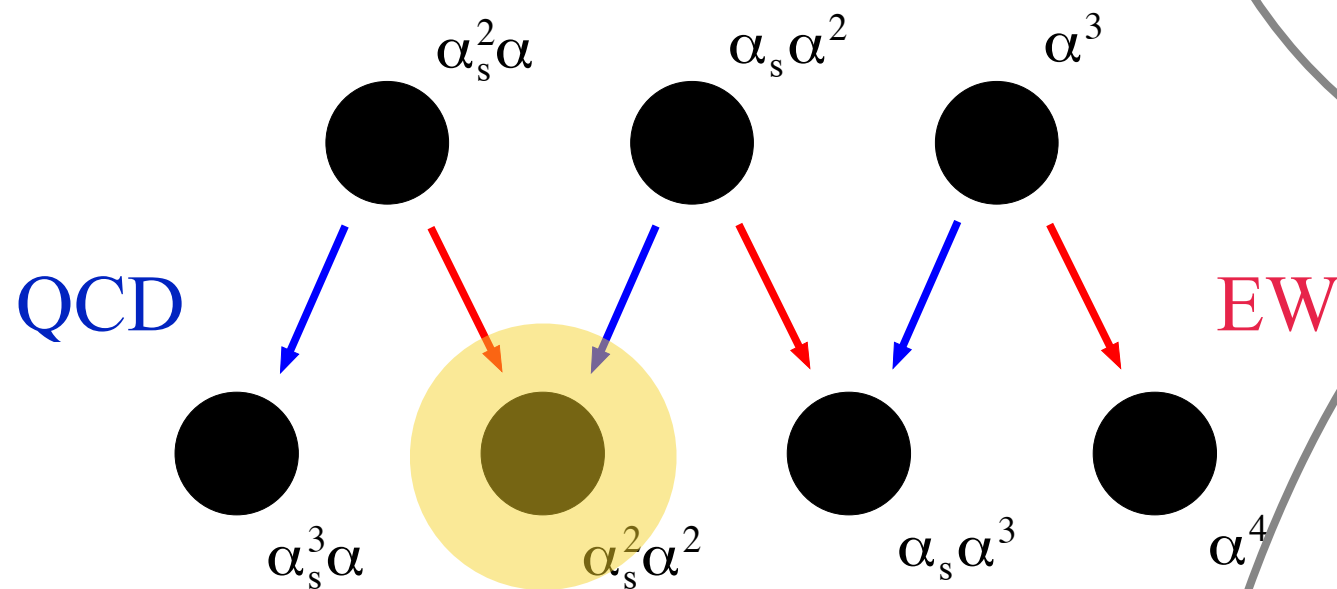


# Structure of NLO EW-QCD corrections

$t\bar{t}H$   
as example

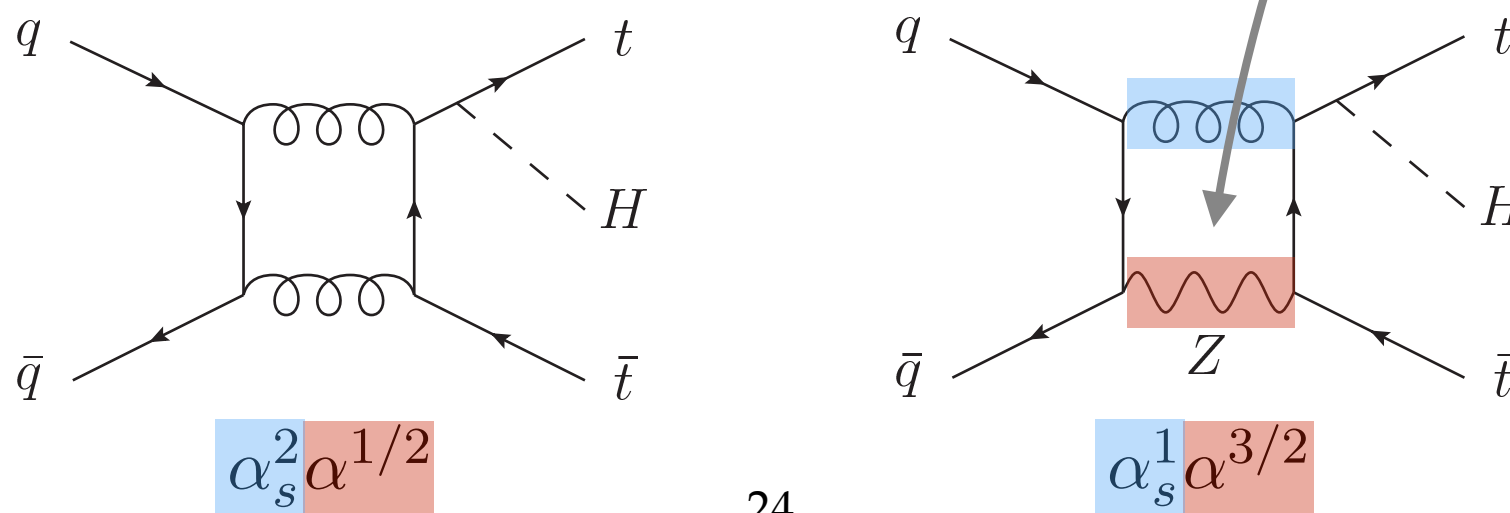


LO



If it is a photon,  
there are new  
IR singularities

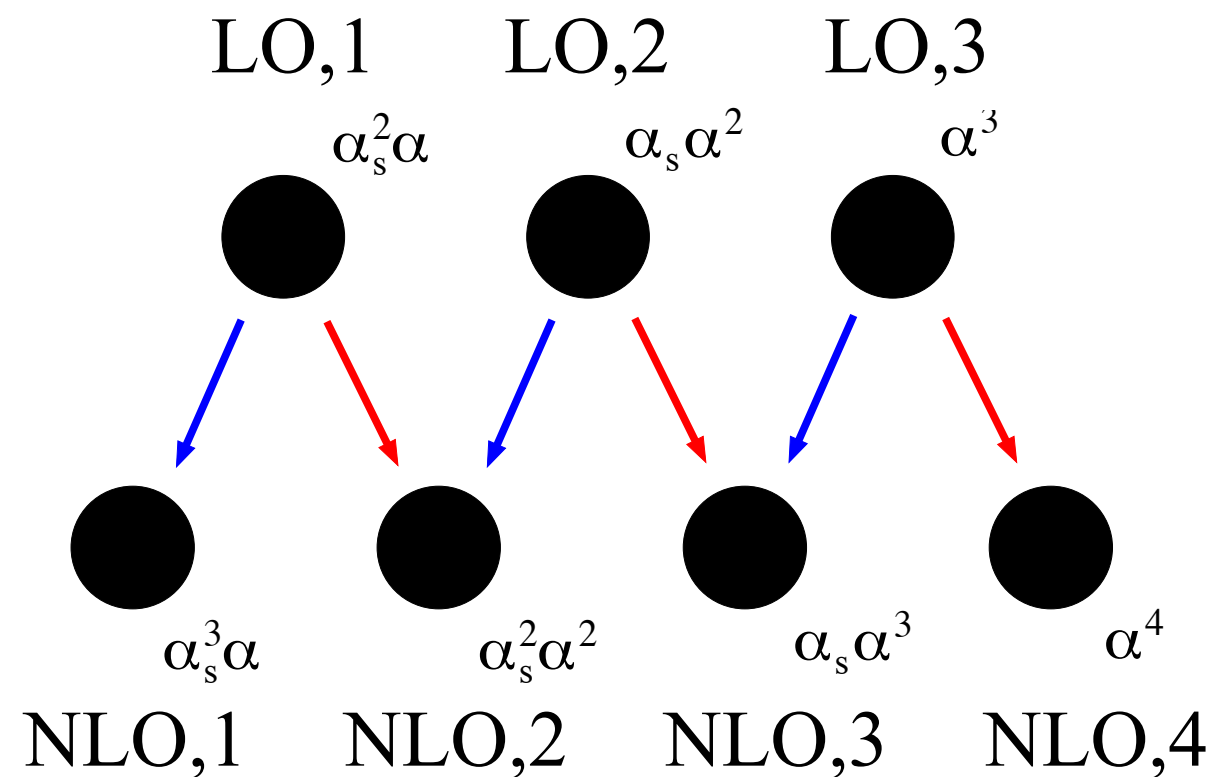
NLO



# Structure of NLO EW-QCD corrections

$t\bar{t}H$   
as example

All the LO,*i* and NLO,*i* can be calculated in a completely automated way. We denote the complete set of LO,*i* and NLO,*i* as “**Complete NLO**”.



NLO,1 = NLO QCD

NLO,2 = NLO EW

In general, NLO,3 and NLO,4 sizes are negligible, but there are exceptions.

# Results: NLO EW

just type:

```
set complex mass scheme true
import model loop_qcd_qed_sm_Gmu
generate process [QED]
output process_NLO_EW_corrections
```

And then wait for the results .....



# Results: NLO EW

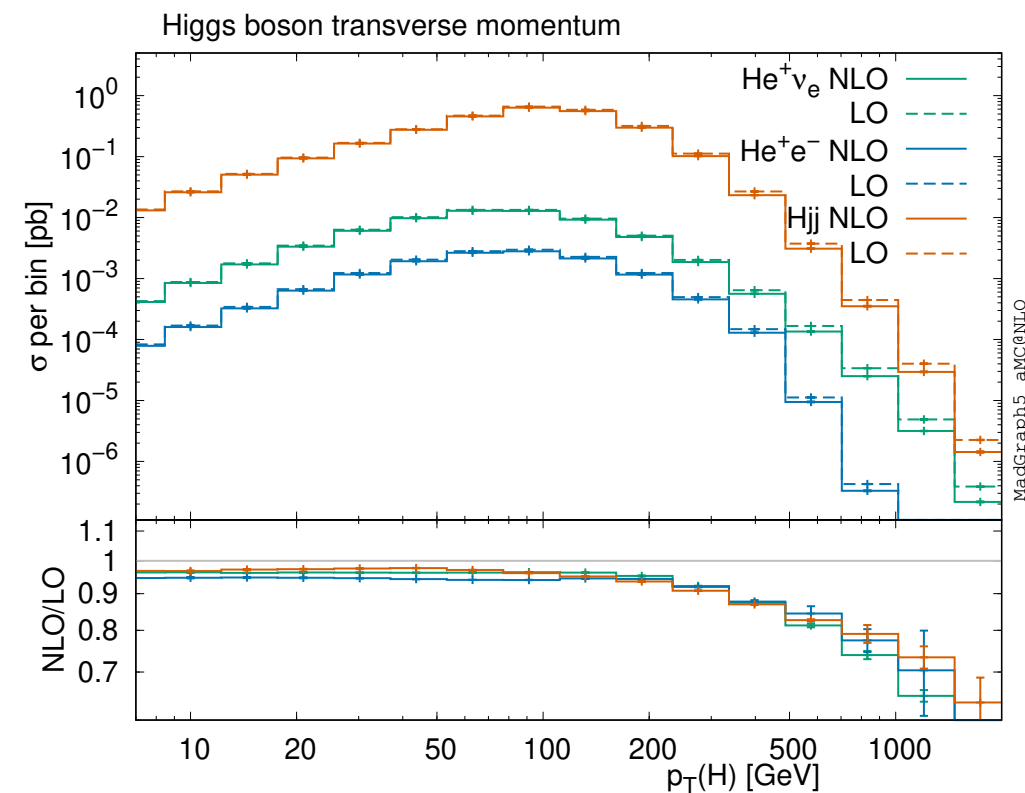
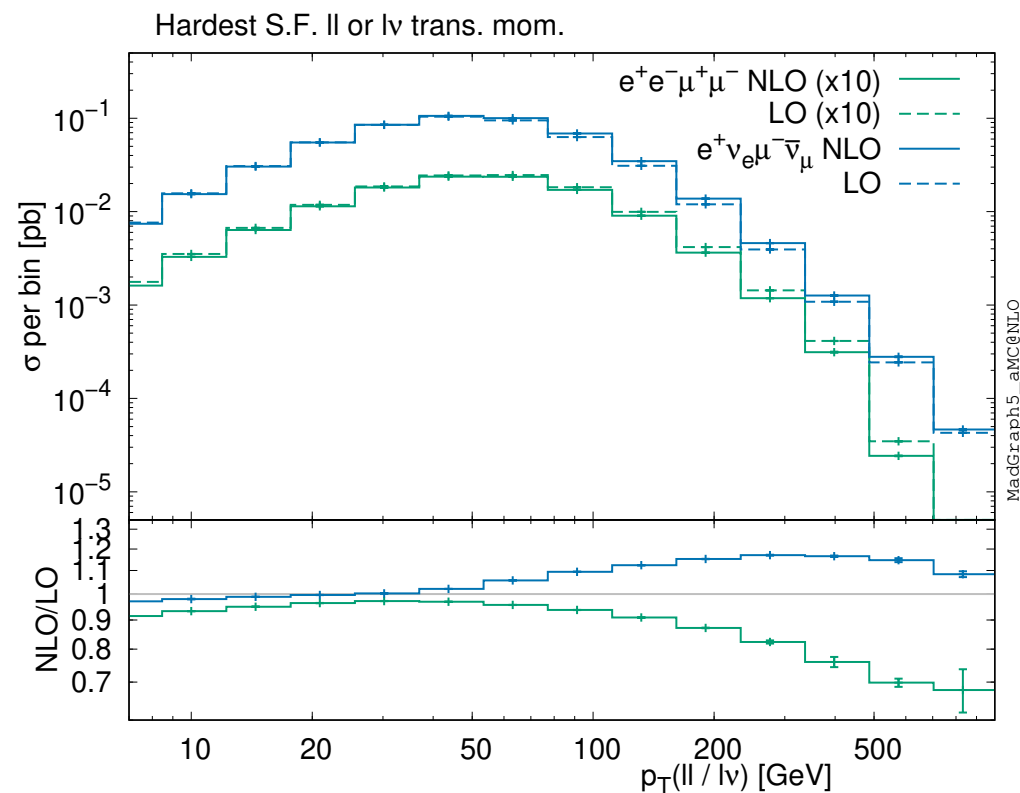
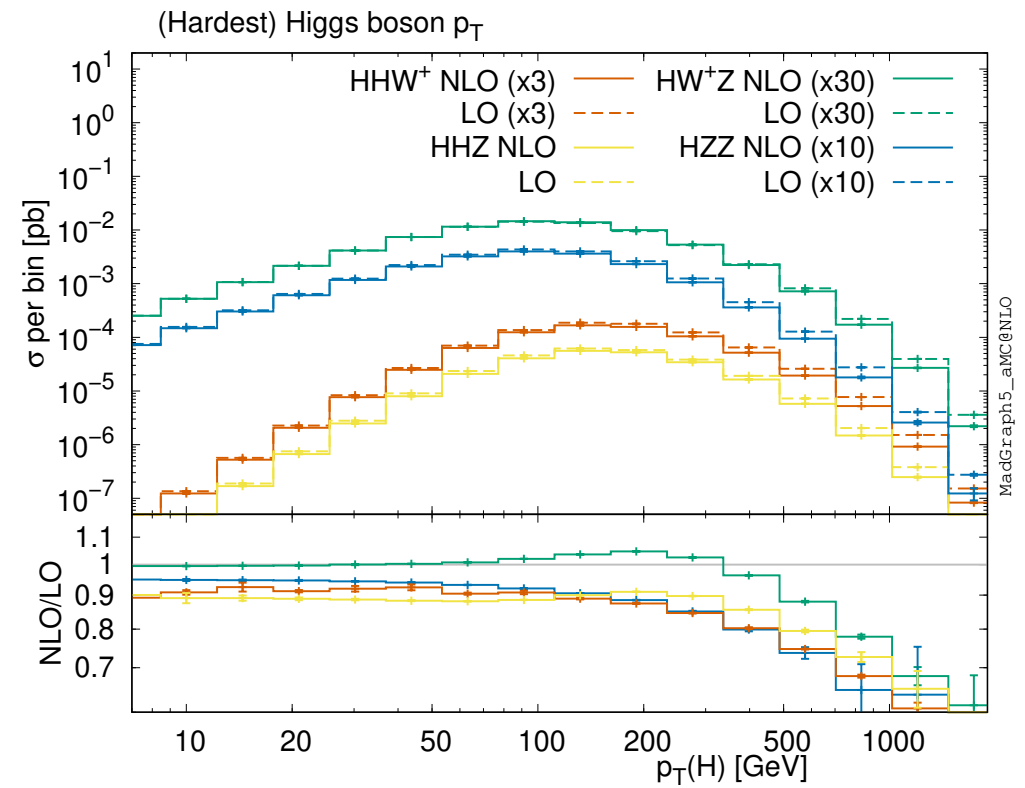
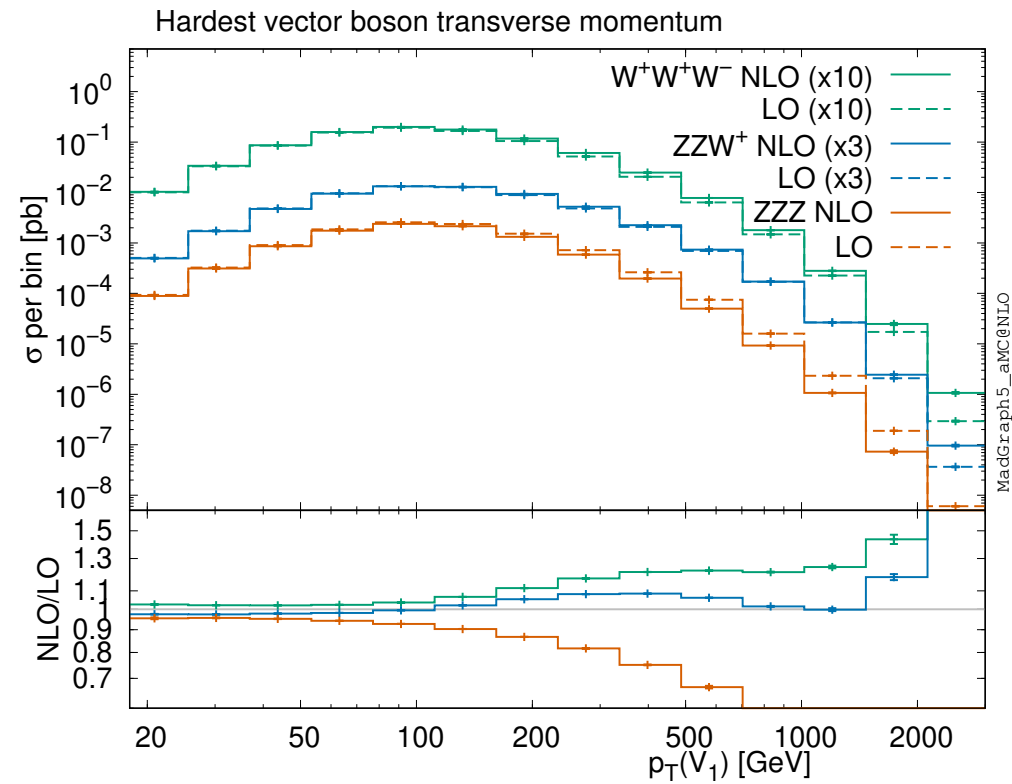
Process	Syntax	Cross section (in pb)		Correction (in %)
		LO	NLO	
$pp \rightarrow e^+ \nu_e$	p p > e+ ve QCD=0 QED=2 [QED]	$5.2498 \pm 0.0005 \cdot 10^3$	$5.2113 \pm 0.0006 \cdot 10^3$	$-0.73 \pm 0.01$
$pp \rightarrow e^+ \nu_e j$	p p > e+ ve j QCD=1 QED=2 [QED]	$9.1468 \pm 0.0012 \cdot 10^2$	$9.0449 \pm 0.0014 \cdot 10^2$	$-1.11 \pm 0.02$
$pp \rightarrow e^+ \nu_e jj$	p p > e+ ve j j QCD=2 QED=2 [QED]	$3.1562 \pm 0.0003 \cdot 10^2$	$3.0985 \pm 0.0005 \cdot 10^2$	$-1.83 \pm 0.02$
$pp \rightarrow e^+ e^-$	p p > e+ e- QCD=0 QED=2 [QED]	$7.5367 \pm 0.0008 \cdot 10^2$	$7.4997 \pm 0.0010 \cdot 10^2$	$-0.49 \pm 0.02$
$pp \rightarrow e^+ e^- j$	p p > e+ e- j QCD=1 QED=2 [QED]	$1.5059 \pm 0.0001 \cdot 10^2$	$1.4909 \pm 0.0002 \cdot 10^2$	$-1.00 \pm 0.02$
$pp \rightarrow e^+ e^- jj$	p p > e+ e- j j QCD=2 QED=2 [QED]	$5.1424 \pm 0.0004 \cdot 10^1$	$5.0410 \pm 0.0007 \cdot 10^1$	$-1.97 \pm 0.02$
$pp \rightarrow e^+ e^- \mu^+ \mu^-$	p p > e+ e- mu+ mu- QCD=0 QED=4 [QED]	$1.2750 \pm 0.0000 \cdot 10^{-2}$	$1.2083 \pm 0.0001 \cdot 10^{-2}$	$-5.23 \pm 0.01$
$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu$	p p > e+ ve mu- vm~ QCD=0 QED=4 [QED]	$5.1144 \pm 0.0007 \cdot 10^{-1}$	$5.3019 \pm 0.0009 \cdot 10^{-1}$	$+3.67 \pm 0.02$
$pp \rightarrow H e^+ \nu_e$	p p > h e+ ve QCD=0 QED=3 [QED]	$6.7643 \pm 0.0001 \cdot 10^{-2}$	$6.4914 \pm 0.0012 \cdot 10^{-2}$	$-4.03 \pm 0.02$
$pp \rightarrow H e^+ e^-$	p p > h e+ e- QCD=0 QED=3 [QED]	$1.4554 \pm 0.0001 \cdot 10^{-2}$	$1.3700 \pm 0.0002 \cdot 10^{-2}$	$-5.87 \pm 0.02$
$pp \rightarrow H jj$	p p > h j j QCD=0 QED=3 [QED]	$2.8268 \pm 0.0002 \cdot 10^0$	$2.7075 \pm 0.0003 \cdot 10^0$	$-4.22 \pm 0.01$
$pp \rightarrow W^+ W^- W^+$	p p > w+ w- w+ QCD=0 QED=3 [QED]	$8.2874 \pm 0.0004 \cdot 10^{-2}$	$8.8017 \pm 0.0012 \cdot 10^{-2}$	$+6.21 \pm 0.02$
$pp \rightarrow ZZW^+$	p p > z z w+ QCD=0 QED=3 [QED]	$1.9874 \pm 0.0001 \cdot 10^{-2}$	$2.0189 \pm 0.0003 \cdot 10^{-2}$	$+1.58 \pm 0.02$
$pp \rightarrow ZZZ$	p p > z z z QCD=0 QED=3 [QED]	$1.0761 \pm 0.0001 \cdot 10^{-2}$	$0.9741 \pm 0.0001 \cdot 10^{-2}$	$-9.47 \pm 0.02$
$pp \rightarrow HZZ$	p p > h z z QCD=0 QED=3 [QED]	$2.1005 \pm 0.0003 \cdot 10^{-3}$	$1.9155 \pm 0.0003 \cdot 10^{-3}$	$-8.81 \pm 0.02$
$pp \rightarrow HZW^+$	p p > h z w+ QCD=0 QED=3 [QED]	$2.4408 \pm 0.0000 \cdot 10^{-3}$	$2.4809 \pm 0.0005 \cdot 10^{-3}$	$+1.64 \pm 0.02$
$pp \rightarrow HHW^+$	p p > h h w+ QCD=0 QED=3 [QED]	$2.7827 \pm 0.0001 \cdot 10^{-4}$	$2.4259 \pm 0.0027 \cdot 10^{-4}$	$-12.82 \pm 0.10$
$pp \rightarrow HHZ$	p p > h h z QCD=0 QED=3 [QED]	$2.6914 \pm 0.0003 \cdot 10^{-4}$	$2.3926 \pm 0.0003 \cdot 10^{-4}$	$-11.10 \pm 0.02$
$pp \rightarrow t\bar{t}W^+$	p p > t t~ w+ QCD=2 QED=1 [QED]	$2.4119 \pm 0.0003 \cdot 10^{-1}$	$2.3025 \pm 0.0003 \cdot 10^{-1}$	$-4.54 \pm 0.02$
$pp \rightarrow t\bar{t}Z$	p p > t t~ z QCD=2 QED=1 [QED]	$5.0456 \pm 0.0006 \cdot 10^{-1}$	$5.0033 \pm 0.0007 \cdot 10^{-1}$	$-0.84 \pm 0.02$
$pp \rightarrow t\bar{t}H$	p p > t t~ h QCD=2 QED=1 [QED]	$3.4480 \pm 0.0004 \cdot 10^{-1}$	$3.5102 \pm 0.0005 \cdot 10^{-1}$	$+1.81 \pm 0.02$
$pp \rightarrow t\bar{t}j$	p p > t t~ j QCD=3 QED=0 [QED]	$3.0277 \pm 0.0003 \cdot 10^2$	$2.9683 \pm 0.0004 \cdot 10^2$	$-1.96 \pm 0.02$
$pp \rightarrow jjj$	p p > j j j QCD=3 QED=0 [QED]	$7.9639 \pm 0.0010 \cdot 10^6$	$7.9472 \pm 0.0011 \cdot 10^6$	$-0.21 \pm 0.02$
$pp \rightarrow tj$	p p > t j QCD=0 QED=2 [QED]	$1.0613 \pm 0.0001 \cdot 10^2$	$1.0539 \pm 0.0001 \cdot 10^2$	$-0.70 \pm 0.02$

NEW

couple of weeks on  $\mathcal{O}(200)$  CPUs

$$\delta_{\text{EW}} = \frac{\Sigma_{\text{NLO}_2}}{\Sigma_{\text{LO}_1}} = \frac{\text{NLO}}{\text{LO}} - 1.$$

# Results: NLO EW



# Results: Complete NLO

just type:

```
set complex mass scheme true
import model loop_qcd_qed_sm_Gmu
generate process QCD=99 QED=99 [QCD QED]
output process_NLO_EW_corrections
```

And then wait for the results .....

# Results: Complete NLO

NEW

	$pp \rightarrow t\bar{t}$	$pp \rightarrow t\bar{t}Z$	$pp \rightarrow t\bar{t}W^+$	$pp \rightarrow t\bar{t}H$	$pp \rightarrow t\bar{t}j$
LO <sub>1</sub>	$4.3803 \pm 0.0005 \cdot 10^2$ pb	$5.0463 \pm 0.0003 \cdot 10^{-1}$ pb	$2.4116 \pm 0.0001 \cdot 10^{-1}$ pb	$3.4483 \pm 0.0003 \cdot 10^{-1}$ pb	$3.0278 \pm 0.0003 \cdot 10^2$ pb
LO <sub>2</sub>	$+0.405 \pm 0.001$ %	$-0.691 \pm 0.001$ %	$+0.000 \pm 0.000$ %	$+0.406 \pm 0.001$ %	$+0.525 \pm 0.001$ %
LO <sub>3</sub>	$+0.630 \pm 0.001$ %	$+2.259 \pm 0.001$ %	$+0.962 \pm 0.000$ %	$+0.702 \pm 0.001$ %	$+1.208 \pm 0.001$ %
LO <sub>4</sub>					$+0.006 \pm 0.000$ %
NLO <sub>1</sub>	$+46.164 \pm 0.022$ %	$+44.809 \pm 0.028$ %	$+49.504 \pm 0.015$ %	$+28.847 \pm 0.020$ %	$+26.571 \pm 0.063$ %
NLO <sub>2</sub>	$-1.075 \pm 0.003$ %	$-0.846 \pm 0.004$ %	$-4.541 \pm 0.003$ %	$+1.794 \pm 0.005$ %	$-1.971 \pm 0.022$ %
NLO <sub>3</sub>	$+0.552 \pm 0.002$ %	$+0.845 \pm 0.003$ %	$+12.242 \pm 0.014$ %	$+0.483 \pm 0.008$ %	$+0.292 \pm 0.007$ %
NLO <sub>4</sub>	$+0.005 \pm 0.000$ %	$-0.082 \pm 0.000$ %	$+0.017 \pm 0.003$ %	$+0.044 \pm 0.000$ %	$+0.009 \pm 0.000$ %
NLO <sub>5</sub>					$+0.005 \pm 0.000$ %

$$\frac{\Sigma_{\text{LO}_i}}{\Sigma_{\text{LO}_1}}, \quad i = 2, 3, 4,$$

$$\frac{\Sigma_{\text{NLO}_i}}{\Sigma_{\text{LO}_1}}, \quad i = 1, \dots, 5;$$

NLO<sub>3</sub> in ttW is ~12%:

A thorough phenomenological study is necessary!

*Frederix, Frixione, Hirschi, DP, Shao, Zaro '18*

$t\bar{t}W^\pm$ 

R. Frederix, D.P., M. Zaro  
JHEP 1802 (2018) 031 (arXiv:1711.02116)

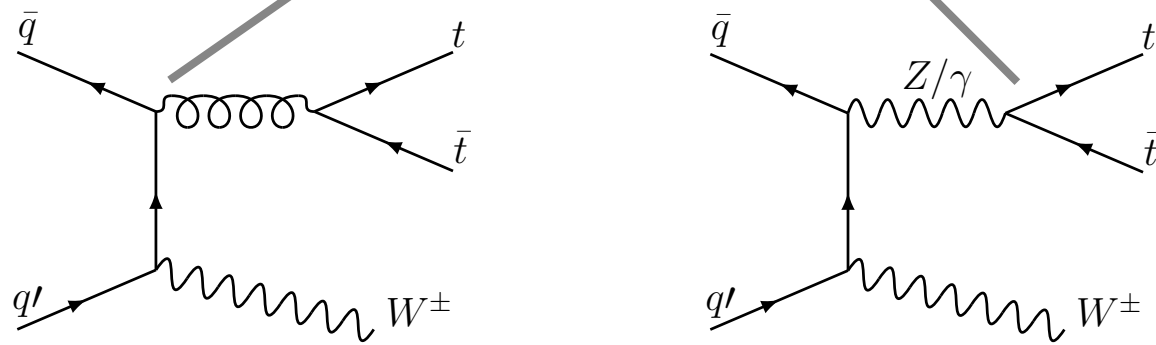
# Complete-NLO

*Frederix, DP, Zaro '17*

$$\Sigma_{\text{LO}}^{t\bar{t}W^\pm}(\alpha_s, \alpha) = \alpha_s^2 \alpha \Sigma_{3,0}^{t\bar{t}W^\pm} + \alpha_s \alpha \Sigma_{3,1}^{t\bar{t}W^\pm} + \alpha^2 \Sigma_{3,2}^{t\bar{t}W^\pm}$$

$$\equiv \Sigma_{\text{LO}_1} + \cancel{\Sigma_{\text{LO}_2}} + \Sigma_{\text{LO}_3},$$

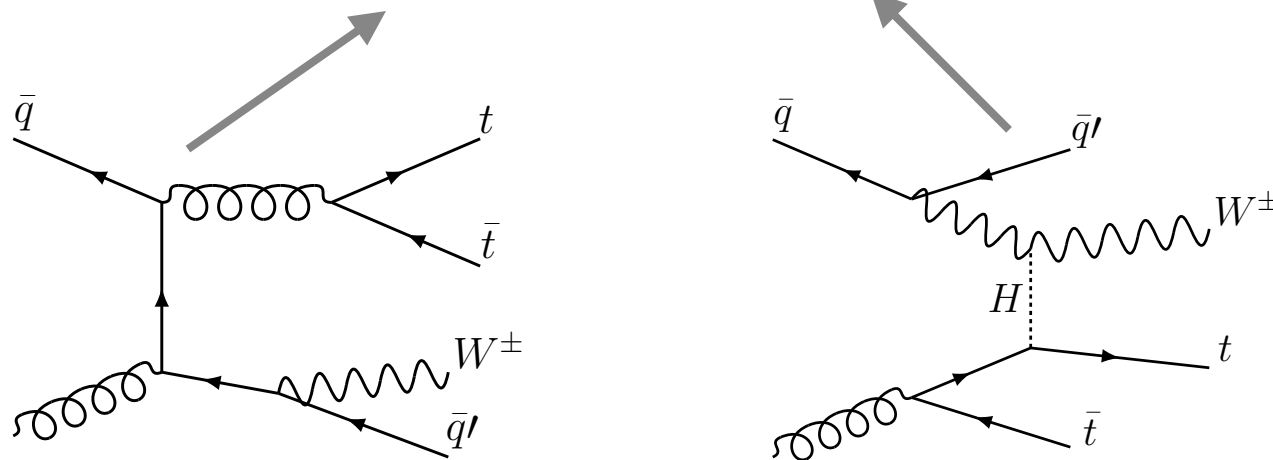
Only initial states without gluons are present.



$$\Sigma_{\text{LO}_1} \longrightarrow \text{LO}_{\text{QCD}}$$

$$\Sigma_{\text{NLO}}^{t\bar{t}W^\pm}(\alpha_s, \alpha) = \alpha_s^3 \alpha \Sigma_{4,0}^{t\bar{t}W^\pm} + \alpha_s^2 \alpha^2 \Sigma_{4,1}^{t\bar{t}W^\pm} + \alpha_s \alpha^3 \Sigma_{4,2}^{t\bar{t}W^\pm} + \alpha^4 \Sigma_{4,3}^{t\bar{t}W^\pm}$$

$$\equiv \Sigma_{\text{NLO}_1} + \Sigma_{\text{NLO}_2} + \Sigma_{\text{NLO}_3} + \Sigma_{\text{NLO}_4},$$



$$\Sigma_{\text{NLO}_1} \longrightarrow \text{NLO}_{\text{QCD}}$$

$$\Sigma_{\text{NLO}_2} \longrightarrow \text{NLO}_{\text{EW}}$$

**MadGraph5\_aMC@NLO**

# Cross sections: order by order

$$\delta_{(N)\text{LO}_i}(\mu) = \frac{\Sigma_{(N)\text{LO}_i}(\mu)}{\Sigma_{\text{LO}_{\text{QCD}}}(\mu)}$$

Numbers in parentheses refer to the case of a jet veto  $p_T(j) > 100 \text{ GeV}$  and  $|y(j)| < 2.5$  applied

13 TeV

Naive estimate

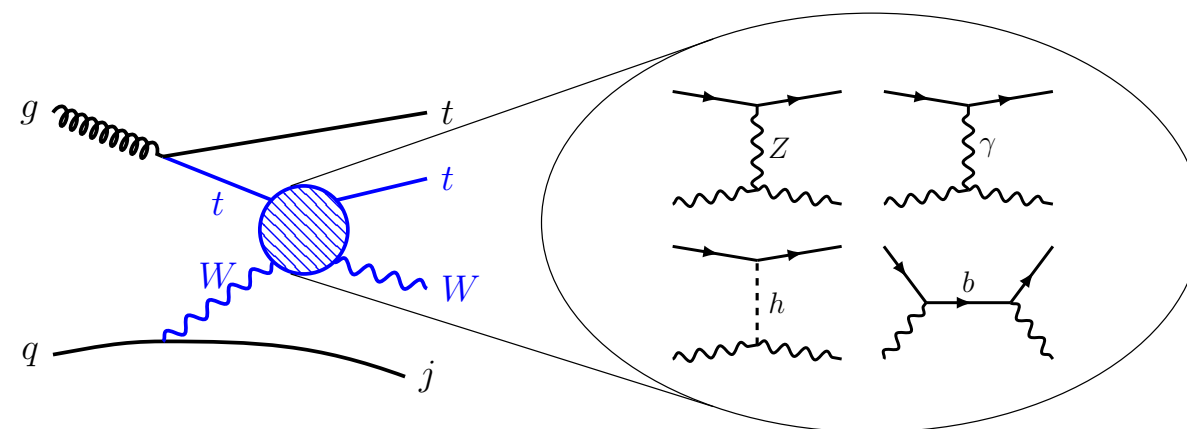
100 TeV

$\delta[\%]$	$\mu = H_T/4$	$\mu = H_T/2$	$\mu = H_T$	
LO <sub>2</sub>	-	-	-	10
LO <sub>3</sub>	0.8	0.9	1.1	1
NLO <sub>1</sub>	34.8 (7.0)	50.0 (25.7)	63.4 (42.0)	10
NLO <sub>2</sub>	-4.4 (-4.8)	-4.2 (-4.6)	-4.0 (-4.4)	1
NLO <sub>3</sub>	11.9 (8.9)	12.2 (9.1)	12.5 (9.3)	0.1
NLO <sub>4</sub>	0.02 (-0.02)	0.04 (-0.02)	0.05 (-0.01)	0.01

$\delta[\%]$	$\mu = H_T/4$	$\mu = H_T/2$	$\mu = H_T$
LO <sub>2</sub>	-	-	-
LO <sub>3</sub>	0.9	1.1	1.3
NLO <sub>1</sub>	159.5 (69.8)	149.5 (71.1)	142.7 (73.4)
NLO <sub>2</sub>	-5.8 (-6.4)	-5.6 (-6.2)	-5.4 (-6.1)
NLO <sub>3</sub>	67.5 (55.6)	68.8 (56.6)	70.0 (57.6)
NLO <sub>4</sub>	0.2 (0.1)	0.2 (0.2)	0.3 (0.2)

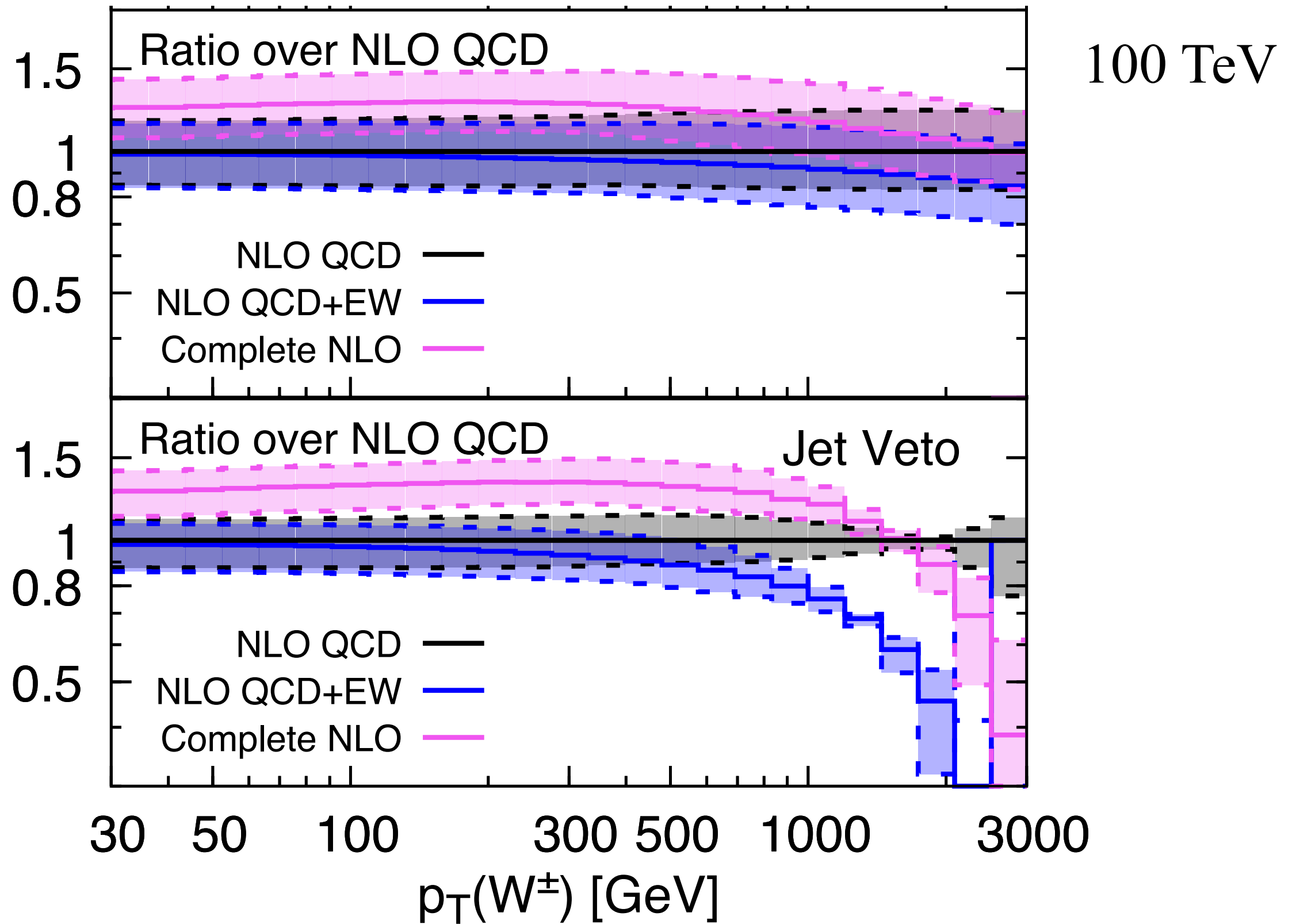
NLO<sub>3</sub> is large and it is not suppressed by the jet veto (numbers in parentheses) as much as NLO QCD corrections.

NLO QCD corrections depend on the scale, while NLO EW and NLO<sub>3</sub> do not.



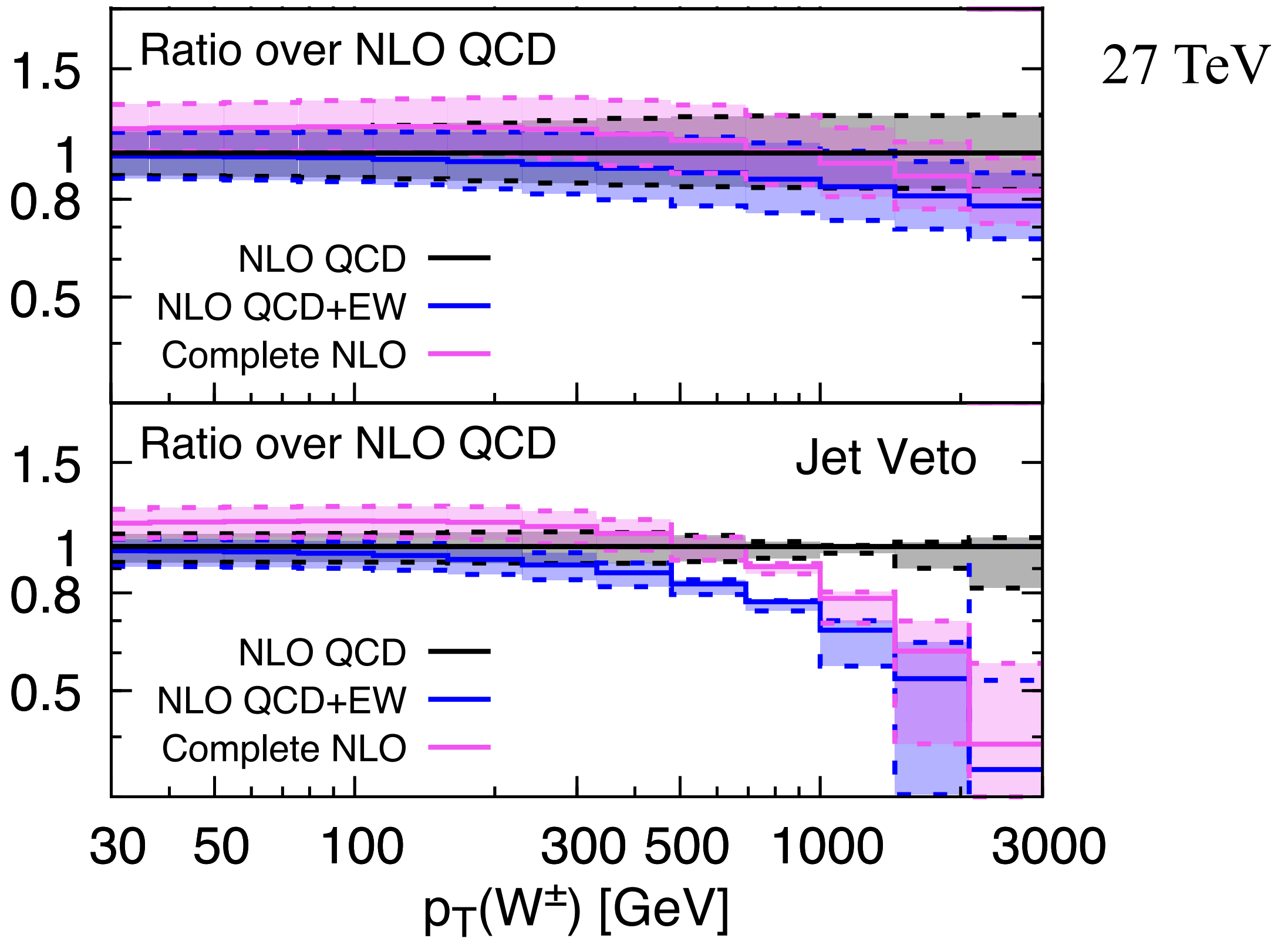
Frederix, DP, Zaro '17

# Distributions

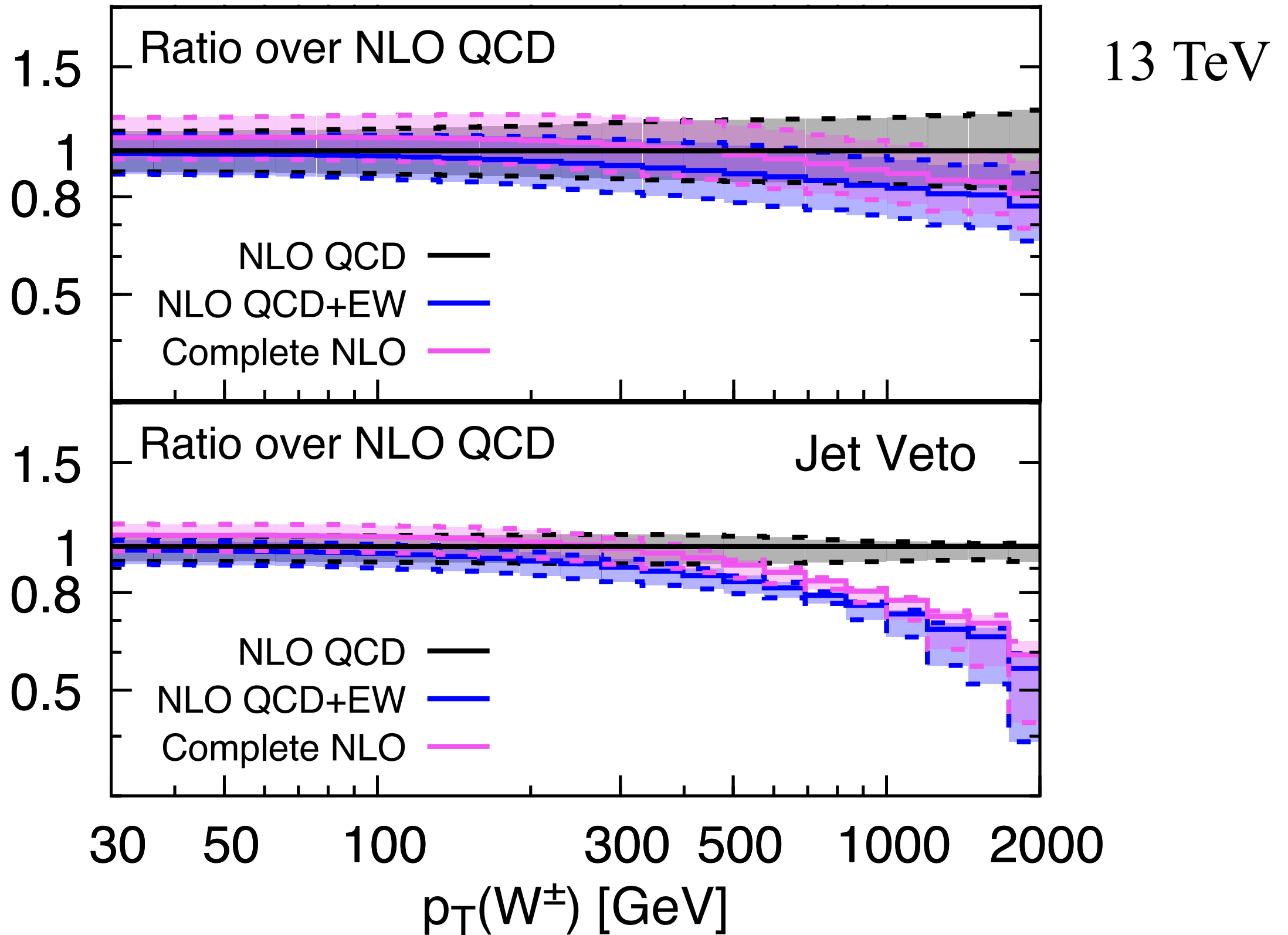




# Distributions



# Distributions



# $t\bar{t}H, t\bar{t}W, t\bar{t}Z$ : Complete-NLO with resummation at NNLL

**Complete-NLO** (QCD and EW) calculated with a public version of MG5\_aMC@NLO. *Frederix, Frixione, Hirschi, DP, Shao, Zaro '18*

**Resummation of soft gluon at NNLL accuracy via SCET:**

*Broggio, Ferroglia, Ossola, Pecjak '16*  $t\bar{t}W$

*Broggio, Ferroglia, Pecjak, Yang '16*  $t\bar{t}H$

*Broggio, Ferroglia, Ossola, Pecjak, Sameshima '17*  $t\bar{t}Z$

**Resummation of soft gluon at NNLL accuracy via resum. in Mellin space:**

*Kulesza, Motyka, Stebel, Theeuwes '17*  $t\bar{t}H$

*Kulesza, Motyka, Schwartländer, Stebel, Theeuwes '17*  $t\bar{t}W$

*Kulesza, Motyka, Schwartländer, Stebel, Theeuwes '18*  $t\bar{t}V$

# $t\bar{t}H, t\bar{t}W, t\bar{t}Z$ : Complete-NLO with resummation at NNLL

**Complete-NLO** (QCD and EW) calculated with a public version of MG5\_aMC@NLO. *Frederix, Frixione, Hirschi, DP, Shao, Zaro '18*

**Resummation of soft gluon at NNLL accuracy via SCET:**

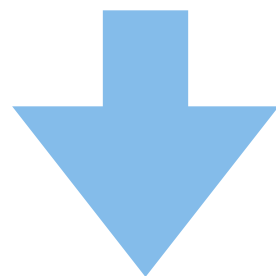
*Broggio, Ferroglia, Ossola, Pecjak '16*  $t\bar{t}W$

*Broggio, Ferroglia, Pecjak, Yang '16*  $t\bar{t}H$

*Broggio, Ferroglia, Ossola, Pecjak, Sameshima '17*  $t\bar{t}Z$

---

**Complete NLO (QCD and EW) + Resummation NNLL**

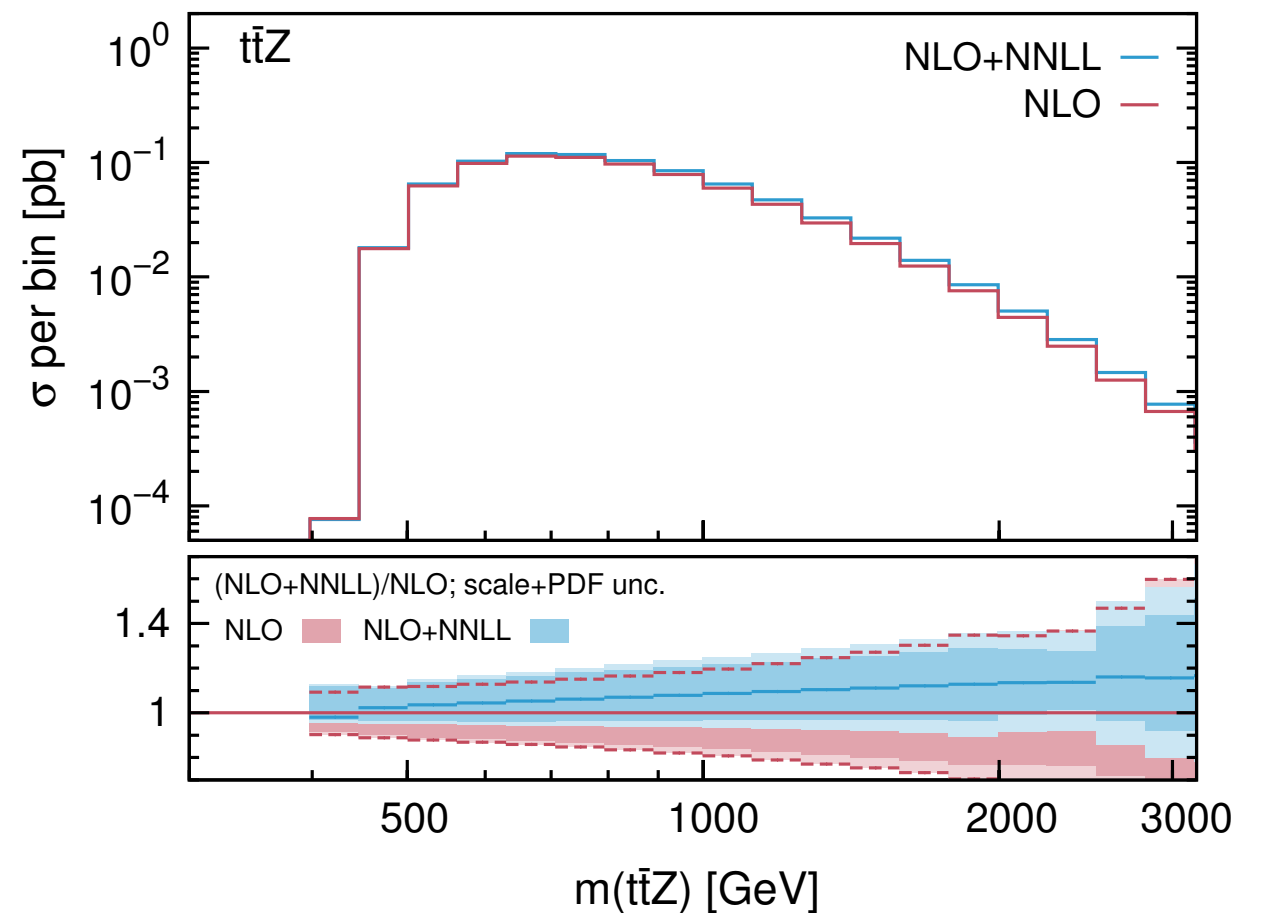
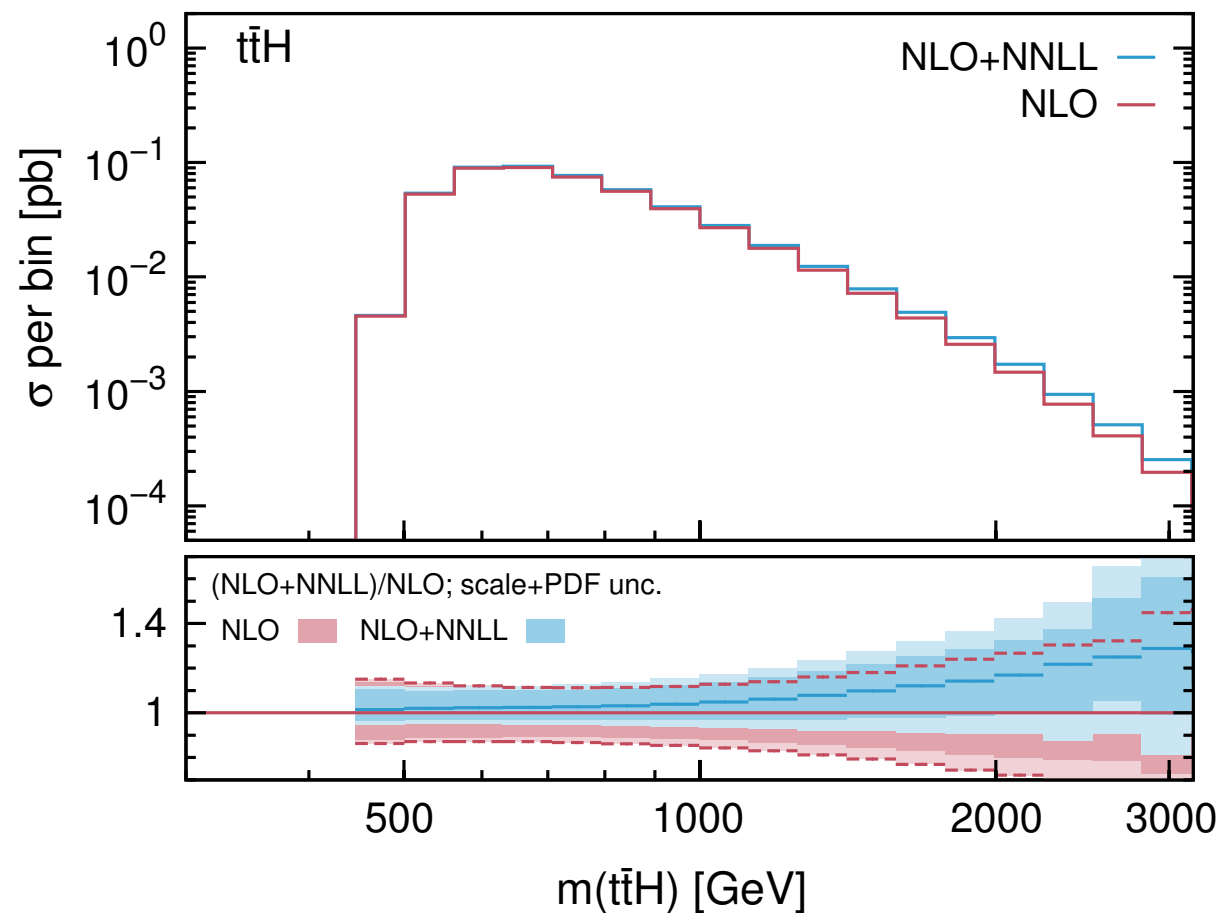


**The currently most accurate predictions for  $t\bar{t}H, t\bar{t}W, t\bar{t}Z$**

*Broggio, Ferroglia, Frederix, DP, Pecjak, Tsinikos arXiv:1907.04343*

# $t\bar{t}H, t\bar{t}Z$ : Complete-NLO with resummation at NNLL

We consider two different functional forms ( $H_T/2$  and  $m(t\bar{t}V)/2$ ) for the hard scale and we identify the envelope of the two associated scale uncertainties, together with PDF uncertainties, as the total theory uncertainty band.

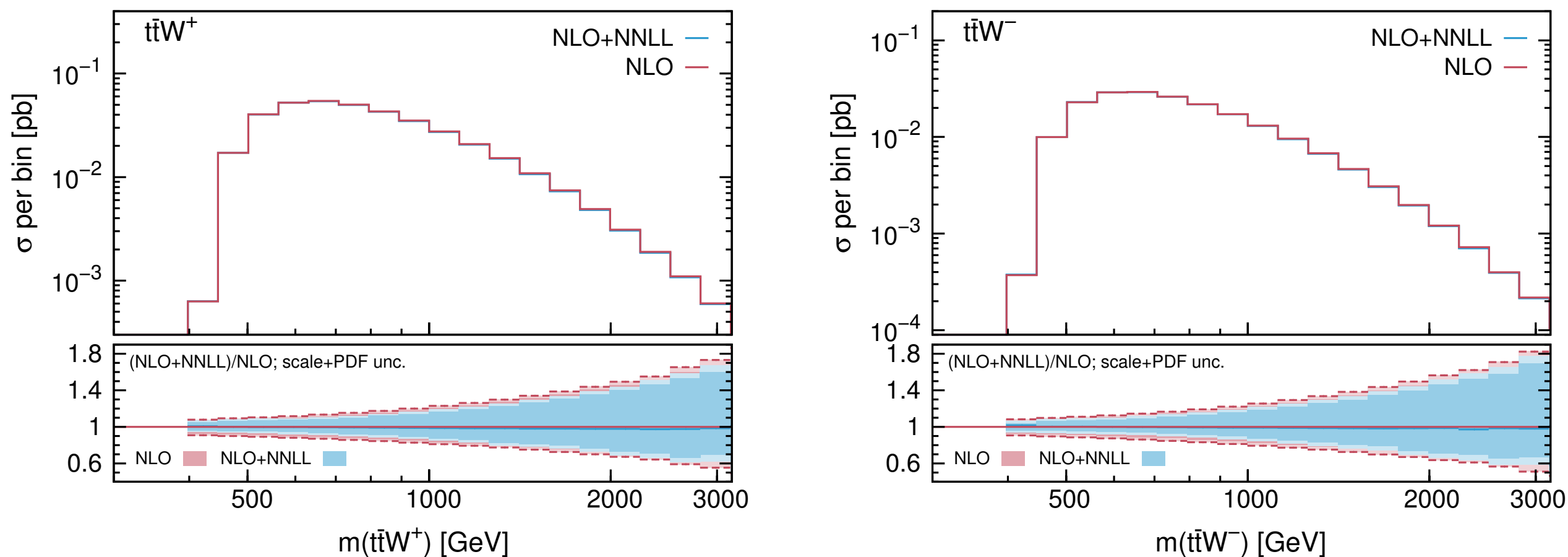


**As expected, in this approach, theory uncertainties are reduced when resummation is also included.** EW effects and especially the Complete NLO are smaller with  $t\bar{t}H$  and  $t\bar{t}Z$ .

*Numbers in the back-up slides*

# $t\bar{t}W$ : Complete-NLO with resummation at NNLL

We consider two different functional forms ( $H_T/2$  and  $m(t\bar{t}V)/2$ ) for the hard scale and we identify the envelope of the two associated scale uncertainties, together with PDF uncertainties, as the total theory uncertainty band.



**Resummation leads to a only small reduction of scale uncertainties,**  
The bulk of QCD corrections originates from hard emissions.

*Numbers in the back-up slides*

$t\bar{t}t\bar{t}$

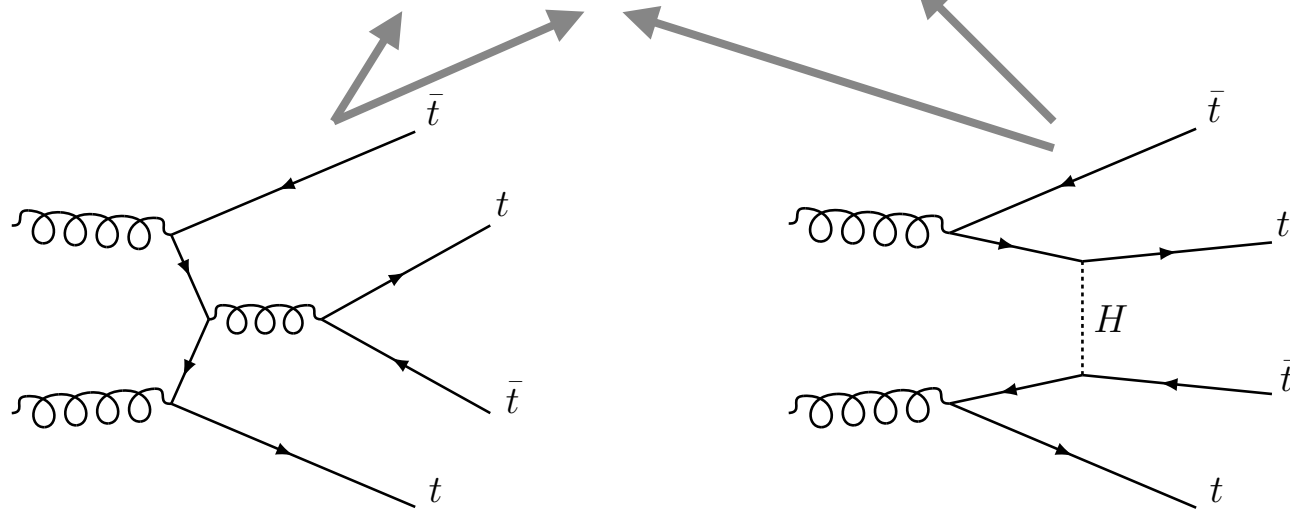
R. Frederix, D.P., M. Zaro  
JHEP 1802 (2018) 031 (arXiv:1711.02116)

# Complete-NLO

$$\Sigma_{\text{LO}}^{t\bar{t}t\bar{t}}(\alpha_s, \alpha) = \alpha_s^4 \Sigma_{4,0}^{t\bar{t}t\bar{t}} + \alpha_s^3 \alpha \Sigma_{4,1}^{t\bar{t}t\bar{t}} + \alpha_s^2 \alpha^2 \Sigma_{4,2}^{t\bar{t}t\bar{t}} + \alpha_s \alpha^3 \Sigma_{4,3}^{t\bar{t}t\bar{t}} + \alpha^4 \Sigma_{4,4}^{t\bar{t}t\bar{t}}$$

$$\equiv \Sigma_{\text{LO}_1} + \Sigma_{\text{LO}_2} + \Sigma_{\text{LO}_3} + \Sigma_{\text{LO}_4} + \Sigma_{\text{LO}_5}.$$

*Frederix, DP, Zaro '17*

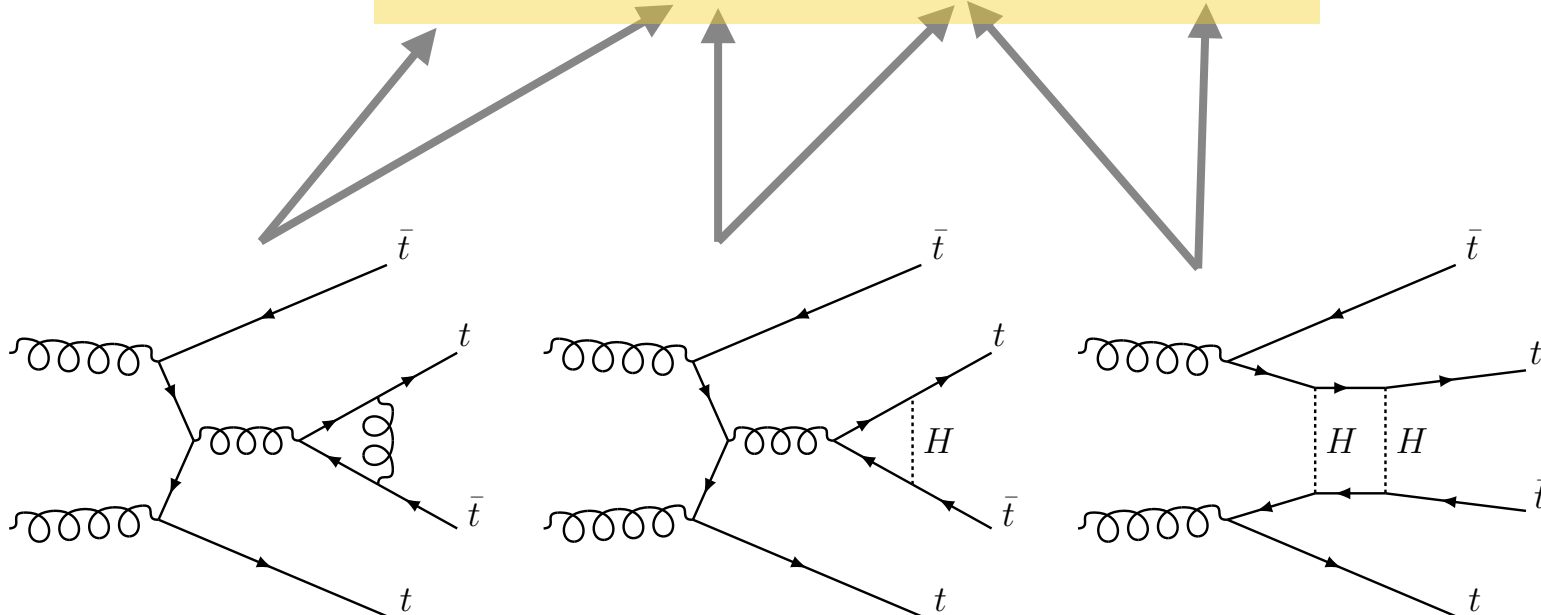


The gg initial state amounts to ~90% of LO cross section at 13 TeV and almost all the cross section at 100 TeV.

There is no gg contribution at LO4 and LO5.

$$\Sigma_{\text{NLO}}^{t\bar{t}t\bar{t}}(\alpha_s, \alpha) = \alpha_s^5 \Sigma_{5,0}^{t\bar{t}t\bar{t}} + \alpha_s^4 \alpha^1 \Sigma_{5,1}^{t\bar{t}t\bar{t}} + \alpha_s^3 \alpha^2 \Sigma_{5,2}^{t\bar{t}t\bar{t}} + \alpha_s^2 \alpha^3 \Sigma_{5,3}^{t\bar{t}t\bar{t}} + \alpha_s^1 \alpha^4 \Sigma_{5,4}^{t\bar{t}t\bar{t}} + \alpha^5 \Sigma_{5,5}^{t\bar{t}t\bar{t}}$$

$$\equiv \Sigma_{\text{NLO}_1} + \Sigma_{\text{NLO}_2} + \Sigma_{\text{NLO}_3} + \Sigma_{\text{NLO}_4} + \Sigma_{\text{NLO}_5} + \Sigma_{\text{NLO}_6}.$$



There is no gg contribution at NLO5 and NLO6.

**MadGraph5\_aMC@NLO**



# Cross sections

13 TeV

Naive estimate

100 TeV

$\delta[\%]$	$\mu = H_T/8$	$\mu = H_T/4$	$\mu = H_T/2$		$\delta[\%]$	$\mu = H_T/8$	$\mu = H_T/4$	$\mu = H_T/2$
LO <sub>2</sub>	-26.0	-28.3	-30.5	10	LO <sub>2</sub>	-18.7	-20.7	-22.8
LO <sub>3</sub>	32.6	39.0	45.9	1	LO <sub>3</sub>	26.3	31.8	37.8
LO <sub>4</sub>	0.2	0.3	0.4	0.1	LO <sub>4</sub>	0.05	0.07	0.09
LO <sub>5</sub>	0.02	0.03	0.05	0.01	LO <sub>5</sub>	0.03	0.05	0.08
NLO <sub>1</sub>	14.0	62.7	103.5	10	NLO <sub>1</sub>	33.9	68.2	98.0
NLO <sub>2</sub>	8.6	-3.3	-15.1	1	NLO <sub>2</sub>	-0.3	-5.7	-11.6
NLO <sub>3</sub>	-10.3	1.8	16.1	0.1	NLO <sub>3</sub>	-3.9	1.7	8.9
NLO <sub>4</sub>	2.3	2.8	3.6	0.01	NLO <sub>4</sub>	0.7	0.9	1.2
NLO <sub>5</sub>	0.12	0.16	0.19	0.001	NLO <sub>5</sub>	0.12	0.14	0.16
NLO <sub>6</sub>	< 0.01	< 0.01	< 0.01	0.0001	NLO <sub>6</sub>	< 0.01	< 0.01	< 0.01
NLO <sub>2</sub> + NLO <sub>3</sub>	-1.7	-1.6	0.9		NLO <sub>2</sub> + NLO <sub>3</sub>	-4.2	-4.0	2.7

LO<sub>2</sub> and LO<sub>3</sub> are large and have also large cancellations.

*Frederix, DP, Zaro '17*

NLO<sub>2</sub> and NLO<sub>3</sub> are mainly given by ‘QCD corrections’ on top of them, so they are large and strongly depend on the scale choice, at variance with standard EW corrections.

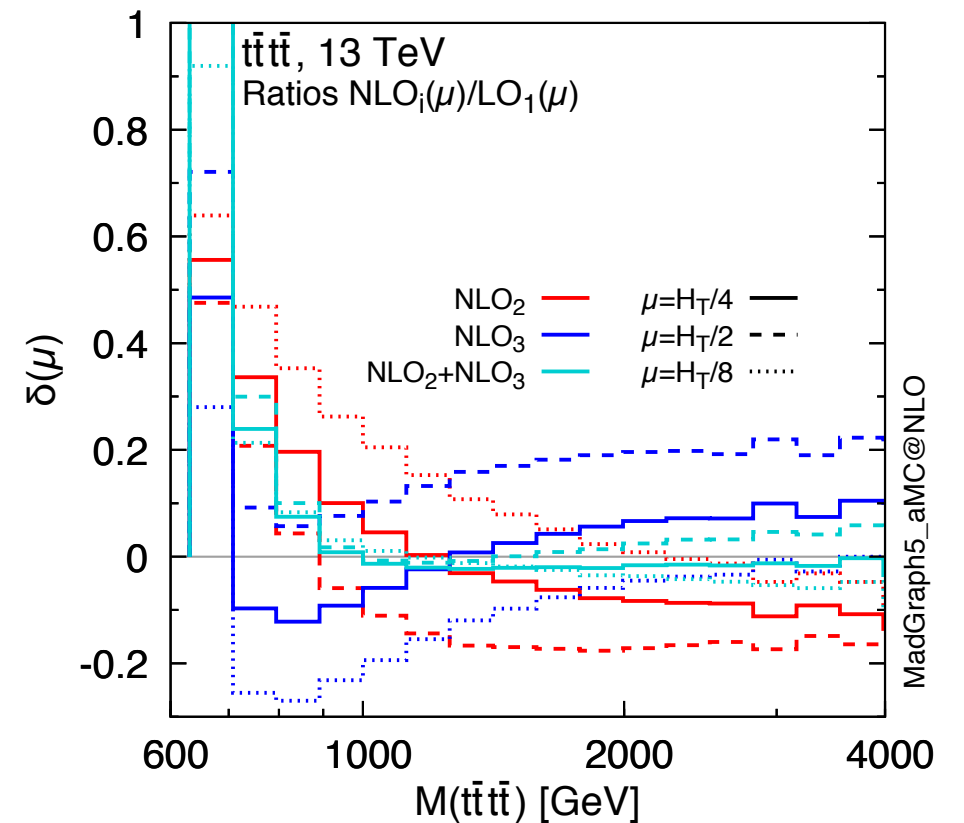
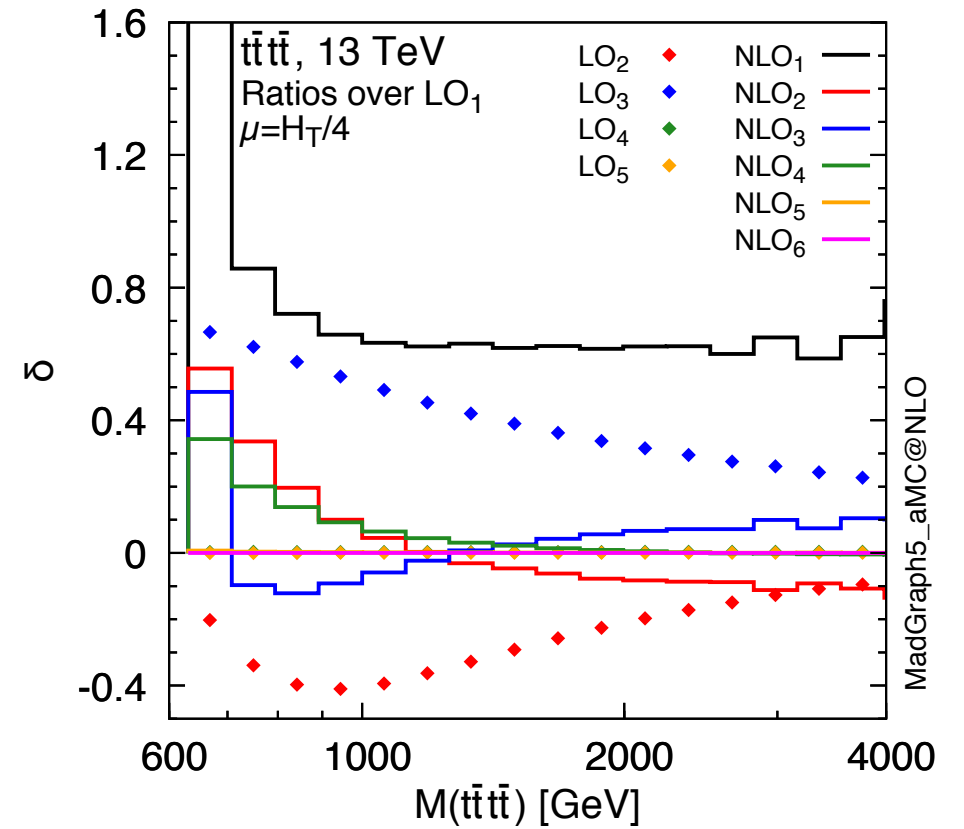
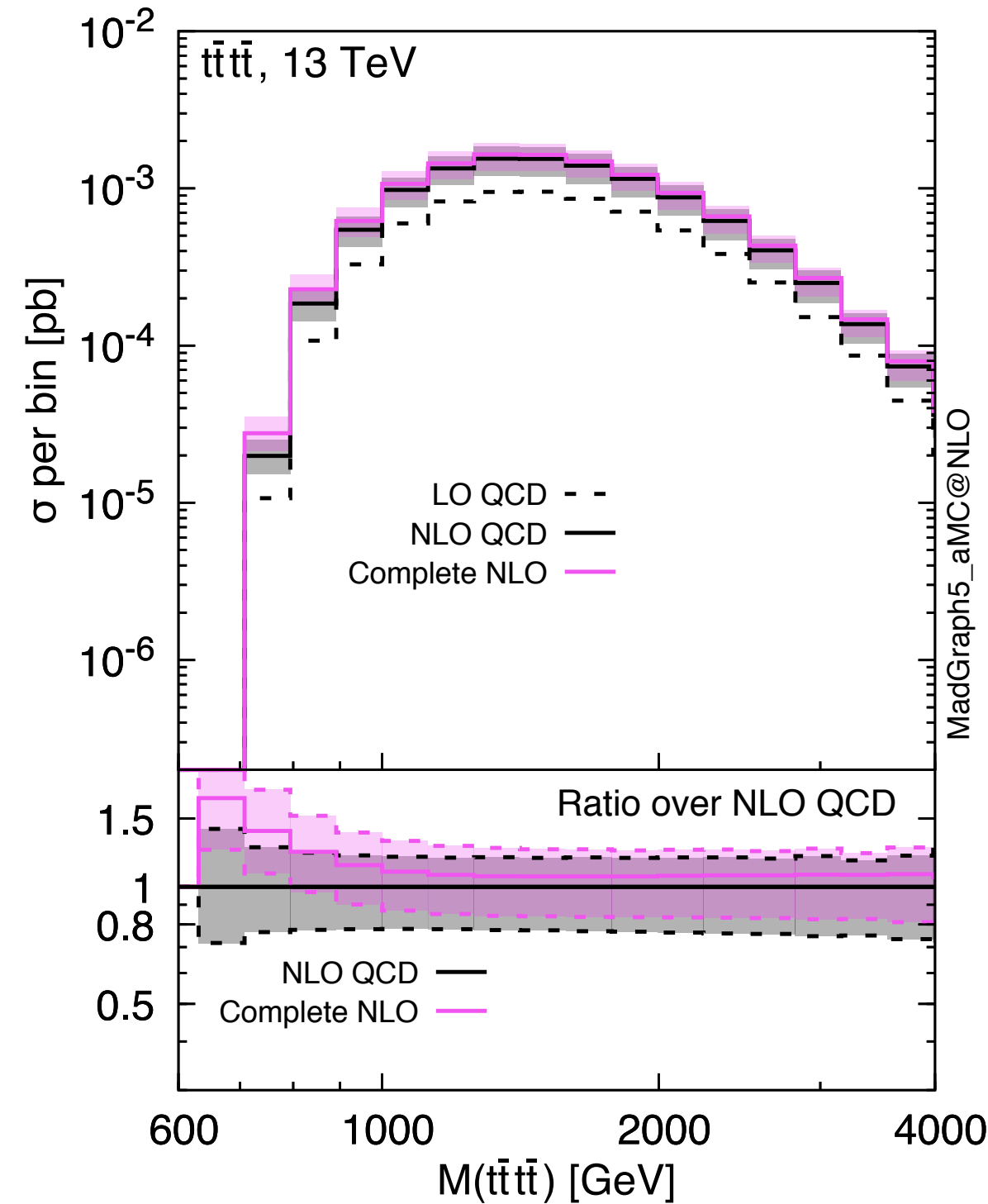
Accidentally, relatively to LO<sub>1</sub>, NLO<sub>2</sub>+NLO<sub>3</sub> scale dependence almost disappears.

**What happens if BSM enters into the game? Anomalous  $y_t$  ?**

# Distributions

13 TeV

*Frederix, DP,  
Zaro '17*



Large cancellations among (N)LO<sub>2</sub> and (N)LO<sub>3</sub> are present also at the differential level. At the threshold also NLO<sub>4</sub> is large.

# Combination with NNLO QCD

$$t\bar{t}$$

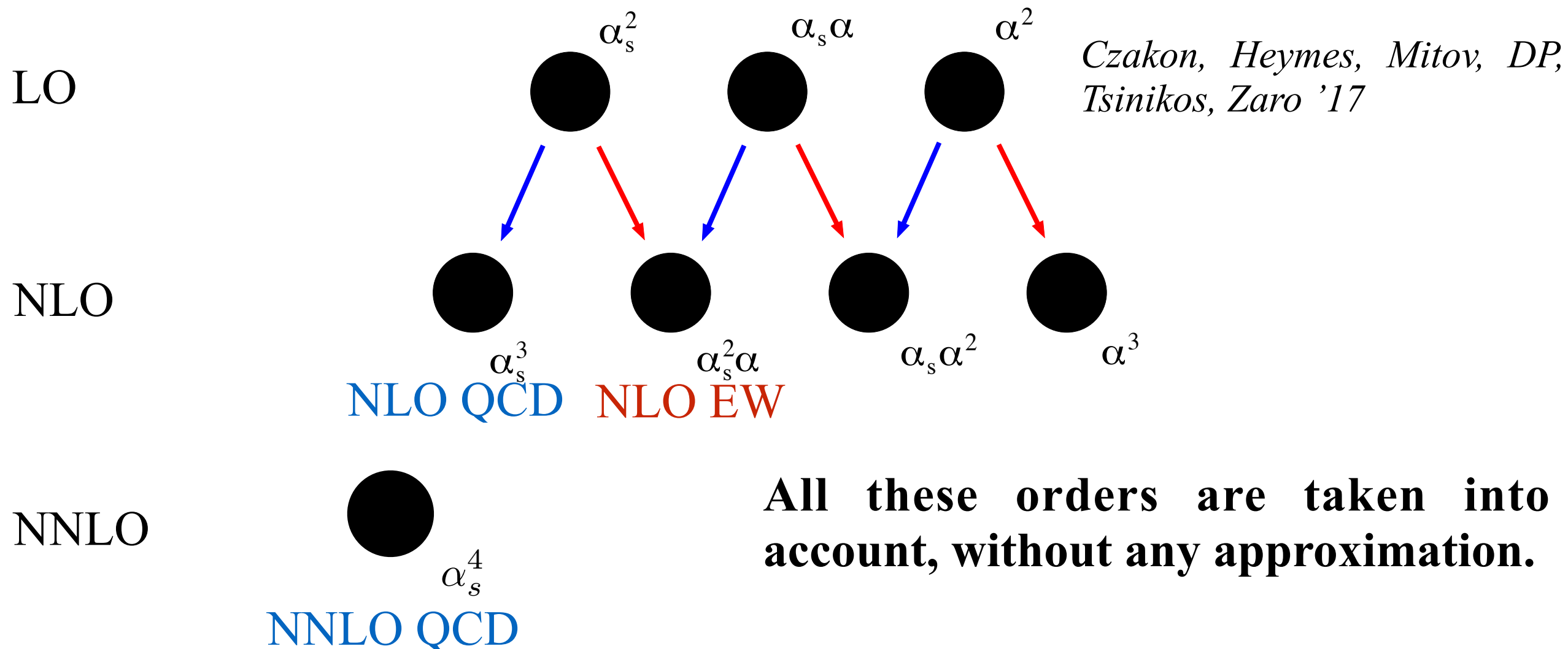
M. Czakon, D. Heymes, A. Mitov, D.P., I.Tsinikos, M. Zaro  
JHEP 1710 (2017) 186 (arXiv:1705.04105)

# NNLO QCD combined with complete-NLO

The calculation of **NNLO QCD** corrections is based on

*Czakon, Fiedler, Mitov '15*

The calculation of the **complete NLO** corrections is performed with the EW branch of **MadGraph5\_aMC@NLO**.

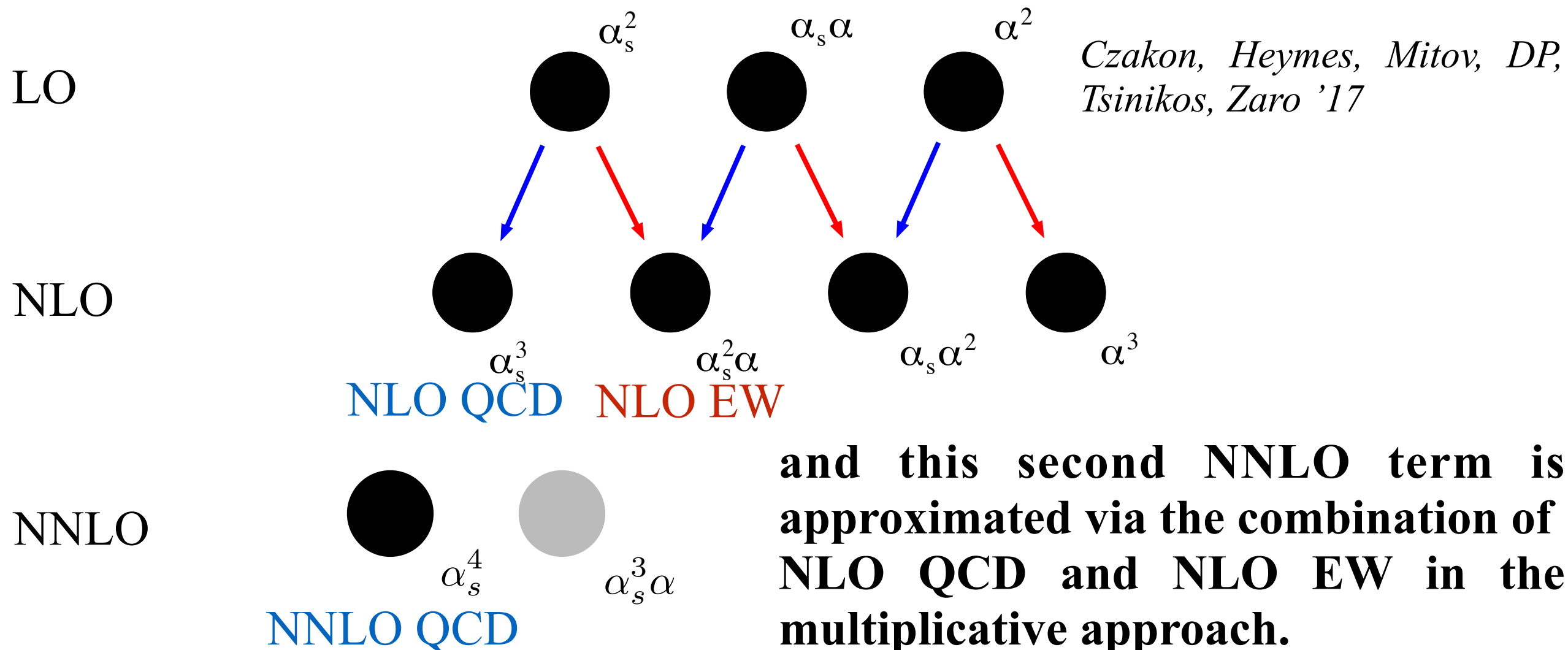


# NNLO QCD combined with complete-NLO

The calculation of **NNLO QCD** corrections is based on

*Czakon, Fiedler, Mitov '15*

The calculation of the **complete NLO** corrections is performed with the EW branch of **MadGraph5\_aMC@NLO**.



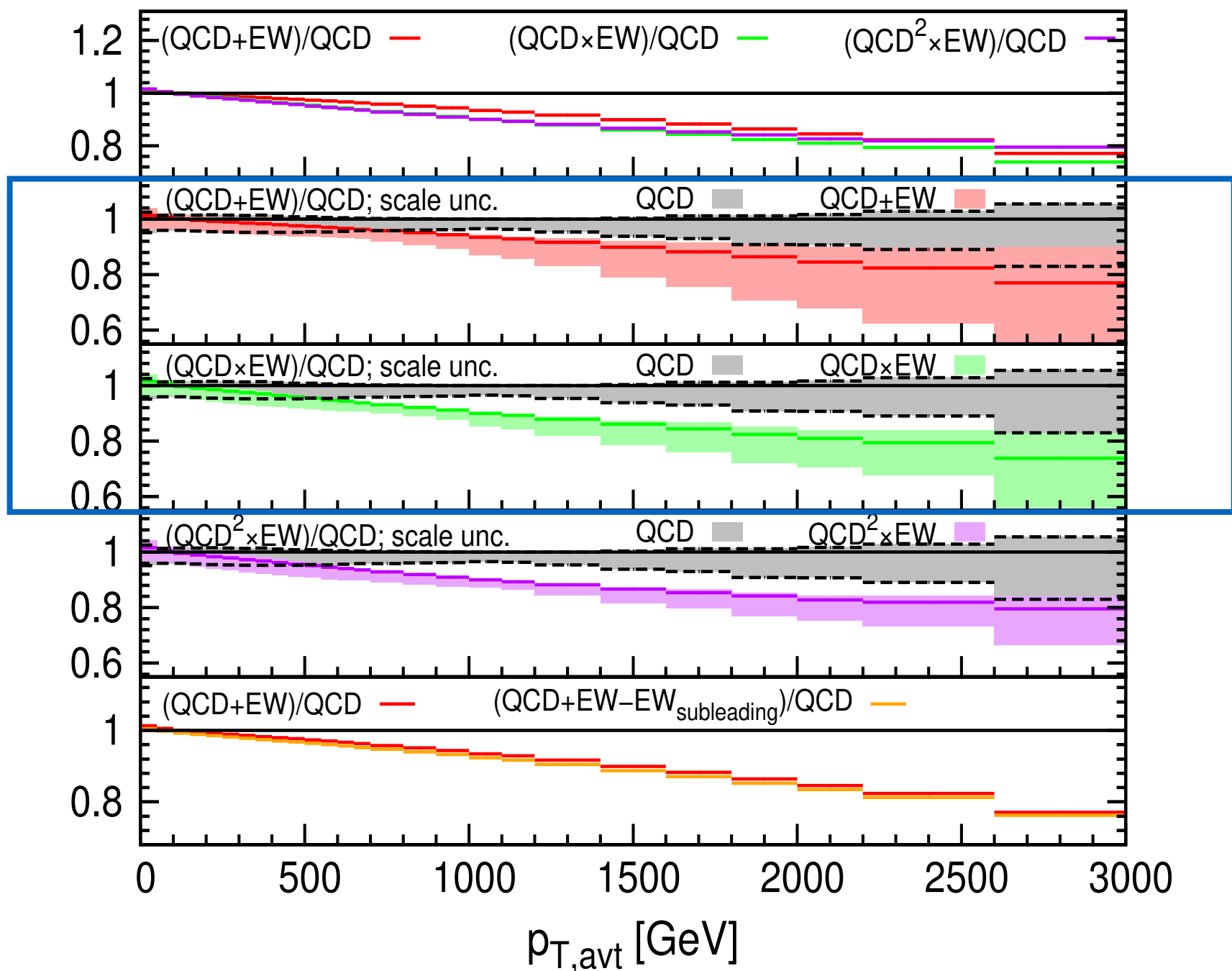
Czakov, Heymes, Mitov, DP,  
Tsinikos, Zaro '17

$p_{T,avt}$

13 TeV

**ADDITIVE**  
**MULTIPLICATIVE**

$t\bar{t}$ , LHC13, LUXqed



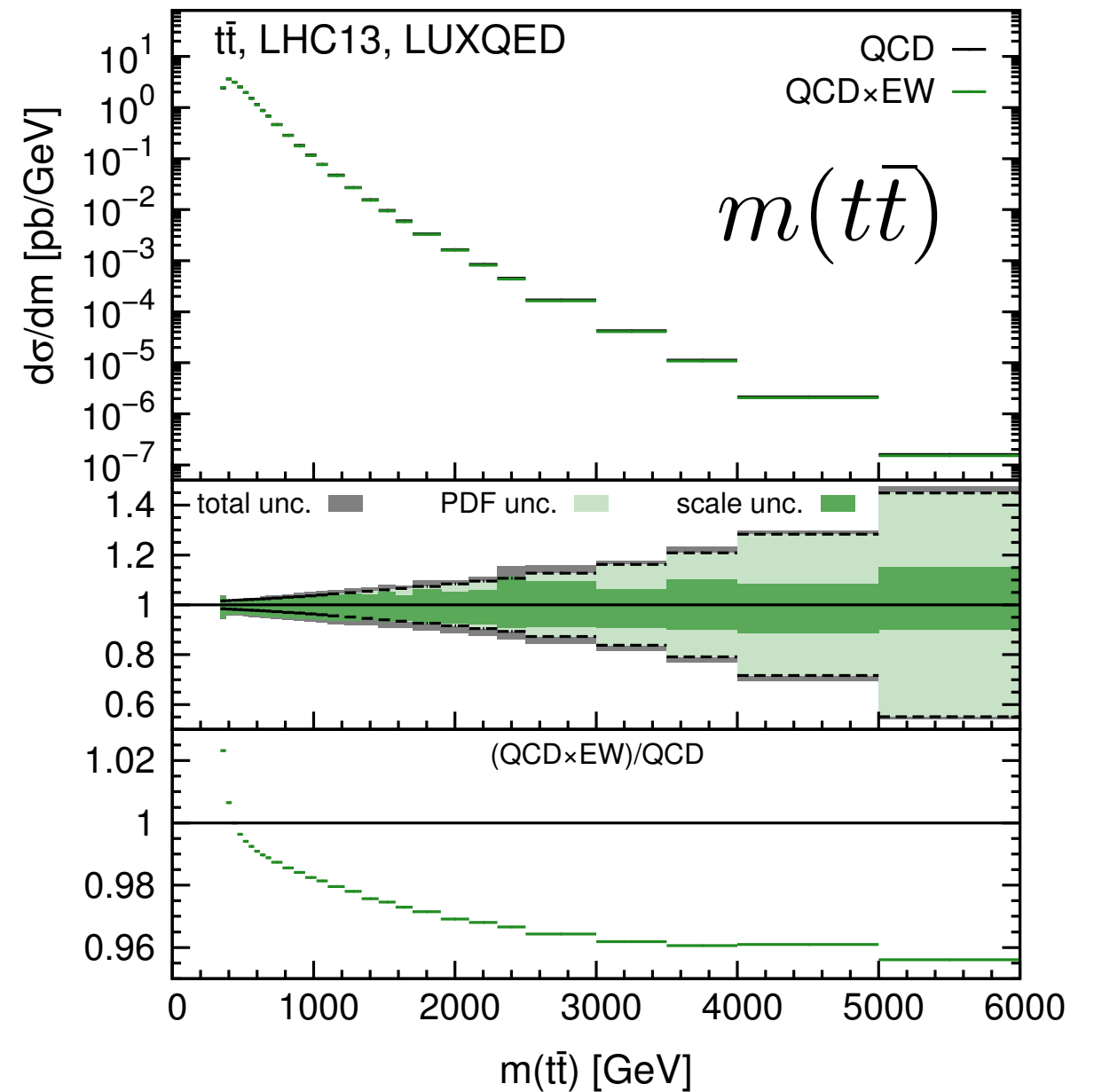
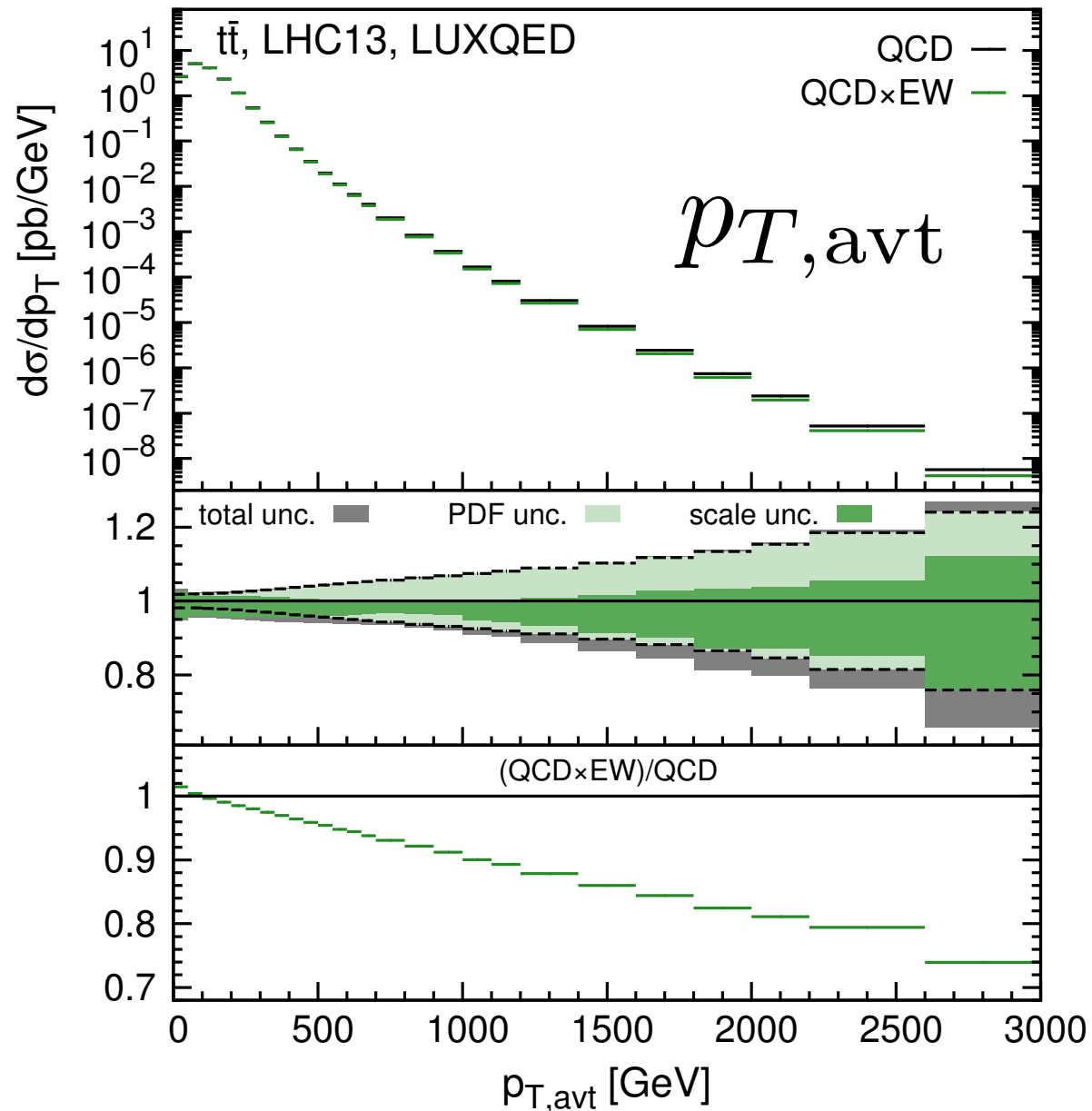
*reduction of scale unc.  
due to EW corrections,  
QCD and QCDxEW  
do not overlap  
(with LUXQED)*

# Reference Predictions

# 13 TeV

already used by CMS and ATLAS,

*Czakon, Heymes, Mitov,  
DP, Tsinikos, Zaro '17*



*scale unc.  $\sim$  PDF unc*

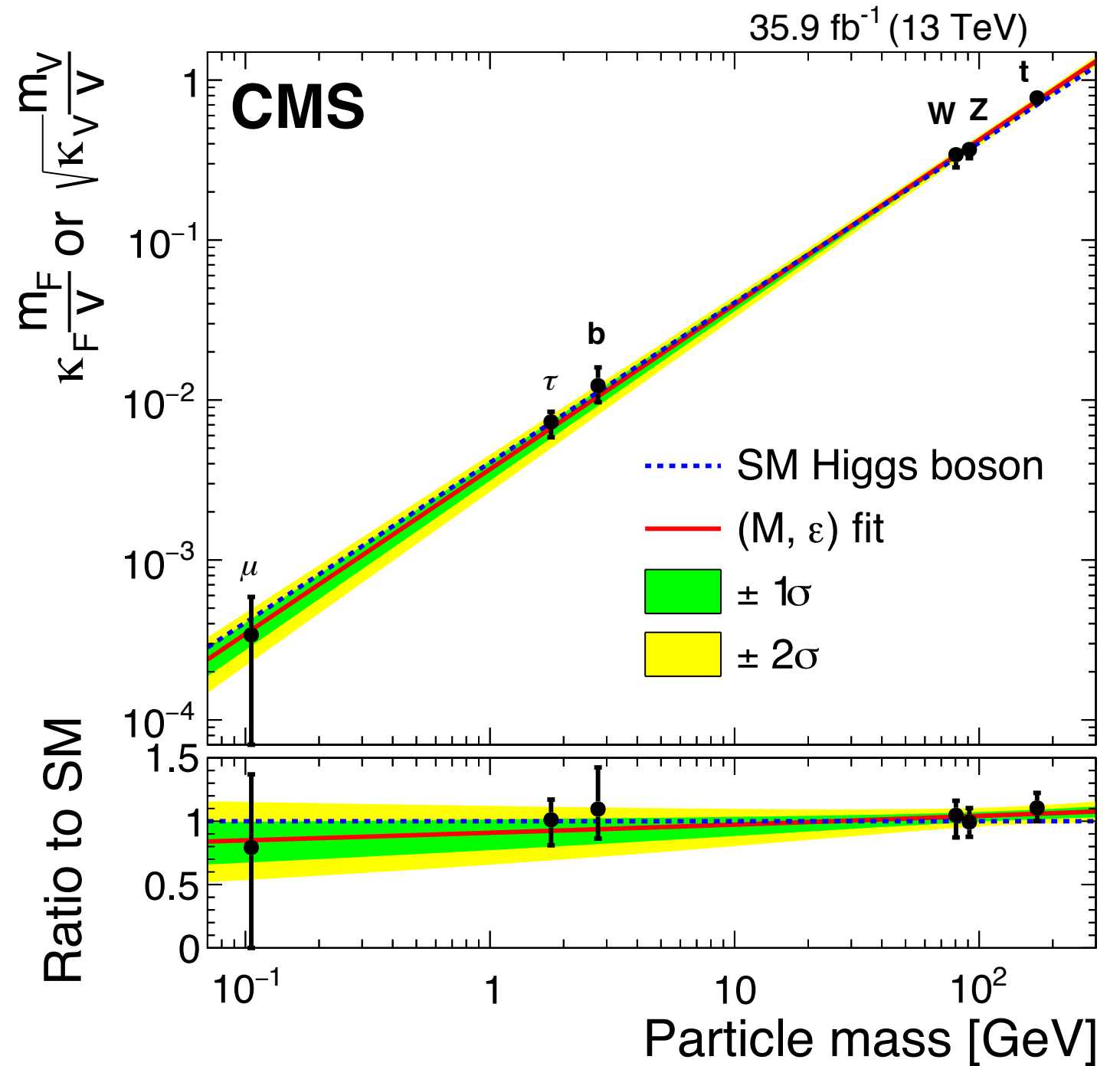
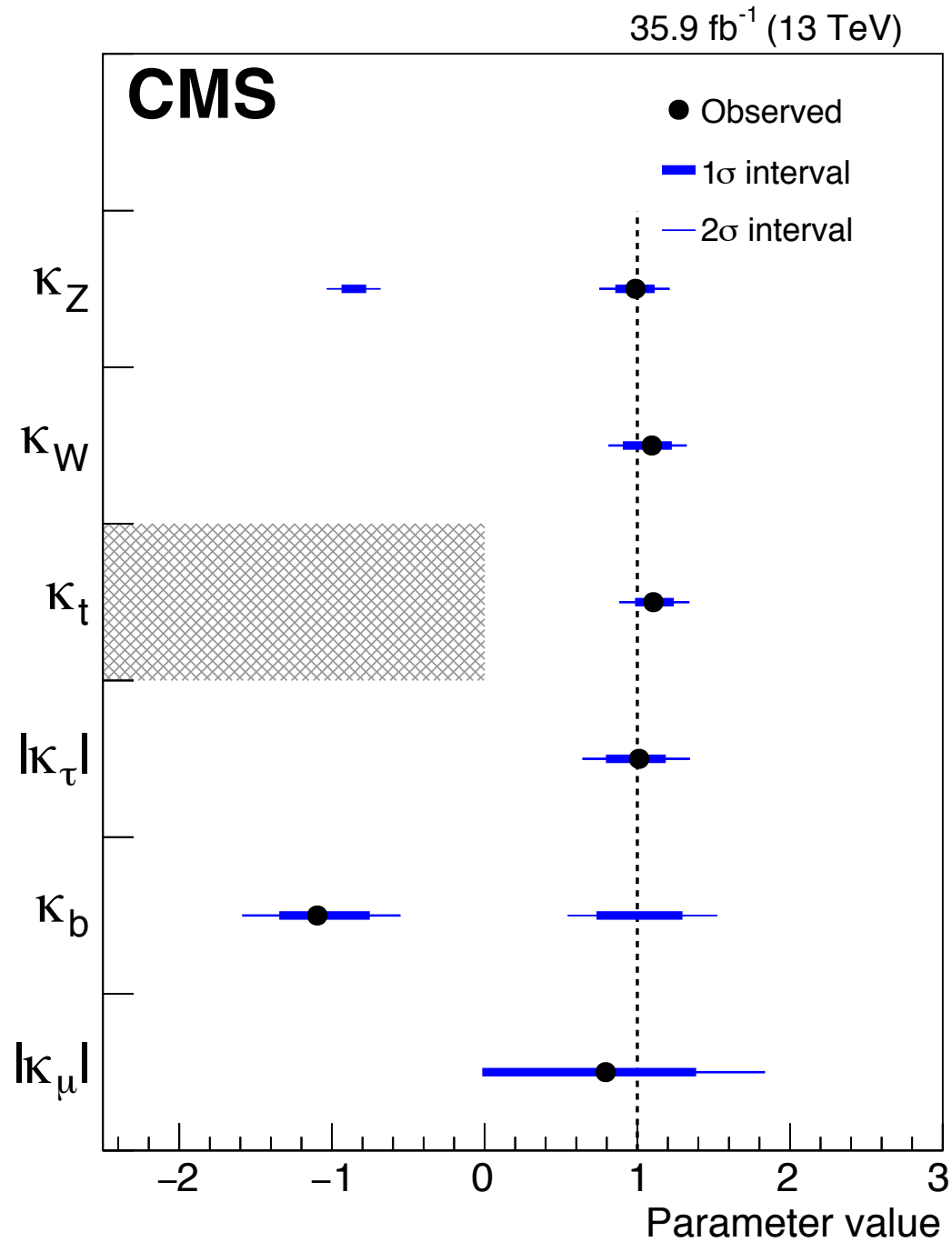
*EW corrections  $\sim$  theory error*

*scale unc.  $<$  PDF unc*

# Higgs self couplings from single Higgs production

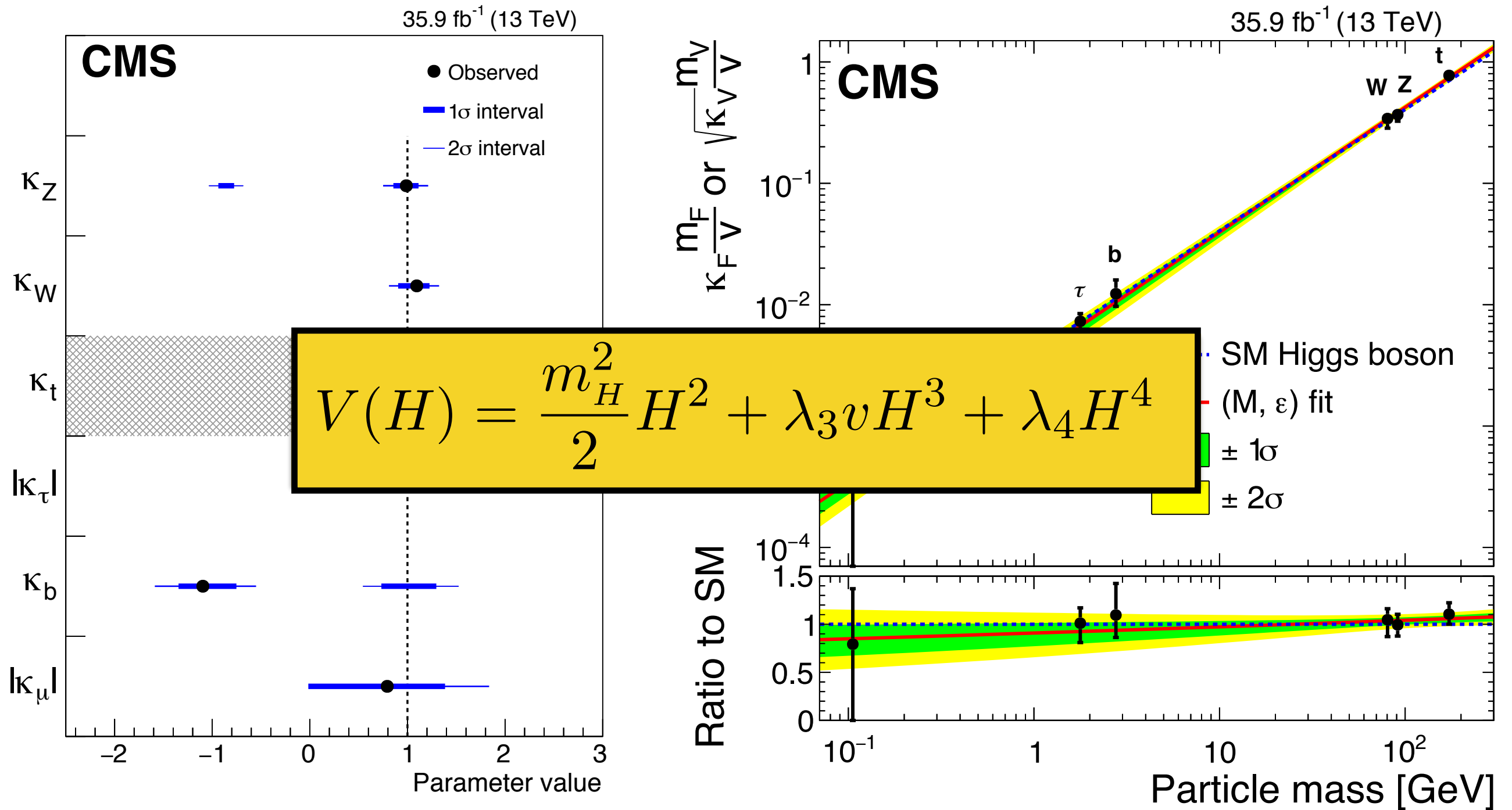


# Higgs boson couplings today



CMS-HIG-17-031

# Higgs boson couplings today



# The Higgs Potential

$$V^{\text{SM}}(\Phi) = -\mu^2(\Phi^\dagger\Phi) + \lambda(\Phi^\dagger\Phi)^2$$



$$V(H) = \frac{m_H^2}{2}H^2 + \lambda_3 v H^3 + \lambda_4 H^4$$

$$v = (\sqrt{2}G_\mu)^{-1/2} \quad \mu^2 = \frac{m_H^2}{2}$$

$$\lambda = \frac{m_H^2}{2v^2} \quad \lambda_3^{\text{SM}} = \lambda \quad \lambda_4^{\text{SM}} = \lambda/4$$

The Higgs **self couplings** are **completely determined in the SM** by the vev and the Higgs mass. On the other hand, Higgs self interactions have not been measured yet.

The measurement of the Higgs self couplings is an **important SM test**, essential for the study of the **Higgs potential**.

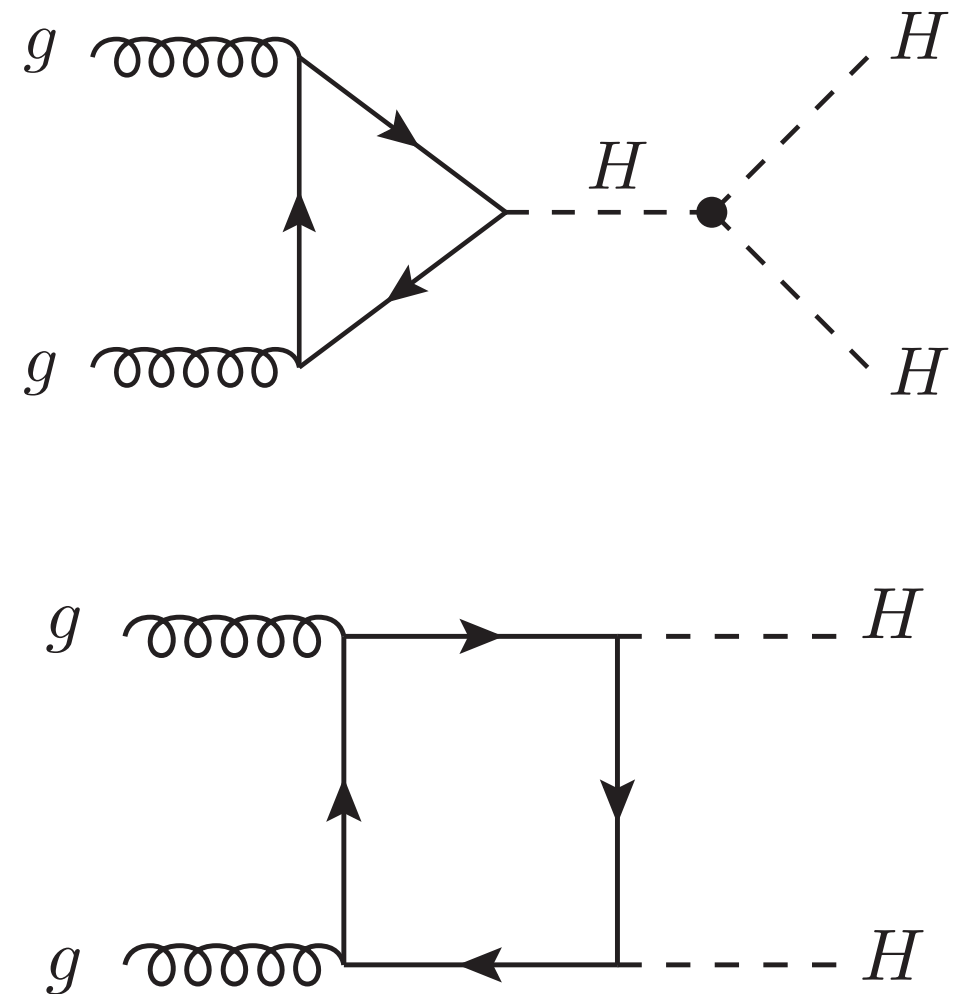
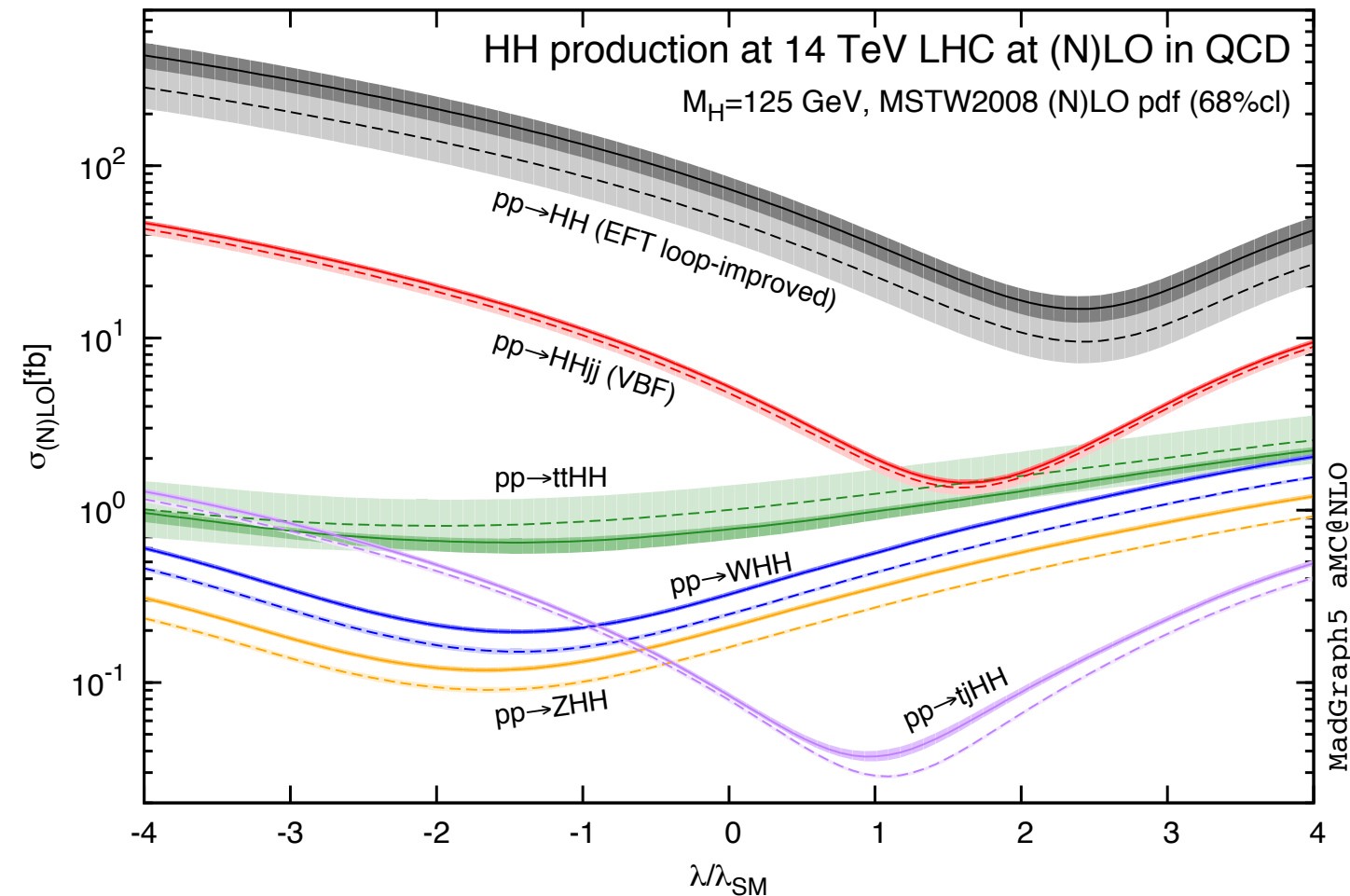
Possible deviations need to be parametrised via **additional parameters**, without altering the value of the Higgs mass and the vev.

**Interpretations** of the additional parameters strongly **depend on the theory assumptions!**

# How do we measure the Higgs self coupling?

Standard Answer: you need to produce **at least two** Higgs!

Frederix et al. '14

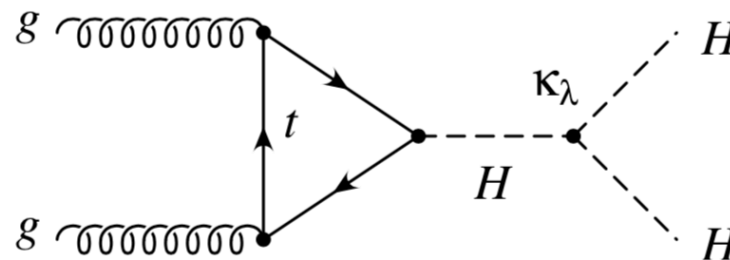


Pheno studies on LHC constraints for  $\kappa_\lambda$ :

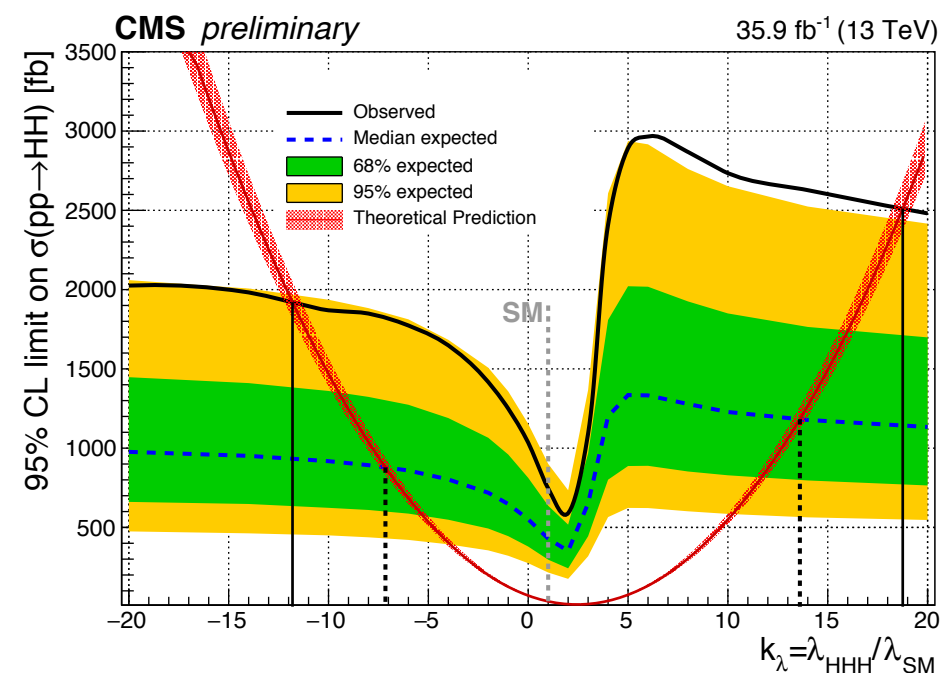
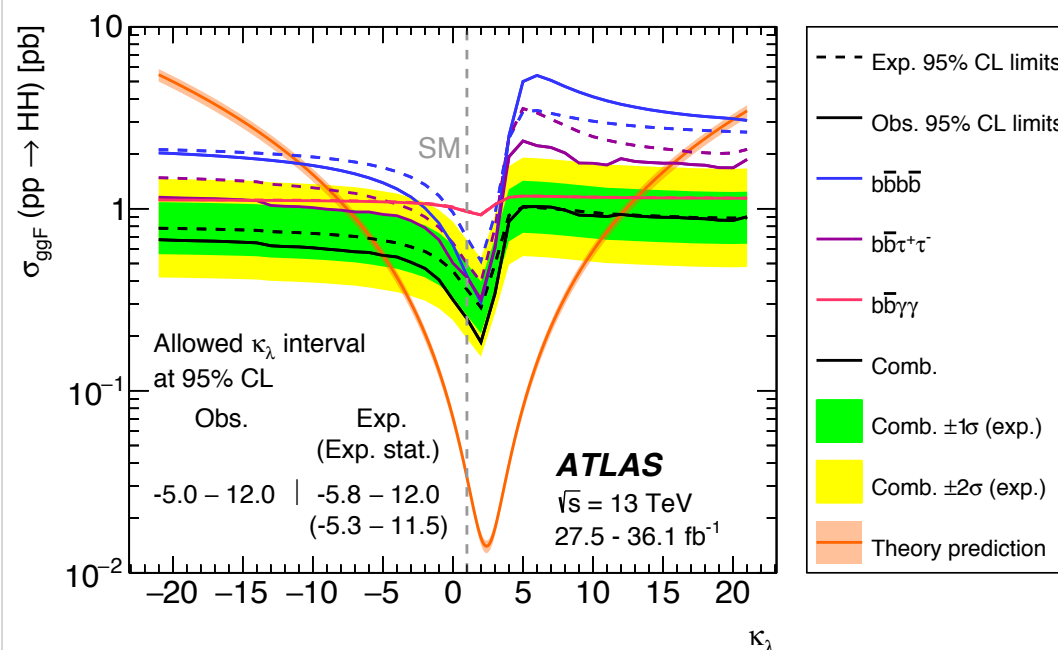
*Baur et al. '03. Baglio et al.; Papaefstathiou et al. '12. Barger et al.; Yao '13. de Lima et al.; Englert et al.; Liu and Zhang; Wardrope et al. '14. Azatov et al.; Behr et al.; Cao et al.; Dolan et al.; Lu et al. '15.*

# Latest results in the HH measurement

- The non-resonant HH production processes (ggF) provide a unique chance to probe  $\kappa_\lambda = \lambda_{HHH}/\lambda_{HHH}^{SM}$  with direct measurements



- Constrain the  $\kappa_\lambda$  by estimating the upper limits of the HH production (assuming SM H decay) with CLs approach



95% CL	Obs.	Exp.
ATLAS [ <a href="https://arxiv.org/abs/1906.02025">arXiv:1906.02025</a> ]	[-5.0, 12.0]	[-5.8, 12.0]
CMS [ <a href="https://arxiv.org/abs/1703.03346">CMS-PAS-HIG-17-030</a> ]	[-11.8, 18.8]	[-7.1, 13.6]

An additional and complementary strategy for the determination (at the LHC) of the Higgs self coupling would be desirable!

We can exploit at the LHC the  
***“High Precision for Hard Processes”***

HP<sup>2</sup>  
*It is time for something new*

*Degrassi, Giardino,  
Maltoni, DP '16*

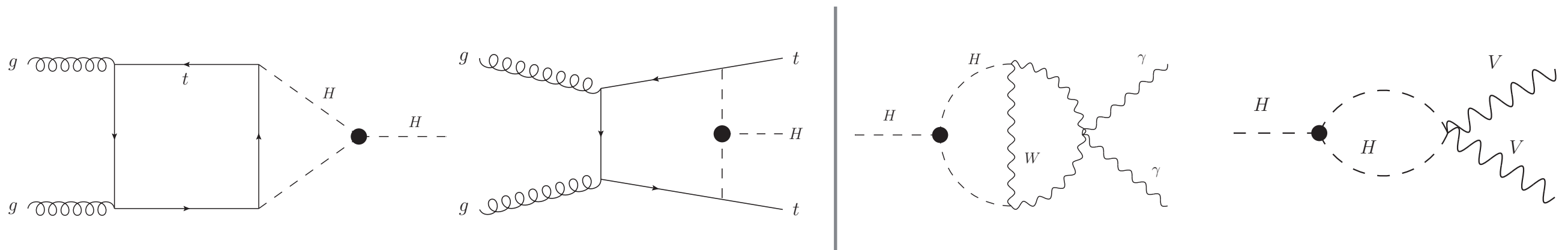
An additional and complementary strategy for the determination (at the LHC) of the Higgs self coupling would be desirable!

We can exploit at the LHC the **“High Precision for Hard Processes”**

**HP<sup>2</sup>**  
It is time for something new

Degrassi, Giardino,  
Maltoni, DP '16

and **probe** the quantum effects (NLO EW) induced by **the Higgs self coupling** on **single Higgs production and decay modes**.



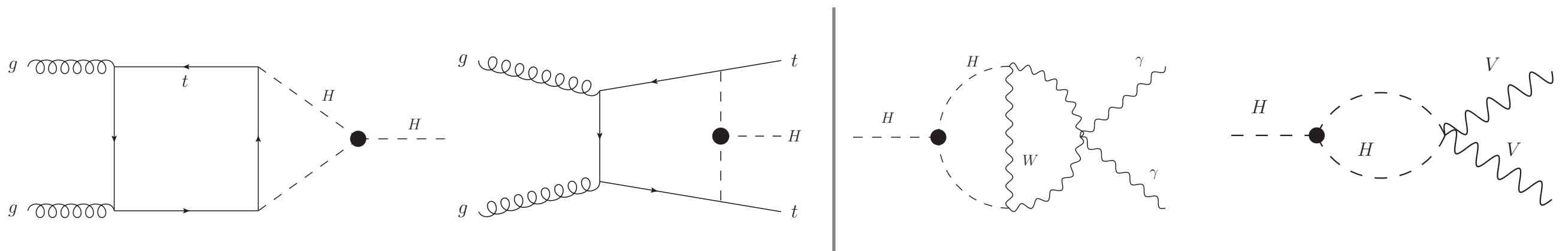
An additional and complementary strategy for the determination (at the LHC) of the Higgs self coupling would be desirable!

We can exploit at the LHC the “*High Precision for Hard Processes*”

HP<sup>2</sup>  
It is time for something new

Degrassi, Giardino,  
Maltoni, DP '16

and *probe* the quantum effects (NLO EW) induced by **the Higgs self coupling** on **single Higgs production and decay** modes.



All the single Higgs production and decay processes are affected by an anomalous trilinear (**not quartic**) Higgs self coupling, parametrized by  $\kappa_\lambda$ .

All the different signal strengths  $\mu_i^f$  have a different dependence on a single parameter  $\kappa_\lambda$ , which can thus be constrained via a global fit.

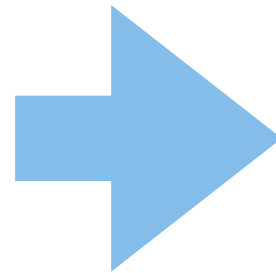


# Calculation framework

We assume that the dominant New Physics effects involve the Higgs potential. At **NLO EW** only the trilinear Higgs self coupling appears; the quartic-coupling dependence enters only at higher orders.

SM

$$V(H) = \frac{m_H^2}{2} H^2 + \lambda_3 v H^3 + \lambda_4 H^4$$
$$m_H^2 = 2\lambda v^2, \lambda_3^{\text{SM}} = \lambda, \lambda_4^{\text{SM}} = \lambda/4$$



NP parameterised via

$$\lambda_3 v H^3 \equiv \kappa_\lambda \lambda_3^{\text{SM}} v H^3$$

*Degrassi, Giardino, Maltoni, DP '16*

The possible range of  $\kappa_\lambda$ , even before the comparison with data, depends on the underlying theory assumptions and it applies also to double-Higgs analyses.

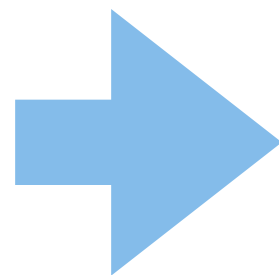
---

# Calculation framework

We assume that the dominant New Physics effects involve the Higgs potential. At **NLO EW** only the trilinear Higgs self coupling appears; the quartic-coupling dependence enters only at higher orders.

SM

$$V(H) = \frac{m_H^2}{2} H^2 + \lambda_3 v H^3 + \lambda_4 H^4$$
$$m_H^2 = 2\lambda v^2, \lambda_3^{\text{SM}} = \lambda, \lambda_4^{\text{SM}} = \lambda/4$$



NP parameterised via

$$\lambda_3 v H^3 \equiv \kappa_\lambda \lambda_3^{\text{SM}} v H^3$$

*Degrassi, Giardino, Maltoni, DP '16*

The possible range of  $\kappa_\lambda$ , even before the comparison with data, depends on the underlying theory assumptions and it applies also to double-Higgs analyses.

---

Equivalent study for only ZH production at e<sup>+</sup>e<sup>-</sup> collider in *McCullough '14*

Similar studies in EFT approach for only gluon-fusion with decays into photons in *Gorbahn, Haisch '16*, and for VBF+VH in *Bizon, Gorbahn, Haisch, Zanderighi '16*

# Numerical results

*Degrassi, Giardino, Maltoni, DP '16*

$$\delta\Sigma_{\lambda_3} \equiv \frac{\Sigma_{\text{NLO}} - \Sigma_{\text{NLO}}^{\text{SM}}}{\Sigma_{\text{LO}}} = (\kappa_\lambda - 1) \boxed{C_1} + (\kappa_\lambda^2 - 1) \boxed{C_2} + \mathcal{O}(\kappa_\lambda^3 \alpha^2) \quad C_2 = \frac{\delta Z_H}{(1 - \kappa_\lambda^2 \delta Z_H)}$$

**universal**

Process and kinetic dependent

$$C_2 = -9.514 \cdot 10^{-4} \text{ for } \kappa_\lambda = \pm 20 \quad C_2 = -1.536 \cdot 10^{-3} \text{ for } \kappa_\lambda = 1$$

# Numerical results

*Degrassi, Giardino, Maltoni, DP '16*

$$\delta\Sigma_{\lambda_3} \equiv \frac{\Sigma_{\text{NLO}} - \Sigma_{\text{NLO}}^{\text{SM}}}{\Sigma_{\text{LO}}} = (\kappa_\lambda - 1) \boxed{C_1} + (\kappa_\lambda^2 - 1) \boxed{C_2} + \mathcal{O}(\kappa_\lambda^3 \alpha^2) \quad C_2 = \frac{\delta Z_H}{(1 - \kappa_\lambda^2 \delta Z_H)}$$

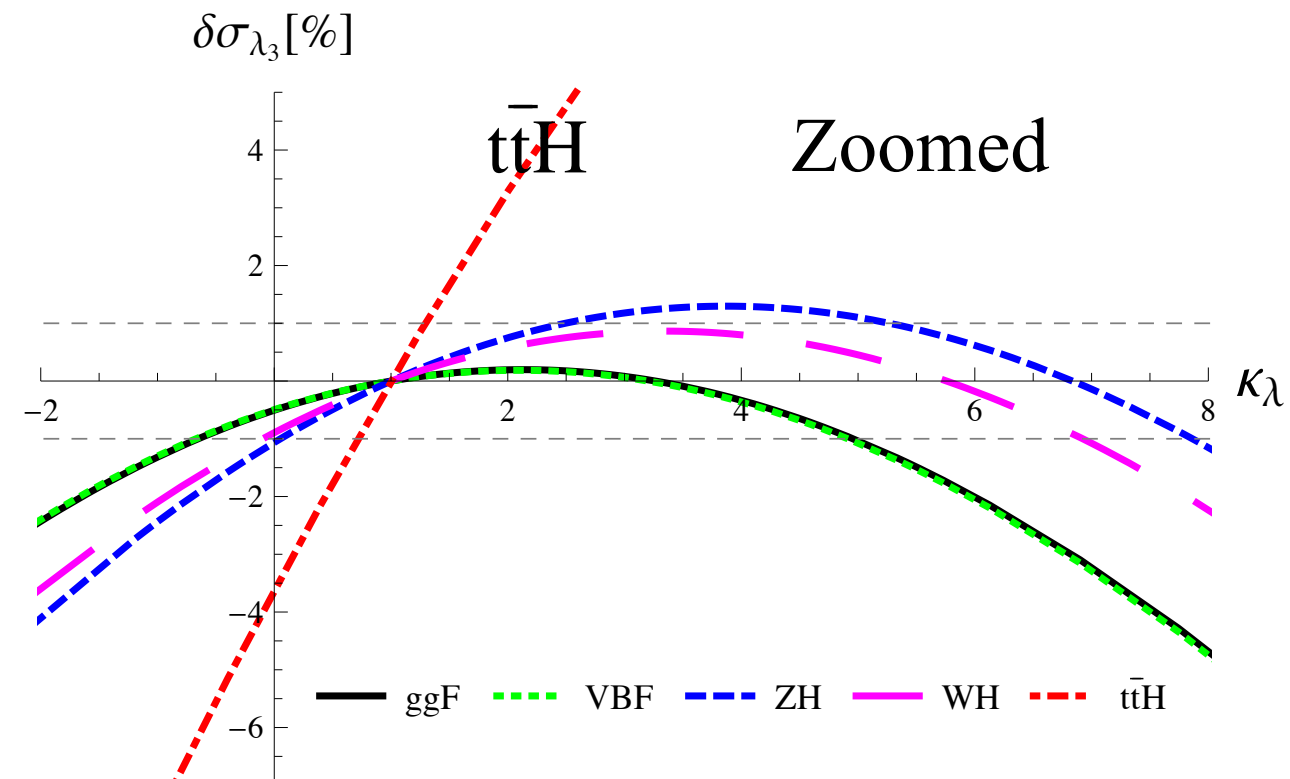
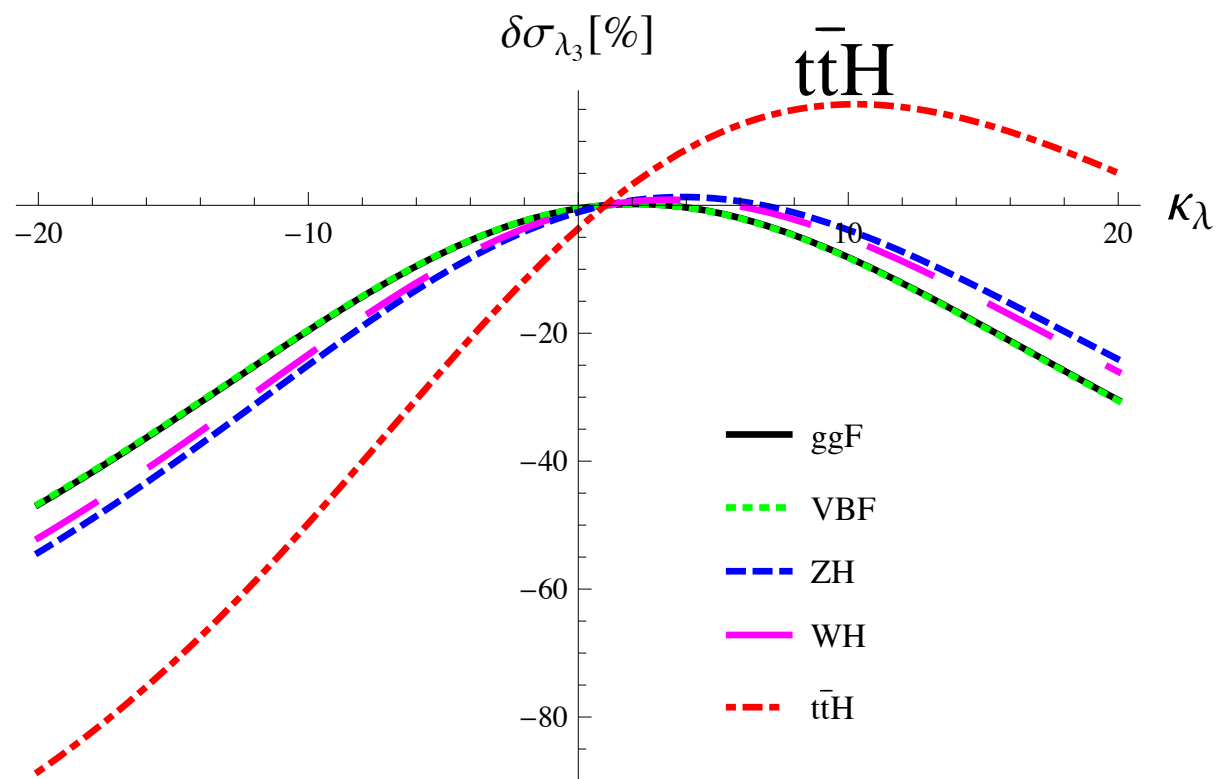
universal

Process and kinetic dependent

$$C_2 = -9.514 \cdot 10^{-4} \text{ for } \kappa_\lambda = \pm 20 \quad C_2 = -1.536 \cdot 10^{-3} \text{ for } \kappa_\lambda = 1$$

Production:  $\delta\sigma_{\lambda_3}$

$C_1^\sigma$ [%]	ggF	VBF	WH	ZH	$t\bar{t}H$
8 TeV	0.66	0.65	1.05	1.22	3.78
13 TeV	0.66	0.64	1.03	1.19	3.51



# Numerical results

*Degrassi, Giardino, Maltoni, DP '16*

$$\delta\Sigma_{\lambda_3} \equiv \frac{\Sigma_{\text{NLO}} - \Sigma_{\text{NLO}}^{\text{SM}}}{\Sigma_{\text{LO}}} = (\kappa_\lambda - 1) \boxed{C_1} + (\kappa_\lambda^2 - 1) \boxed{C_2} + \mathcal{O}(\kappa_\lambda^3 \alpha^2) \quad C_2 = \frac{\delta Z_H}{(1 - \kappa_\lambda^2 \delta Z_H)}$$

universal

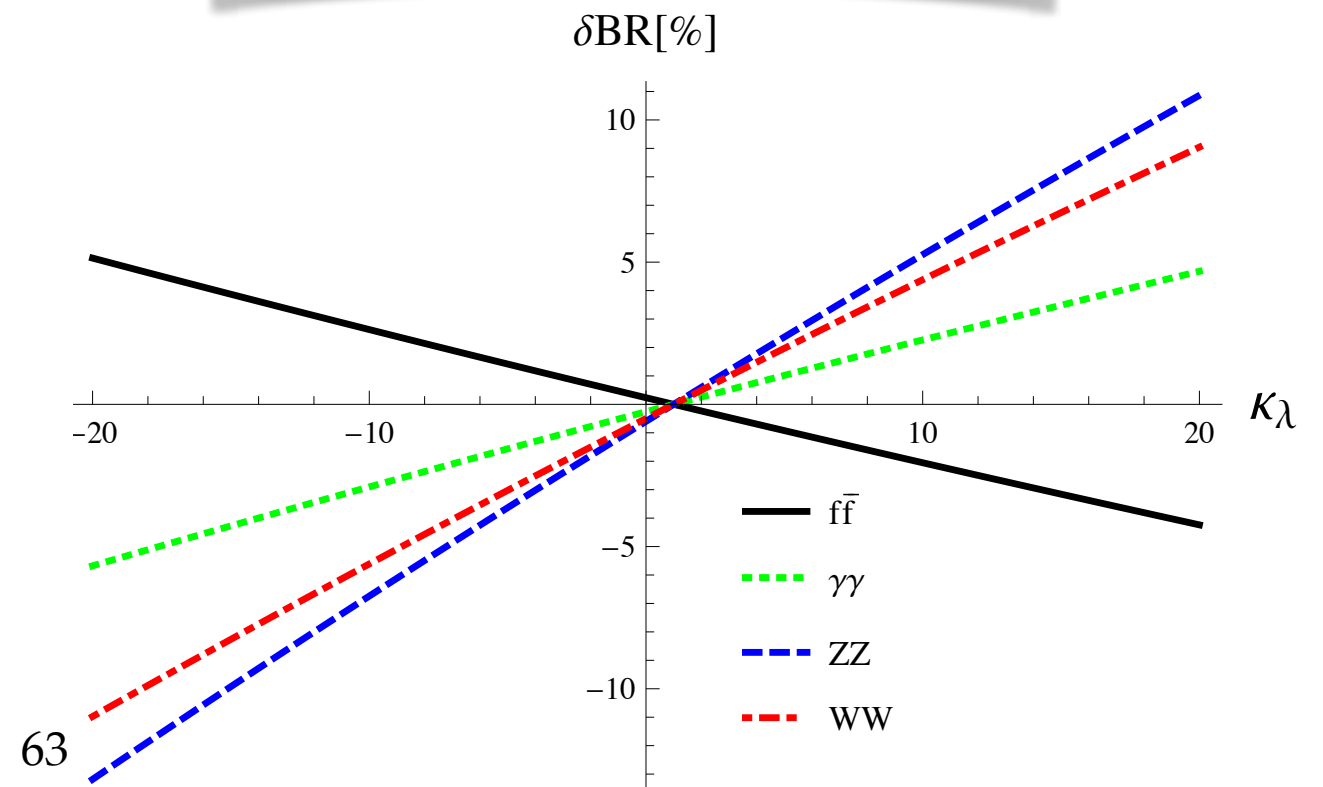
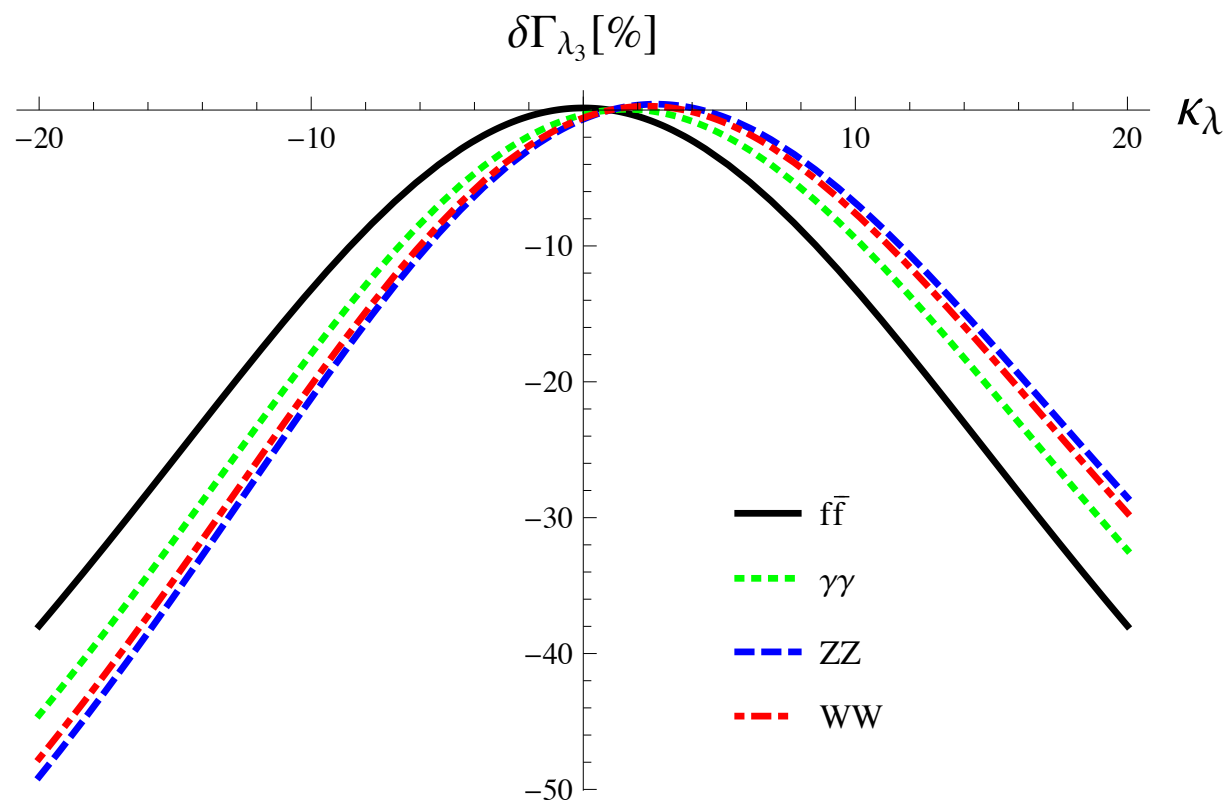
Process and kinetic dependent

$$C_2 = -9.514 \cdot 10^{-4} \text{ for } \kappa_\lambda = \pm 20 \quad C_2 = -1.536 \cdot 10^{-3} \text{ for } \kappa_\lambda = 1$$

Decay:  $\delta\Gamma_{\lambda_3}$  and  $\delta\text{BR}_{\lambda_3}$

$C_1^\Gamma$ [%]	$\gamma\gamma$	$ZZ$	$WW$	$f\bar{f}$	$gg$
on-shell $H$	0.49	0.83	0.73	0	0.66

$$\delta\text{BR}_{\lambda_3}(i) = \frac{(\kappa_\lambda - 1)(C_1^\Gamma(i) - C_1^{\Gamma_{\text{tot}}})}{1 + (\kappa_\lambda - 1)C_1^{\Gamma_{\text{tot}}}}$$

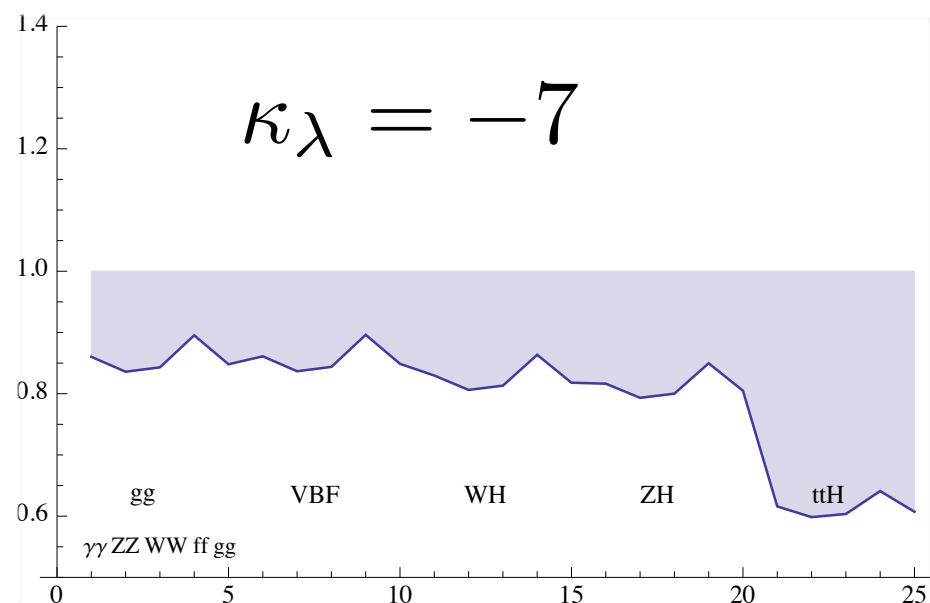


# Fitting from LHC current analysis

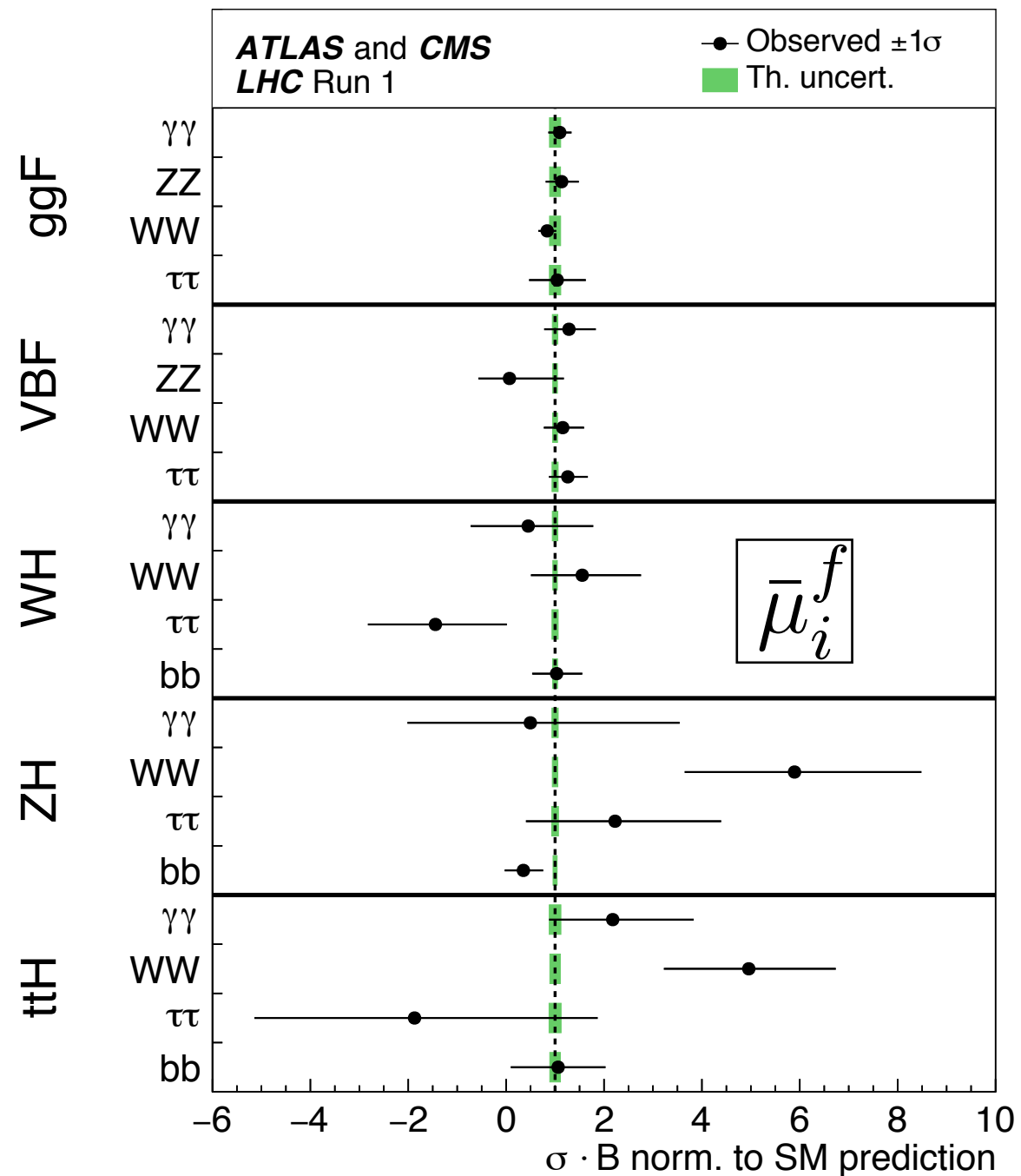
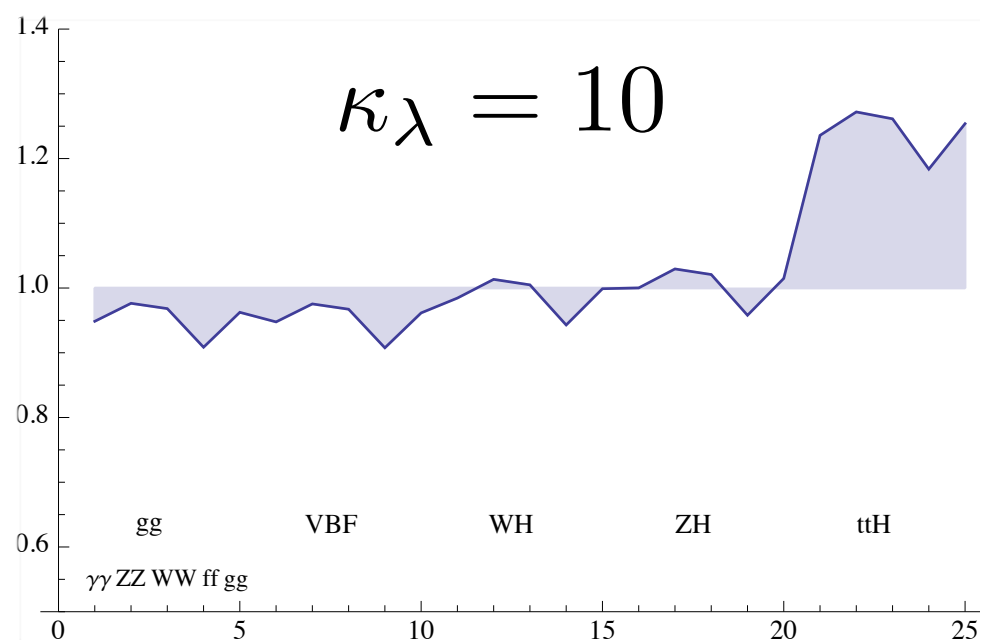
$$i \rightarrow H \rightarrow f \quad \rightarrow \quad \mu_i^f \equiv \mu_i \times \mu^f$$

$$\mu_i = 1 + \delta\sigma_{\lambda_3}(i)$$

$$\mu^f = 1 + \delta\text{BR}_{\lambda_3}(f)$$



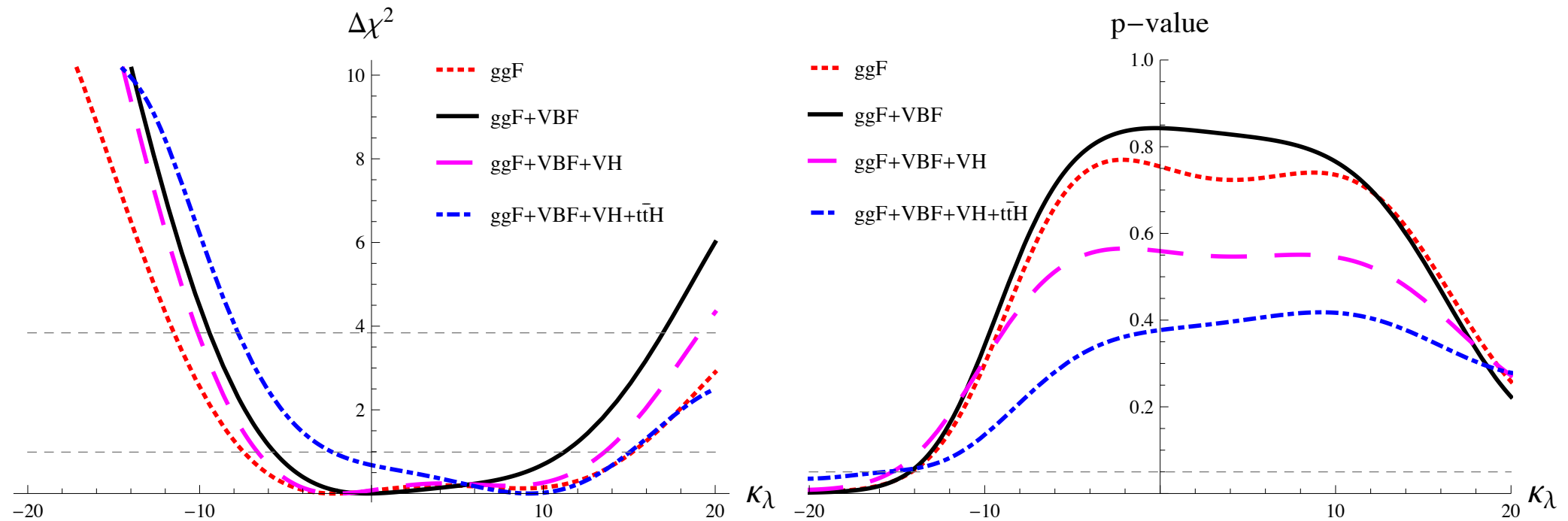
$$\mu_i^f(\kappa_\lambda)$$



# Results for present data (8 TeV)

Minimization of

$$\chi^2(\kappa_\lambda) \equiv \sum_{\bar{\mu}_i^f \in \{\bar{\mu}_i^f\}} \frac{(\mu_i^f(\kappa_\lambda) - \bar{\mu}_i^f)^2}{(\Delta_i^f(\kappa_\lambda))^2}$$



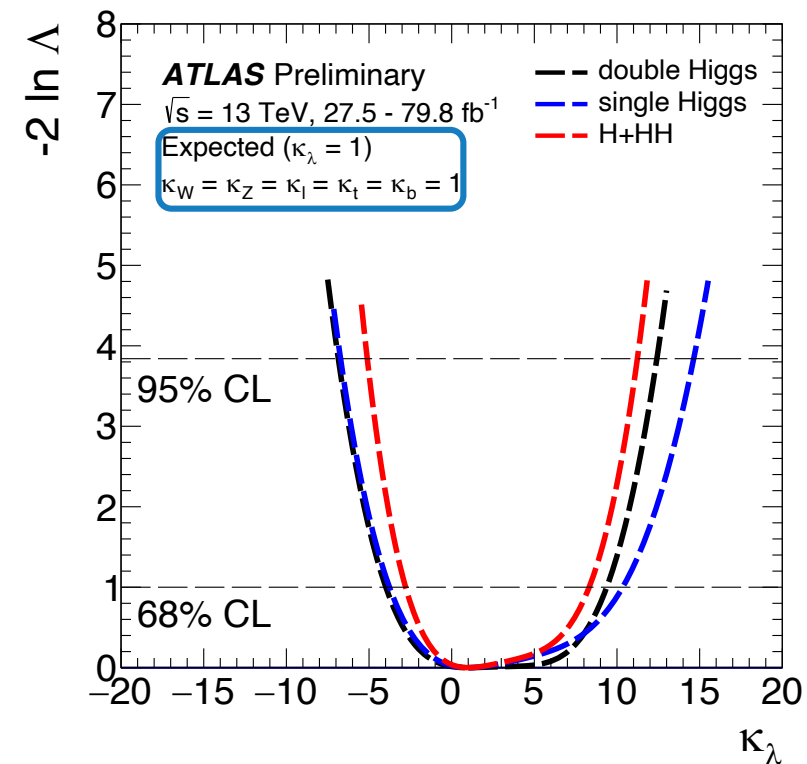
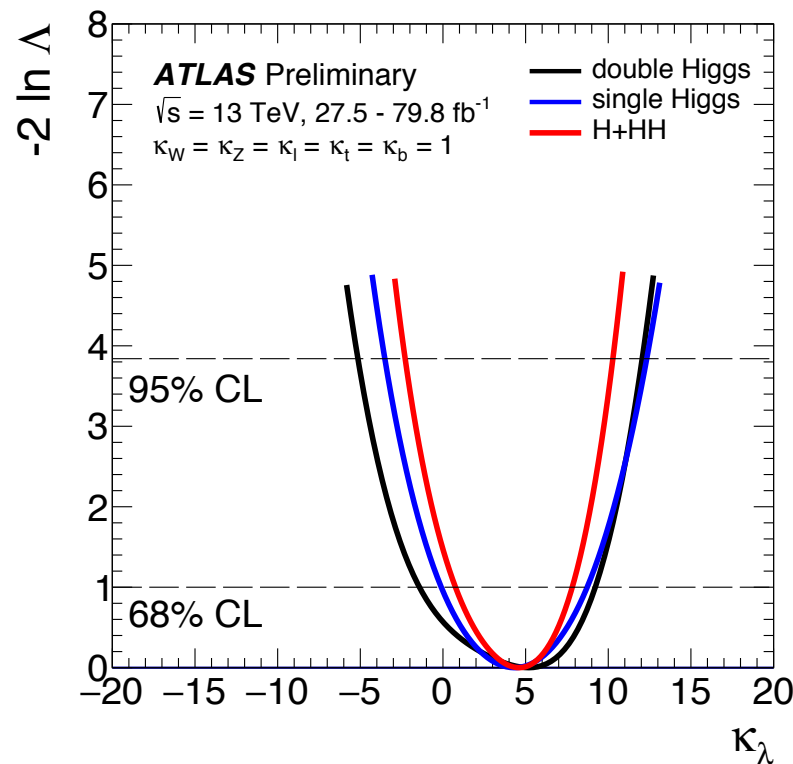
$$\kappa_\lambda^{\text{best}} = -0.24, \quad \kappa_\lambda^{1\sigma} = [-5.6, 11.2], \quad \kappa_\lambda^{2\sigma} = [-9.4, 17.0]$$

*Degrassi, Giardino, Maltoni, DP '16*

This alternative strategy is already now competitive and complementary to double-Higgs production measurements!

# $\kappa_\lambda$ -only results slide from Kunlin Ran talk (ATLAS)

- A likelihood fit is performed to constrain  $\kappa_\lambda$  in the combination of single-Higgs and double-Higgs
- All other Higgs boson couplings are fixed to the SM ( $\kappa_t = \kappa_b = \kappa_l = \kappa_W = \kappa_Z = 1$ )



- $\kappa_\lambda = 4.6_{-3.8}^{+3.2} = 4.6_{-3.5}^{+2.9}(\text{stat.})_{-1.2}^{+1.2}(\text{exp.})_{-0.5}^{+0.7}(\text{sig. th.})_{-1.0}^{+0.6}(\text{bkg. th.})$  (obs.)
- $\kappa_\lambda = 1.0_{-3.8}^{+7.3} = 1.0_{-3.0}^{+6.2}(\text{stat.})_{-1.7}^{+3.0}(\text{exp.})_{-1.2}^{+1.8}(\text{sig. th.})_{-1.1}^{+1.7}(\text{bkg. th.})$  (exp.)

95% CL	Obs.	Exp.
H [ <a href="#">ATL-PHYS-PUB-2019-009</a> ]	[-3.2, 11.9]	[-6.2, 14.4]
HH [ <a href="#">arXiv:1906.02025</a> ]	[-5.0, 12.0]	[-5.8, 12.0]
H+HH [ <a href="#">ATLAS-CONF-2019-049</a> ]	[-2.3, 10.3]	[-5.1, 11.2]

- The combination can better constrain  $\kappa_\lambda$



# Combined fit with others EFT parameters

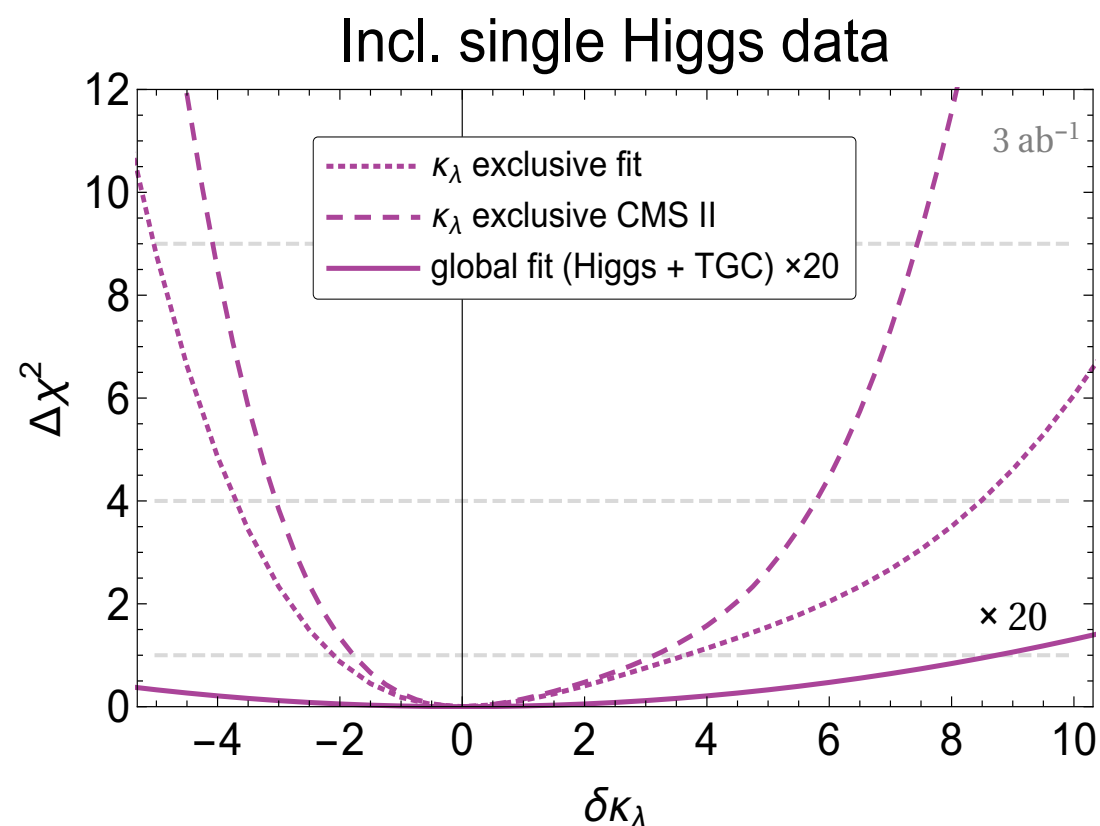
How are limits on  $\kappa_\lambda$  affected by lifting the condition that Higgs interactions with the other particle are SM-like? *Di Vita, Grojean, Panico, Riemann, Vantalon '17*

## Assumptions:

- Consider **all** the possible EFT dimension-6 operators that enter **only** in single Higgs production and decay (**10** independent parameters).

*tree-level:*  $\{\delta c_z, c_{zz}, c_{z\Box}, \hat{c}_{z\gamma}, \hat{c}_{\gamma\gamma}, \hat{c}_{gg}, \delta y_t, \delta y_b, \delta y_\tau$  *loop:*  $\kappa_\lambda$

- Consider **only inclusive** single-Higgs observable (**9** independent constraints)



**10** parameters vs **9** constraints  $\rightarrow$  1 flat direction so no constraints for the weakest:  $\kappa_\lambda$

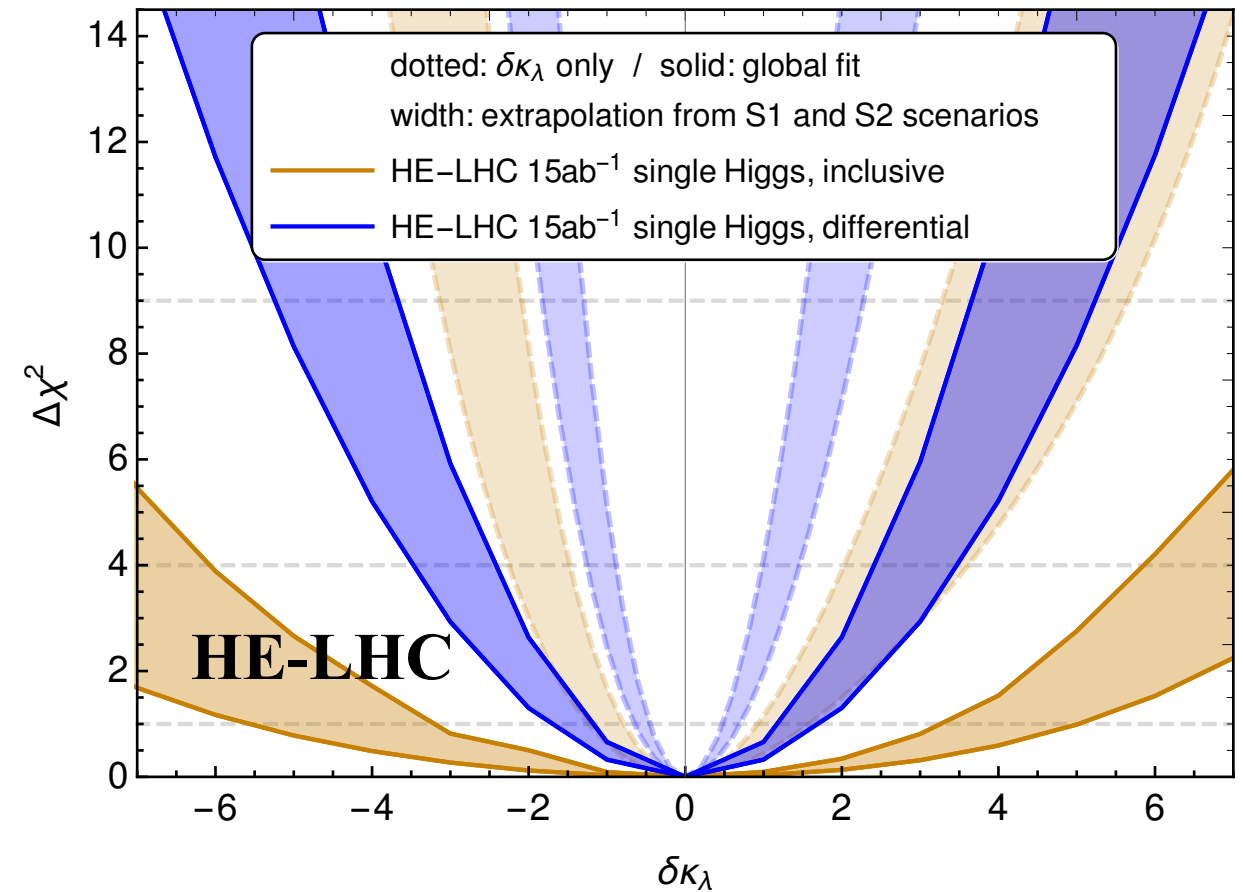
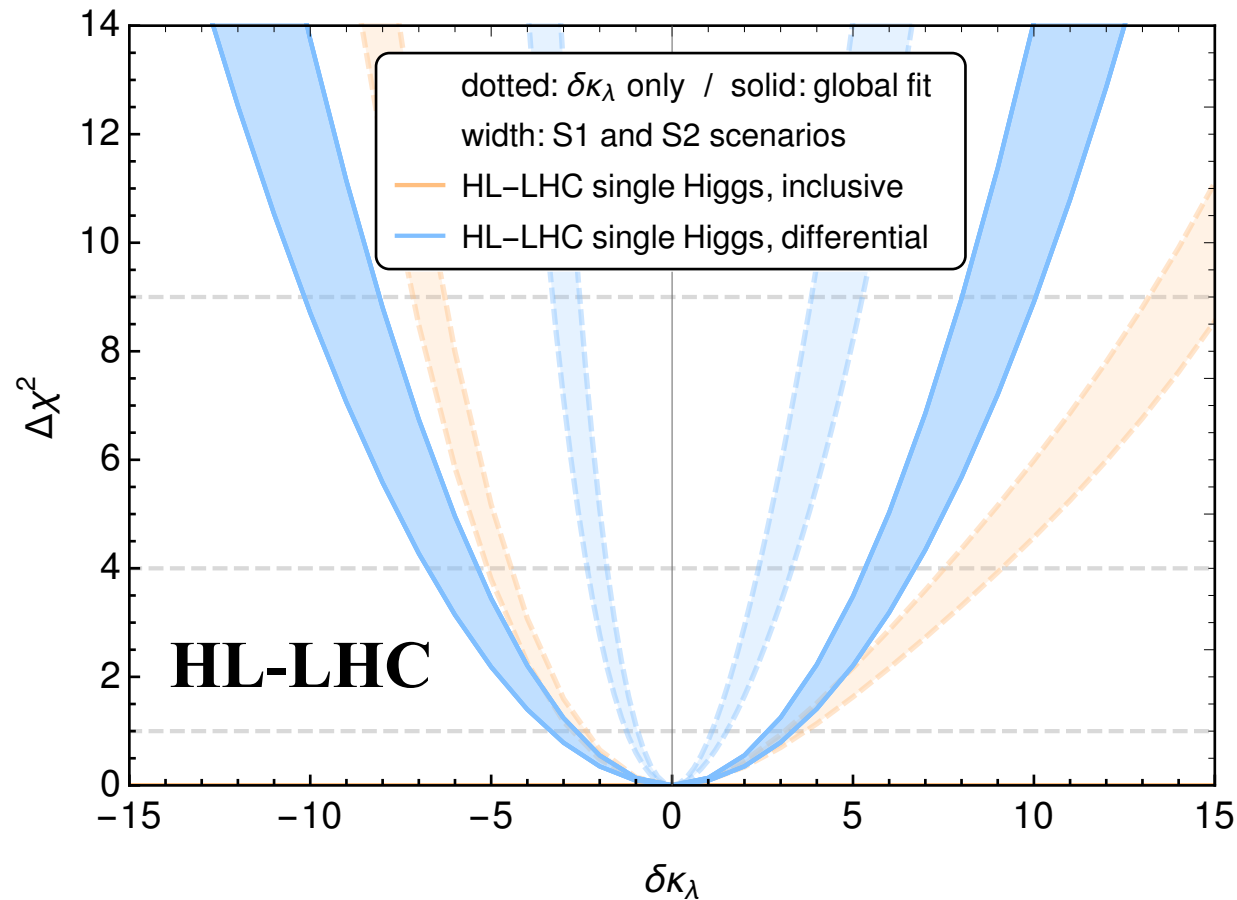
We moved from **1** to **10**: **no Physics in the middle?**

Effect of top chromo-dipole operators (**11**)?

**9** constraints can become **10** (Higgs plus jet, **Double Higgs** ..), or **many** (look at **distributions**)

# Combined fit with other EFT parameters

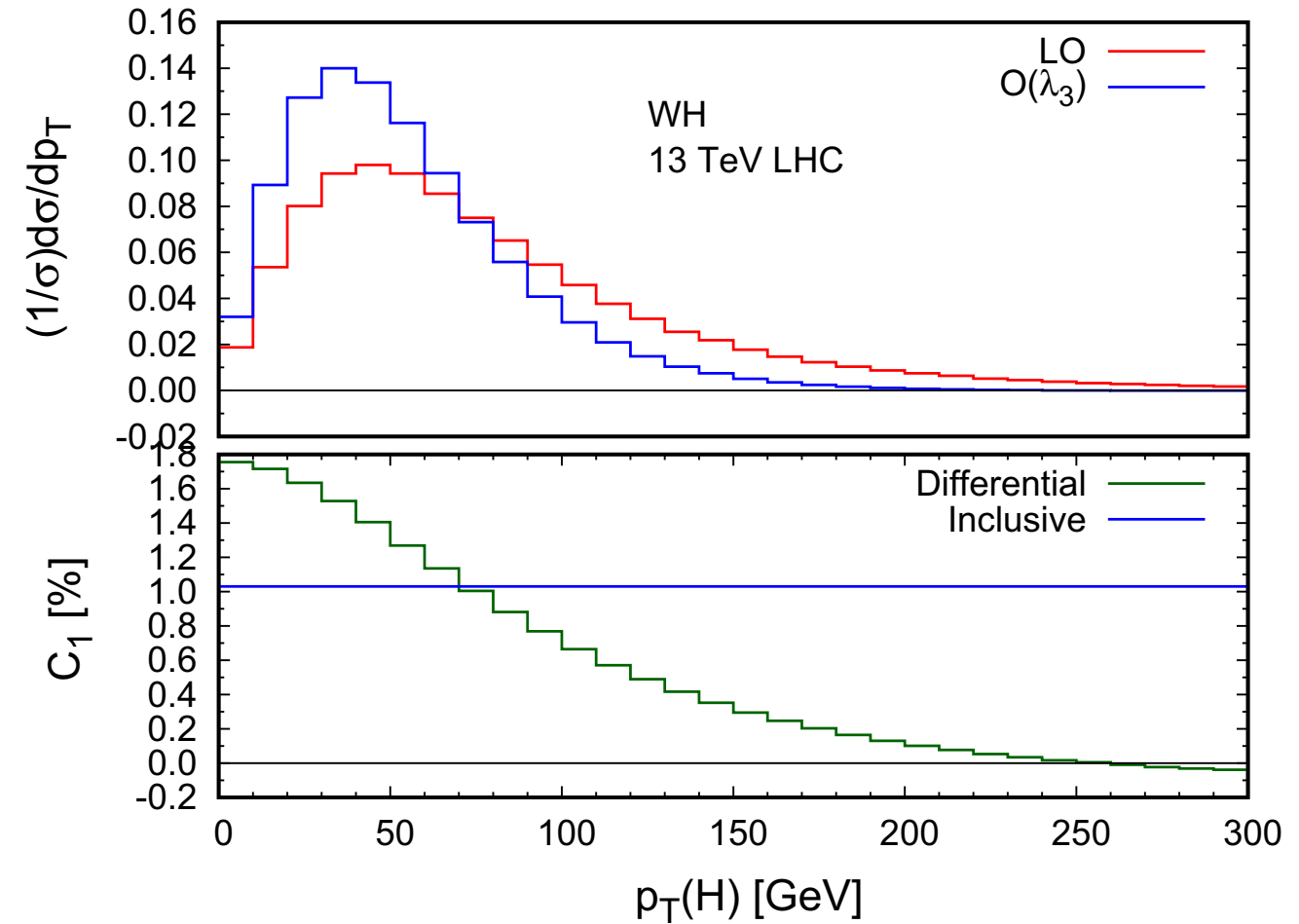
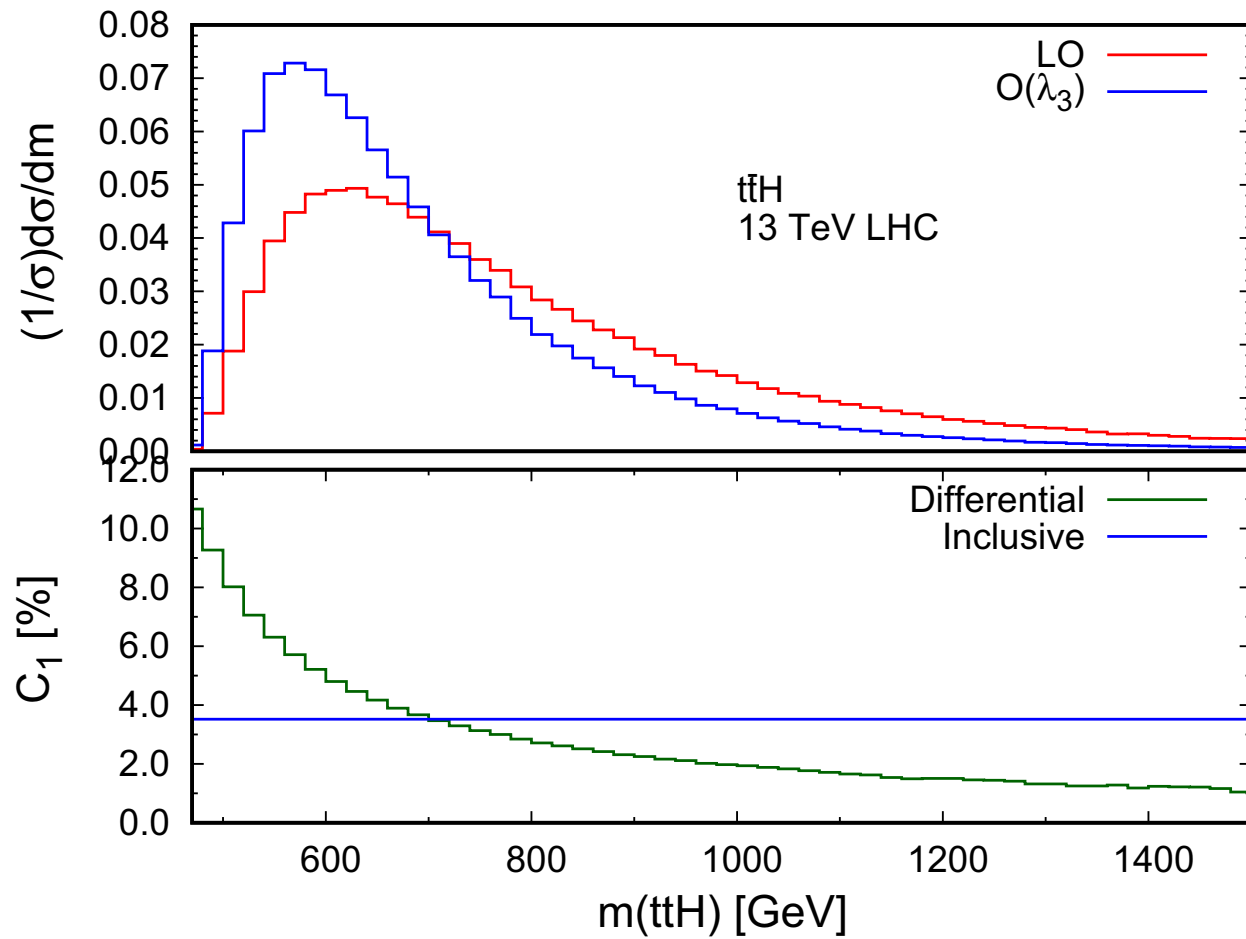
*Di Vita, Grojean, Panico, Riemann, Vantalon '17 (updated results from HL-HE-LHC report)*



Even with **10** independent parameters, **using differential distributions**, single-Higgs measurements at the HL-LHC can be sensitive to loop-induced anomalous trilinear contributions. Results further improve at HE-LHC (27 TeV).

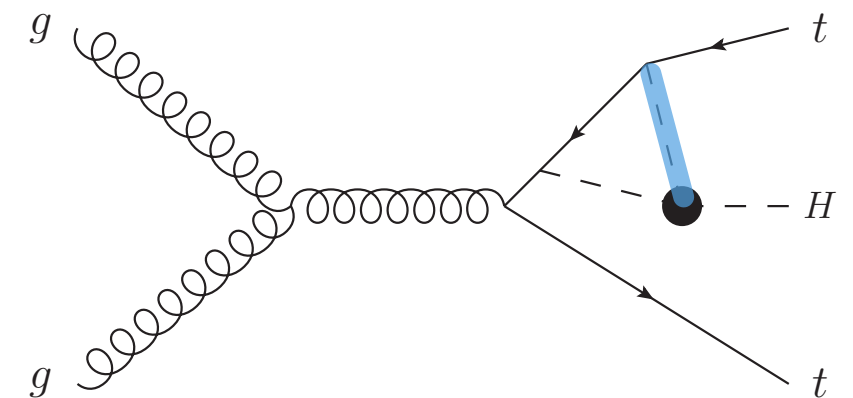
Single-Higgs differential measurements can improve the constraints from differential measurements in Double Higgs.

# C1: kinematic dependence

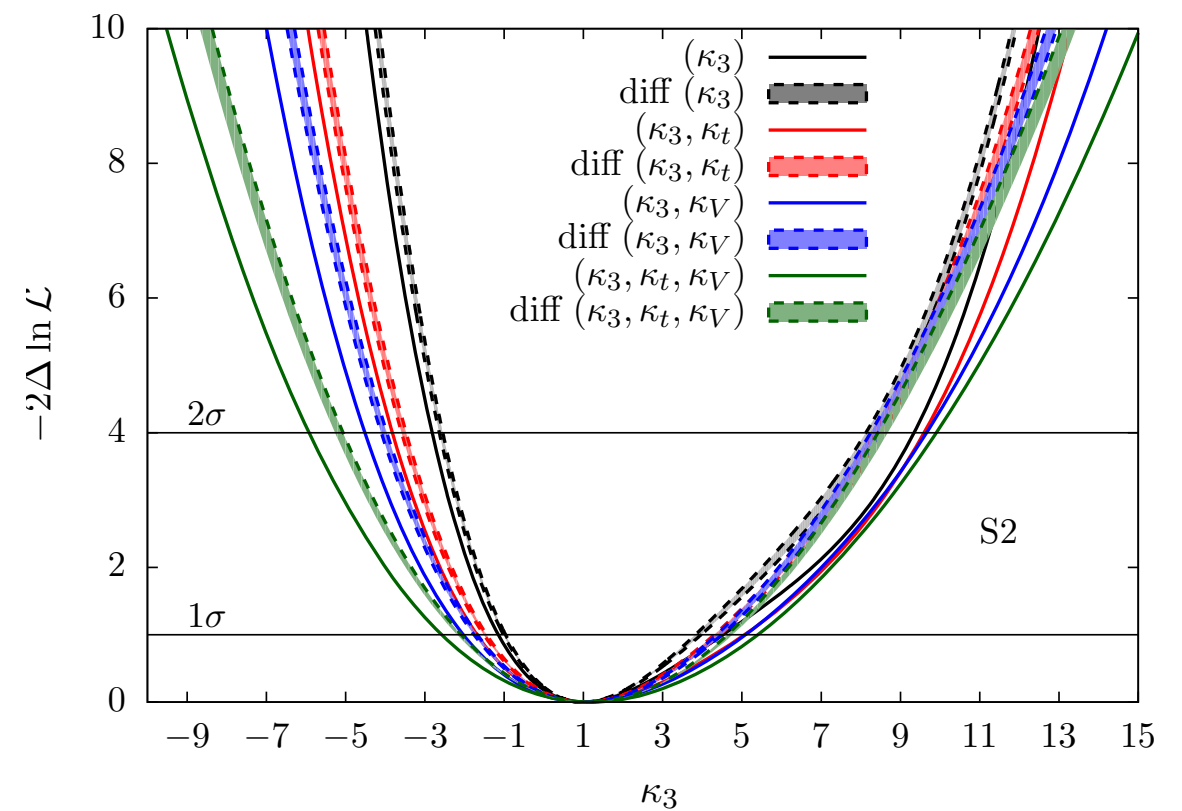
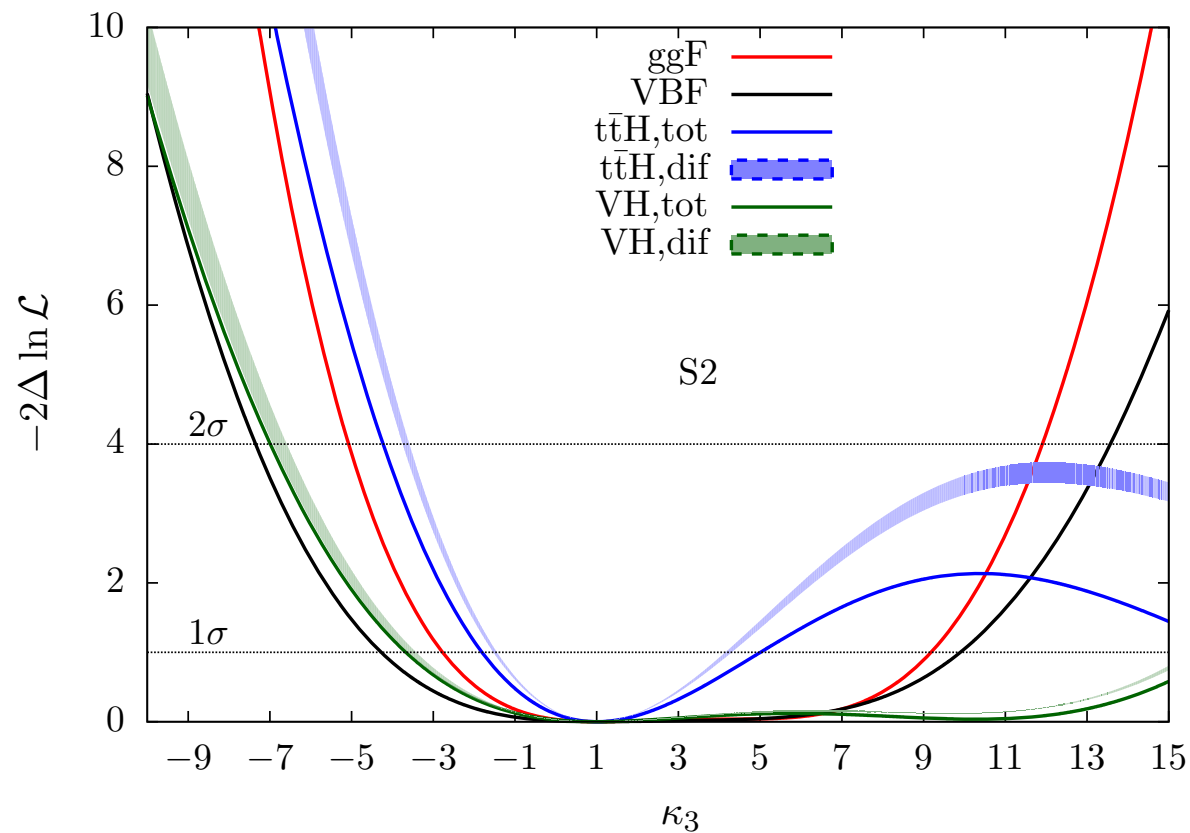


*Maltoni, DP, Shivaji, Zhao '17*

Contributions to  $ttH$  and  $HV$  processes can be seen as induced by a Yukawa potential, giving a Sommerfeld enhancement at the threshold.



# The relevance of differential information

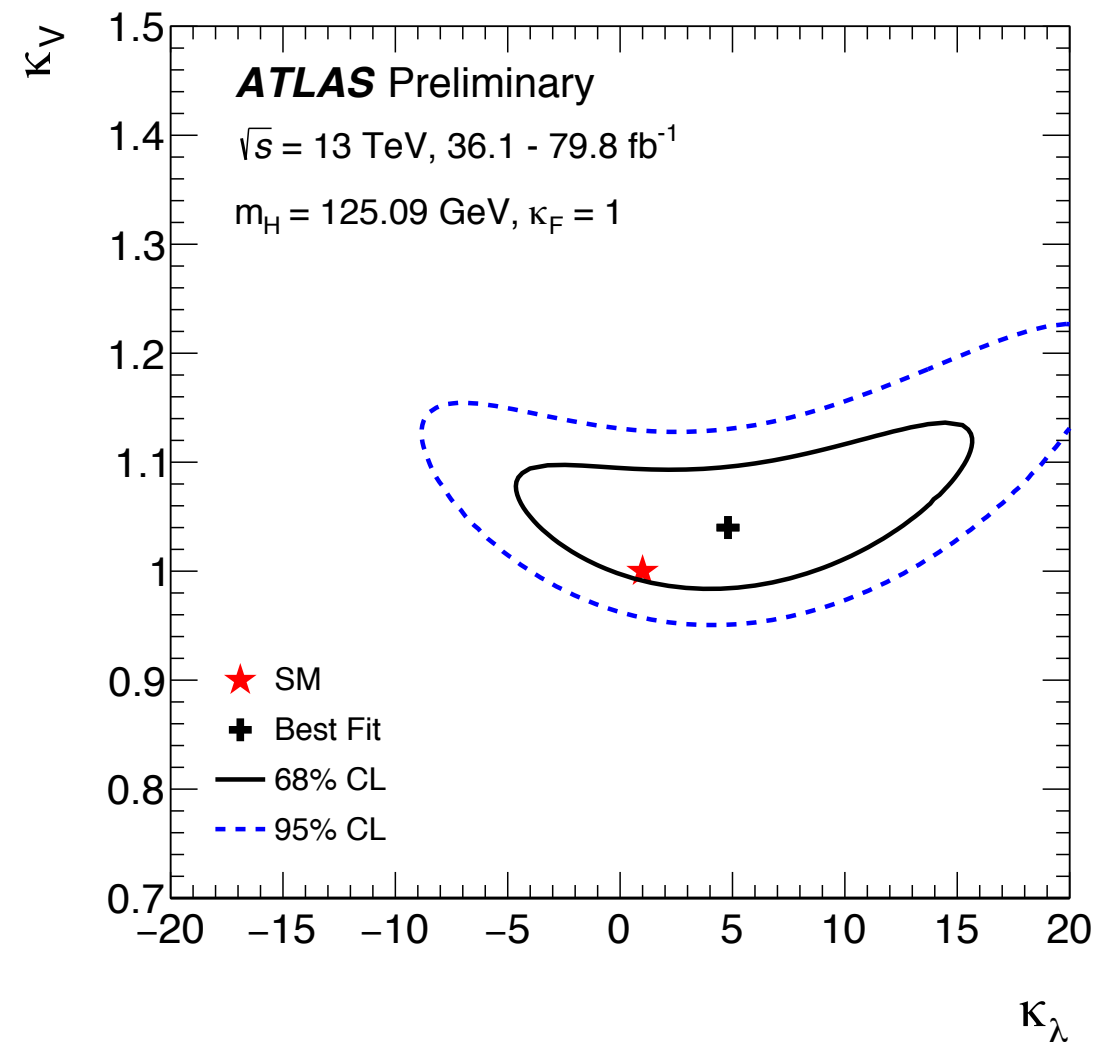
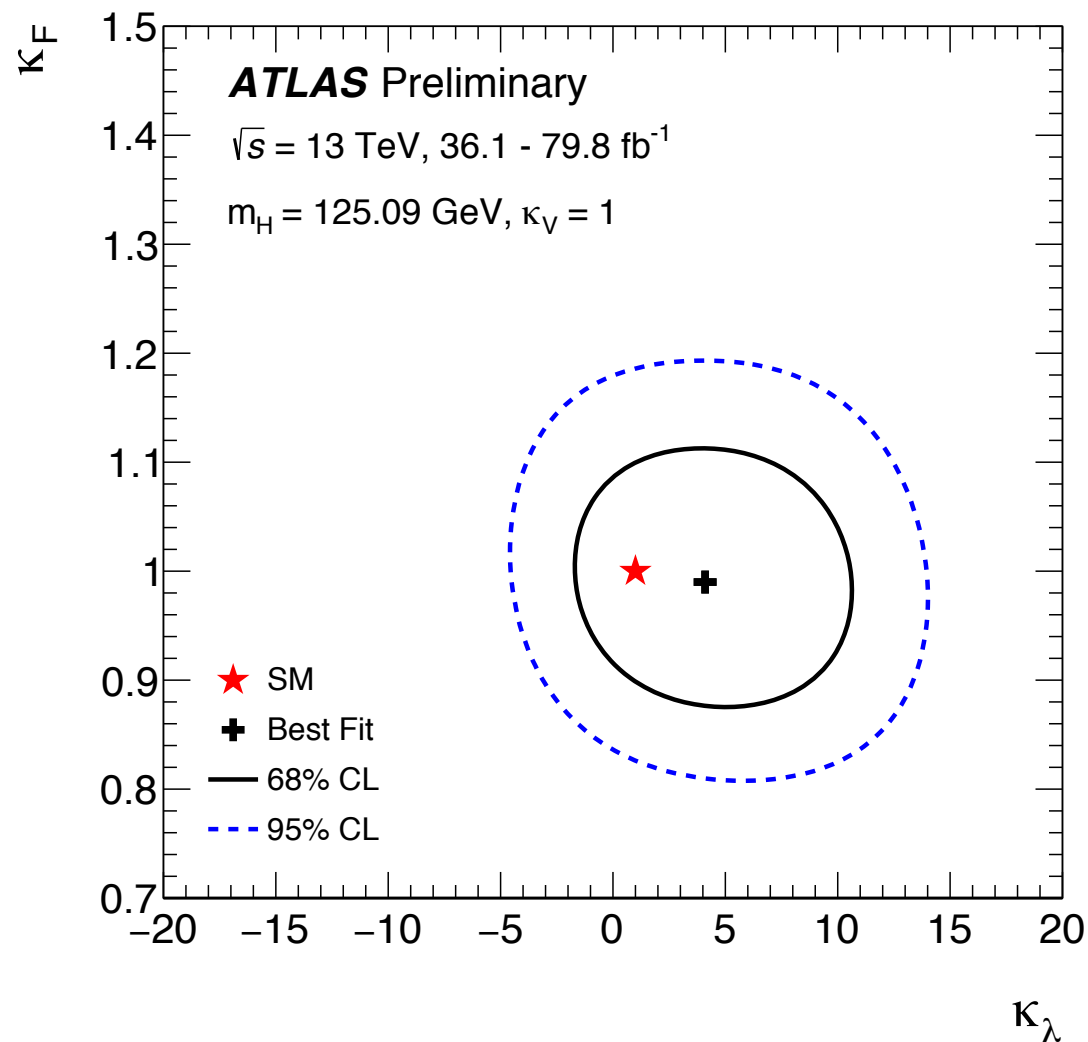


*Maltoni, DP, Shivaji, Zhao '17*

The interplay between additional possible couplings, experimental uncertainties and differential information leads to different results.

In general, differential information improves constraints, especially when additional couplings are considered.

# Experimental results (ATLAS) for present data (13 TeV)



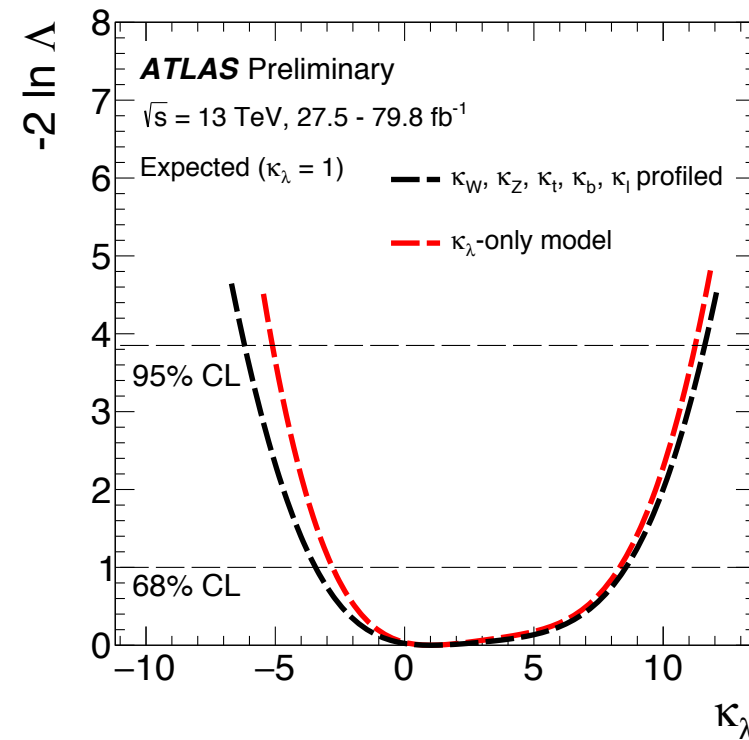
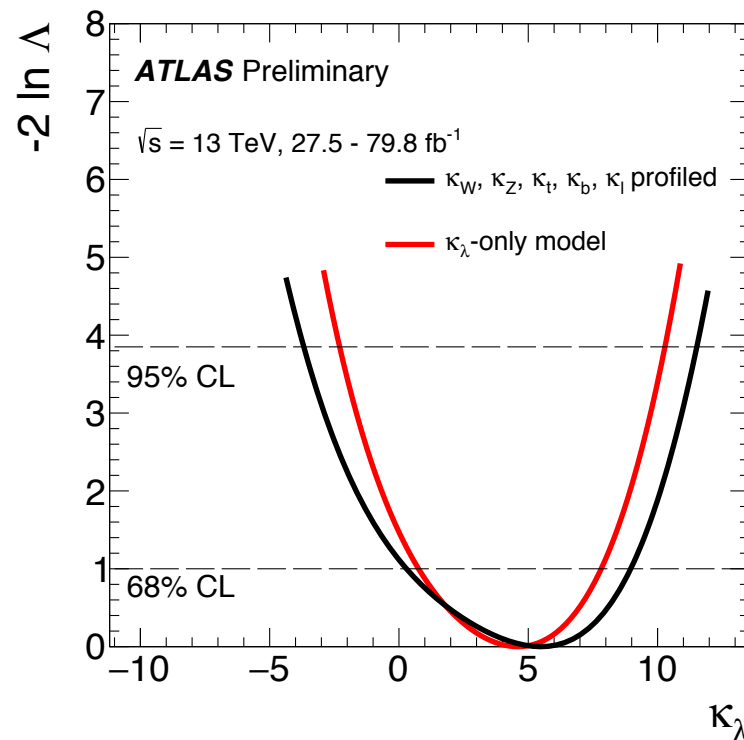
$\kappa_\lambda, \kappa_V$	STXS	1	$1.04^{+0.05}_{-0.04}$	$4.8^{+7.4}_{-6.7}$	$[-6.7, 18.4]$
$\kappa_\lambda, \kappa_F$	STXS	$0.99^{+0.08}_{-0.08}$	1	$4.1^{+4.3}_{-4.1}$	$[-3.2, 11.9]$

The presence of other anomalous couplings affects the bounds on the value of the Higgs self coupling.

# Limits in a generic Kappa-framework are already available!

## Generic model slide from Kunlin Ran talk (ATLAS)

- To give the most generic measurement, a likelihood fit is performed to constrain simultaneously  $\kappa_\lambda$ ,  $\kappa_W$ ,  $\kappa_Z$ ,  $\kappa_t$ ,  $\kappa_b$  and  $\kappa_l$

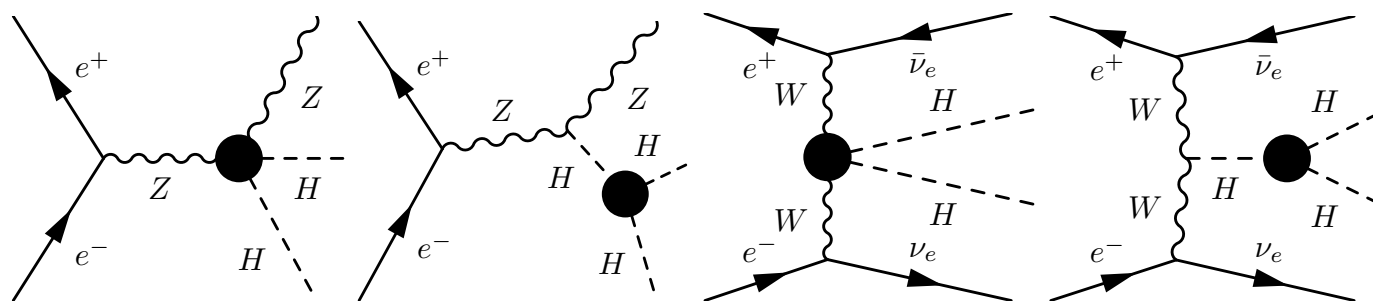


[ATLAS-CONF-2019-049]

Model	$\kappa_W^{+1\sigma}_{-1\sigma}$	$\kappa_Z^{+1\sigma}_{-1\sigma}$	$\kappa_t^{+1\sigma}_{-1\sigma}$	$\kappa_b^{+1\sigma}_{-1\sigma}$	$\kappa_l^{+1\sigma}_{-1\sigma}$	$\kappa_\lambda^{+1\sigma}_{-1\sigma}$	$\kappa_\lambda$ [95% CL]	
$\kappa_\lambda$ -only	1	1	1	1	1	$4.6^{+3.2}_{-3.8}$	[-2.3, 10.3]	obs.
						$1.0^{+7.3}_{-3.8}$	[-5.1, 11.2]	exp.
Generic	$1.03^{+0.08}_{-0.08}$	$1.10^{+0.09}_{-0.09}$	$1.00^{+0.12}_{-0.11}$	$1.03^{+0.20}_{-0.18}$	$1.06^{+0.16}_{-0.16}$	$5.5^{+3.5}_{-5.2}$	[-3.7, 11.5]	obs.
	$1.00^{+0.08}_{-0.08}$	$1.00^{+0.08}_{-0.08}$	$1.00^{+0.12}_{-0.12}$	$1.00^{+0.21}_{-0.19}$	$1.00^{+0.16}_{-0.15}$	$1.0^{+7.6}_{-4.5}$	[-6.2, 11.6]	exp.

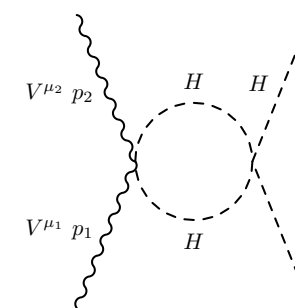
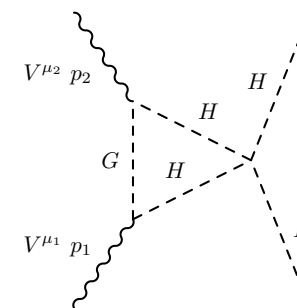
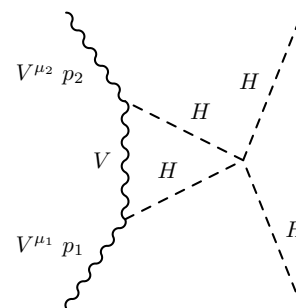
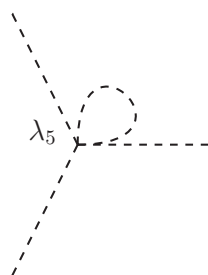
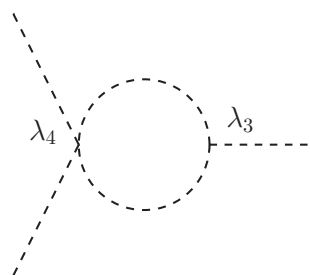
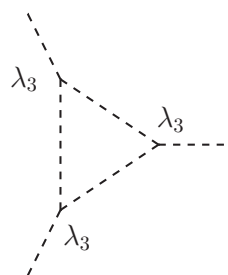
- Only the **single-Higgs and double-Higgs combination** could give enough sensitivity to exploit the generic model

# Quartic coupling at lepton colliders



from **triple** in **single** Higgs  
to **quartic** in **double** Higgs

*Maltoni, DP, Zhao '18*



EFT is mandatory, UV divergences have to be renormalised.

$$\kappa_3 \equiv \frac{\lambda_3}{\lambda_3^{\text{SM}}} = 1 + \frac{c_6 v^2}{\lambda \Lambda^2} \equiv 1 + \bar{c}_6,$$

$$\kappa_4 \equiv \frac{\lambda_4}{\lambda_4^{\text{SM}}} = 1 + \frac{6c_6 v^2}{\lambda \Lambda^2} + \frac{4c_8 v^4}{\lambda \Lambda^4} \equiv 1 + 6\bar{c}_6 + \bar{c}_8$$

$$\sigma_{\text{NLO}}^{\text{pheno}}(HH) = \sigma_{\text{LO}}(HH) + \Delta\sigma_{\bar{c}_6}(HH) + \Delta\sigma_{\bar{c}_8}(HH),$$

$$\Delta\sigma_{\bar{c}_6}(HH) = \bar{c}_6^3 \left[ \sigma_{30} + \sigma_{40} \bar{c}_6 \right],$$

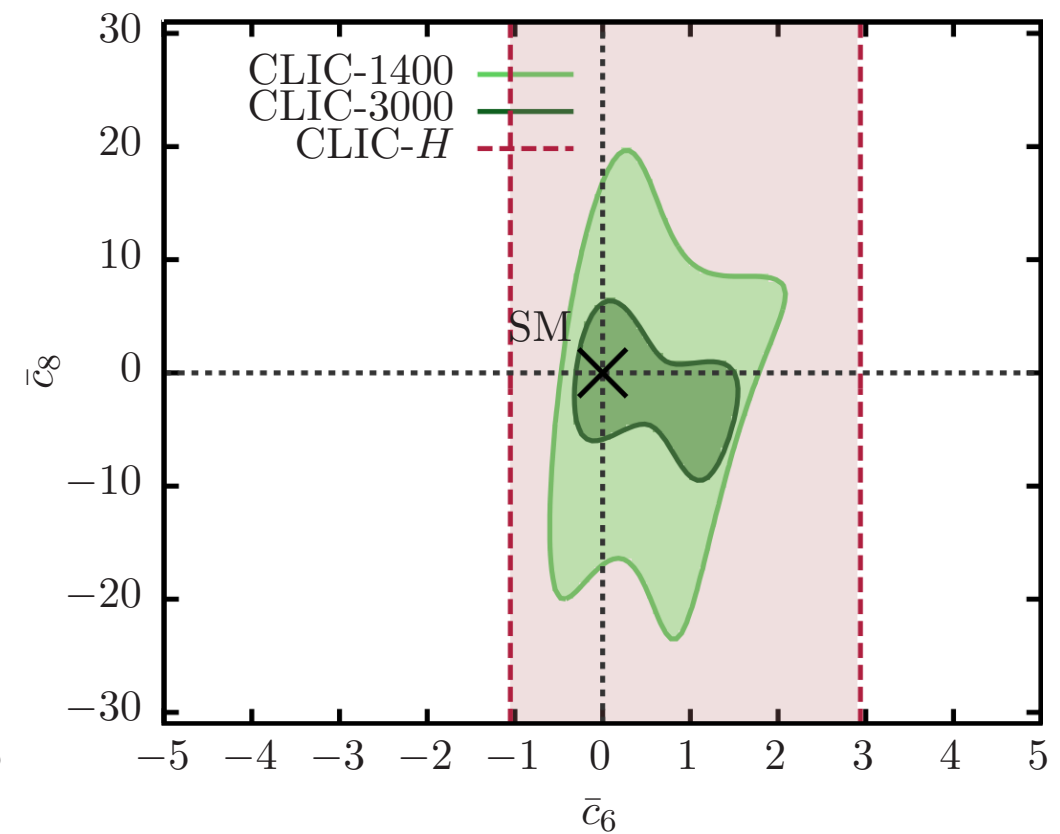
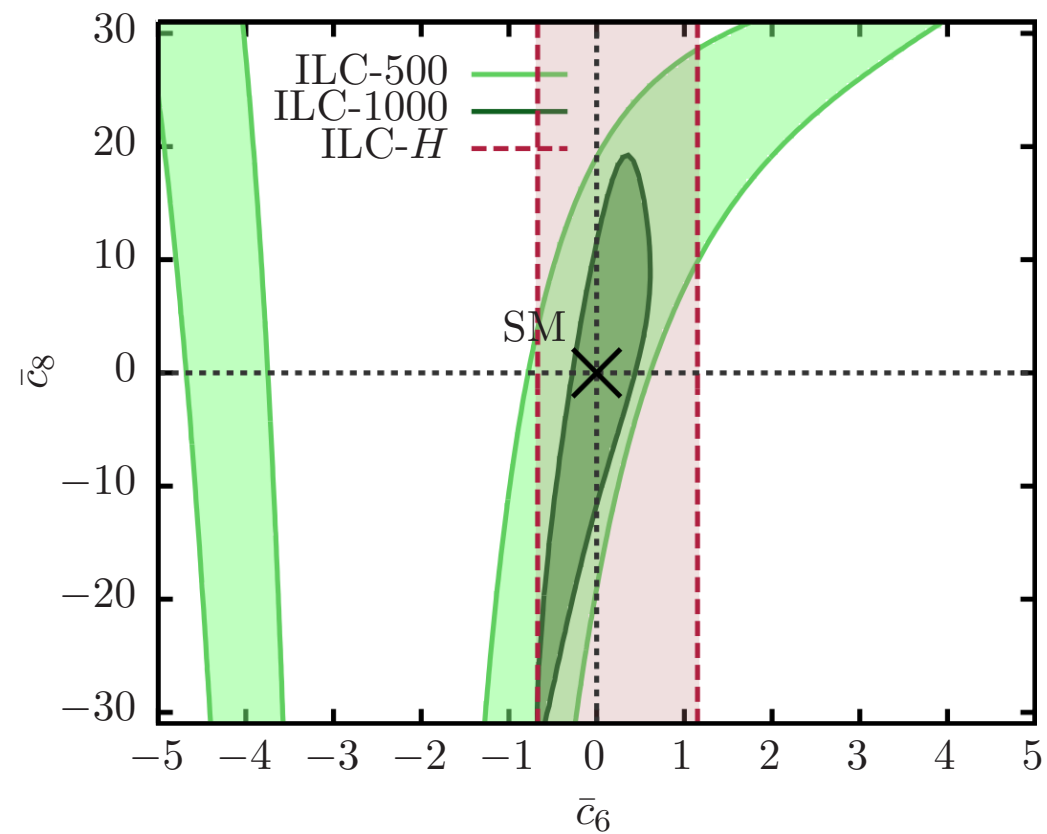
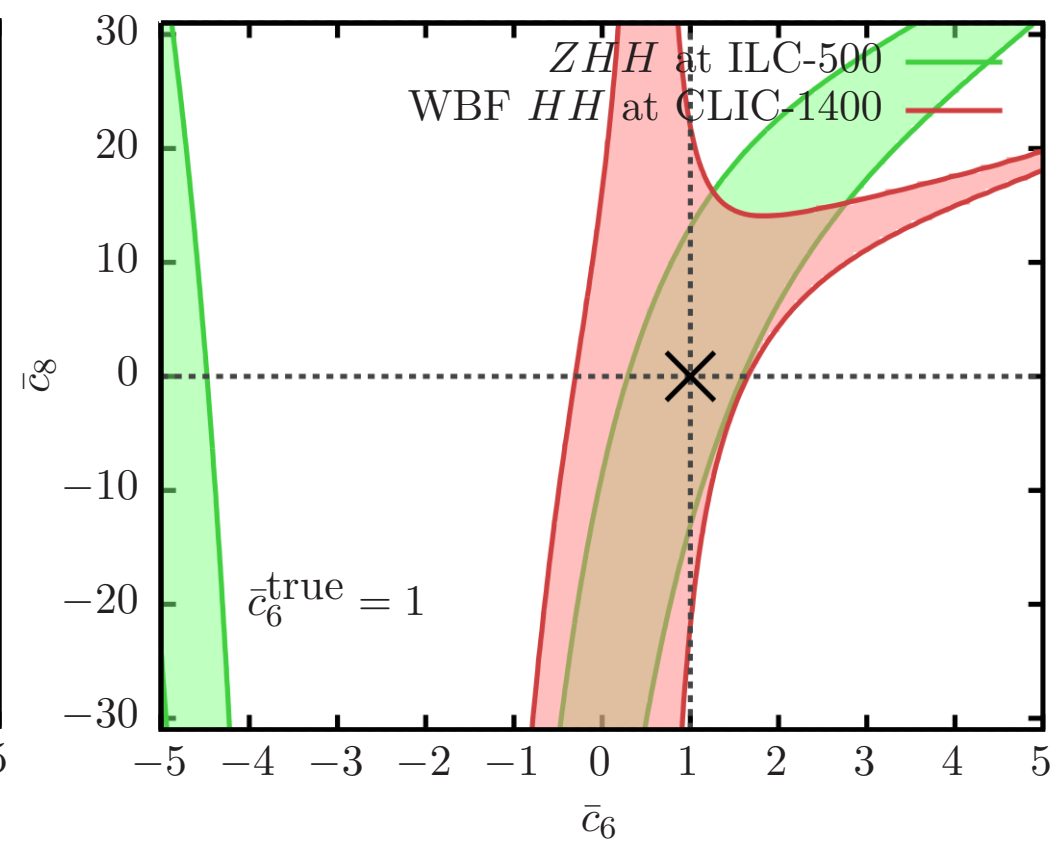
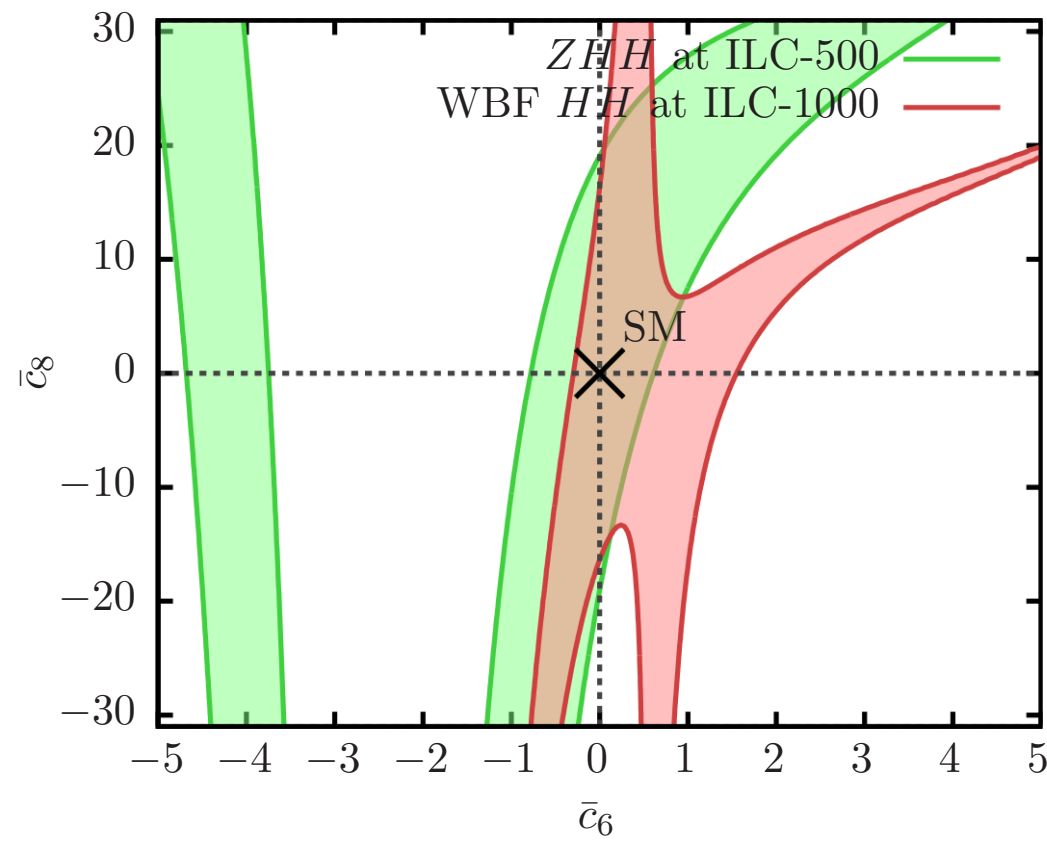
$$\Delta\sigma_{\bar{c}_8}(HH) = \bar{c}_8 \left[ \sigma_{01} + \sigma_{11} \bar{c}_6 + \sigma_{21} \bar{c}_6^2 \right].$$

Triple corrections to the triple  
Sensitivity quartic



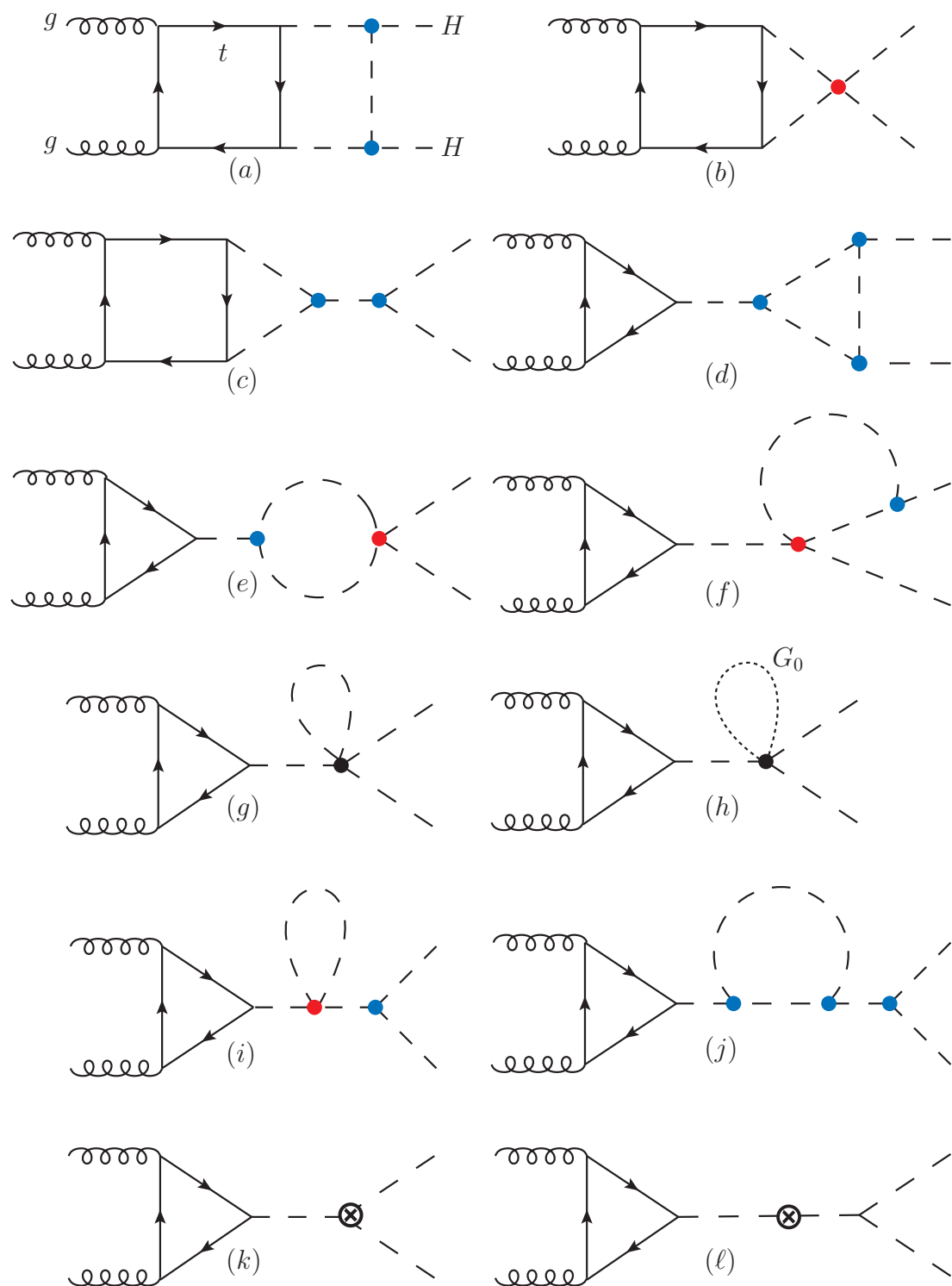
# Results

Maltoni, DP, Zhao '18





# Quartic coupling at hadron colliders: full result



$$\sigma_{\text{NLO}}^{\text{pheno}} = \sigma_{\text{LO}} + \Delta\sigma_{\bar{c}_6} + \Delta\sigma_{\bar{c}_8}$$

$$\Delta\sigma_{\bar{c}_6} = \bar{c}_6^2 \left[ \sigma_{30}\bar{c}_6 + \sigma_{40}\bar{c}_6^2 \right] + \tilde{\sigma}_{20}\bar{c}_6^2,$$

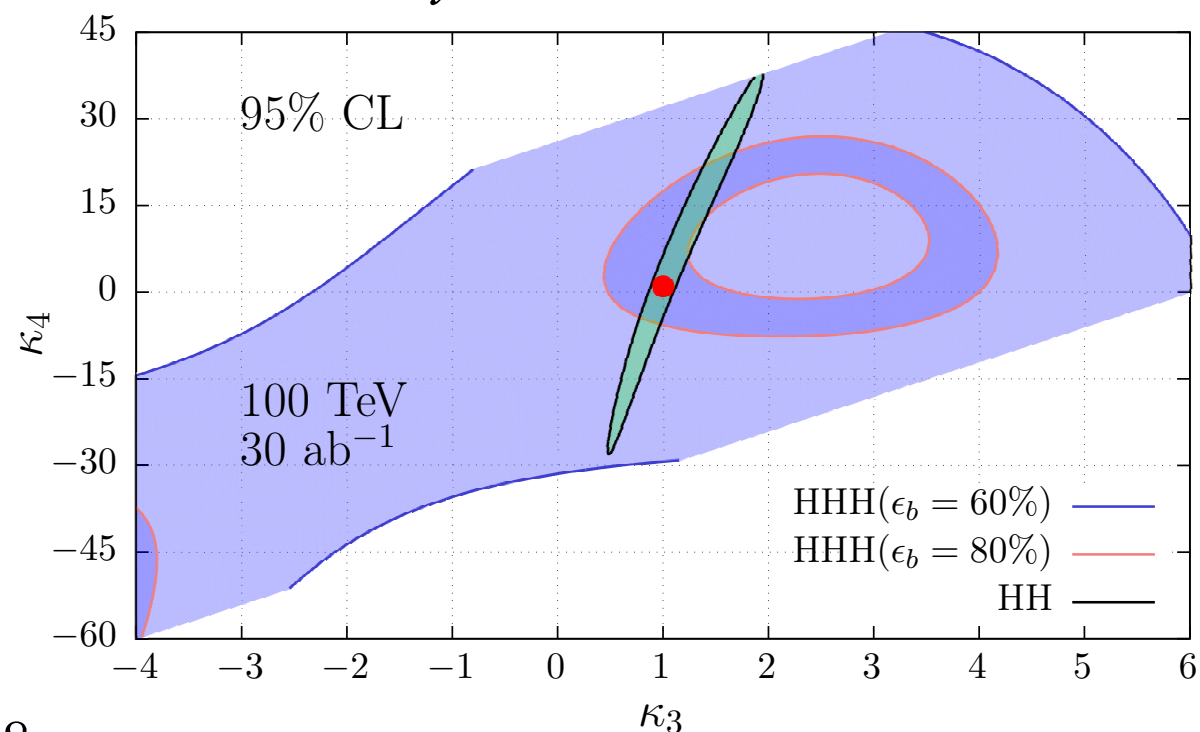
$$\Delta\sigma_{\bar{c}_8} = \bar{c}_8 \left[ \sigma_{01} + \sigma_{11}\bar{c}_6 + \sigma_{21}\bar{c}_6^2 \right]$$

All 2-loop contributions from  $c_8$  and at  $c_6^3$  and  $c_6^4$  order are taken into account and renormalised.

The  $m(\text{HH})$  distribution is exploited in the analysis.

Only  $b\bar{b}\gamma\gamma$  signature is considered.

Similar study in: *Bizon, Haisch, Rottoli '18*



# Conclusion

For a correct interpretation of current and future measurements and the possible identification of **BSM** effects, **precise predictions** and therefore **radiative corrections** are **paramount**.

**NLO EW** corrections cannot be neglected and they can be much larger than order  $\sim 1\%$  effects, especially in the **tail of the distributions**. (**Sudakov logs**)

Formally **subleading** orders may be in reality **large**. (**Top Physics**)

**EW corrections**, involving additional interactions, can be exploited as proxy for **New Physics** effects via **loop** corrections. (**Higgs self couplings**)

For the **first time**, the calculation of **NLO EW** and **Complete NLO** corrections can be performed in a **fully automated** way, via the **Madgraph5 \_aMC@NLO** framework. <https://launchpad.net/mg5amcnlo>

EXTRA SLIDES

# $t\bar{t}W^+$ : Complete-NLO with resummation at NNLL

Combined scales						
Order	$\sigma$ [fb]			$A_C$ [%]		
LO <sub>QCD</sub>	233.297(8)	+64.88(+27.8%)	+6.16(+2.6%)	0		
		-47.26(-20.3%)	-6.16(-2.6%)			
NLO <sub>QCD</sub>	365.66(3)	+57.95(+15.85%)	+8.35(+2.3%)	2.68(1)	+0.66(+24.6%)	+0.08(+2.9%)
		-49.27(-13.5%)	-8.35(-2.3%)		-0.47(-17.4%)	-0.08(-2.9%)
NLO	387.24(4)	+62.05(+16.0%)	+8.25(+2.1%)	2.85(1)	+0.60(+21.1%)	+0.09(+3.2%)
		-52.39(-13.5%)	-8.25(-2.1%)		-0.42(-14.7%)	-0.09(-3.2%)
nNLO <sub>QCD</sub>	371.72(3)	+51.11(+13.8%)	+8.50(+2.3%)	3.30(2)	+0.19(+5.8%)	+0.09(+2.6%)
		-35.88(-9.7%)	-8.50(-2.3%)		-0.08(-2.5%)	-0.09(-2.6%)
nNLO	393.29(4)	+55.21(+14.0%)	+8.40(+2.1%)	3.43(2)	+0.21(+6.2%)	+0.10(+2.9%)
		-39.00(-9.9%)	-8.40(-2.1%)		-0.11(-3.3%)	-0.10(-2.9%)
NLO <sub>QCD</sub> +NNLL	362.59(8)	+47.94(+13.2%)	+8.26(+2.3%)		-	
		-29.95(-8.3%)	-8.26(-2.3%)			
NLO+NNLL	384.17(9)	+51.52(+13.4%)	+8.16(+2.1%)		-	
		-32.36(-8.4%)	-8.16(-2.1%)			

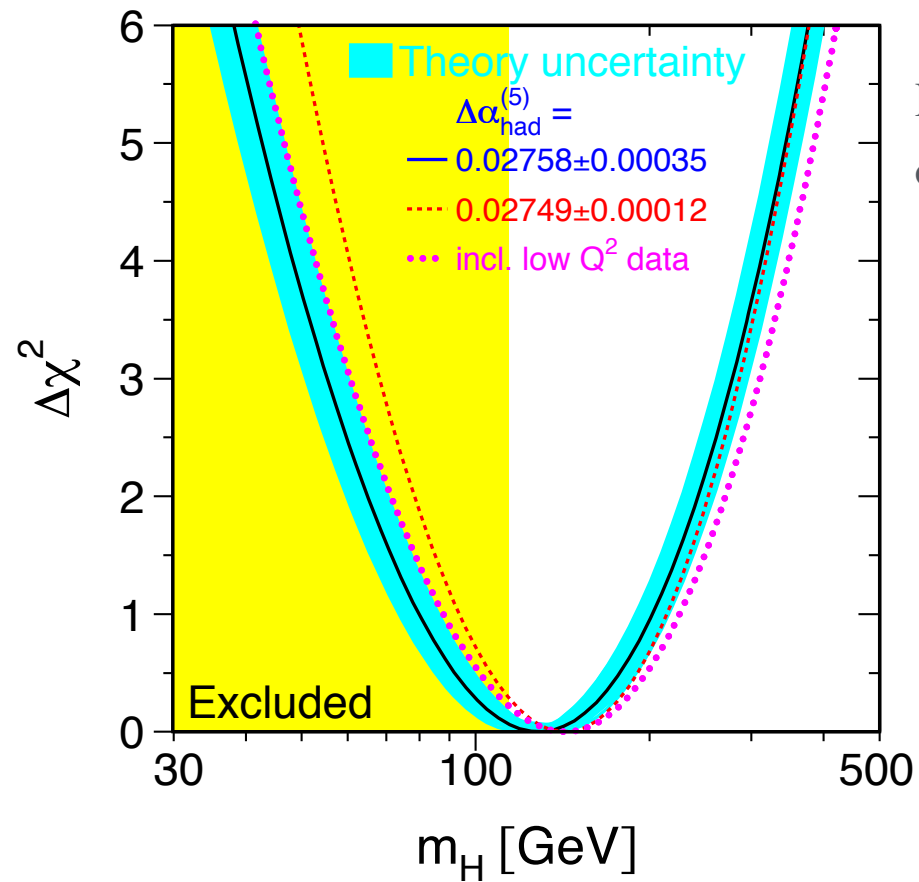
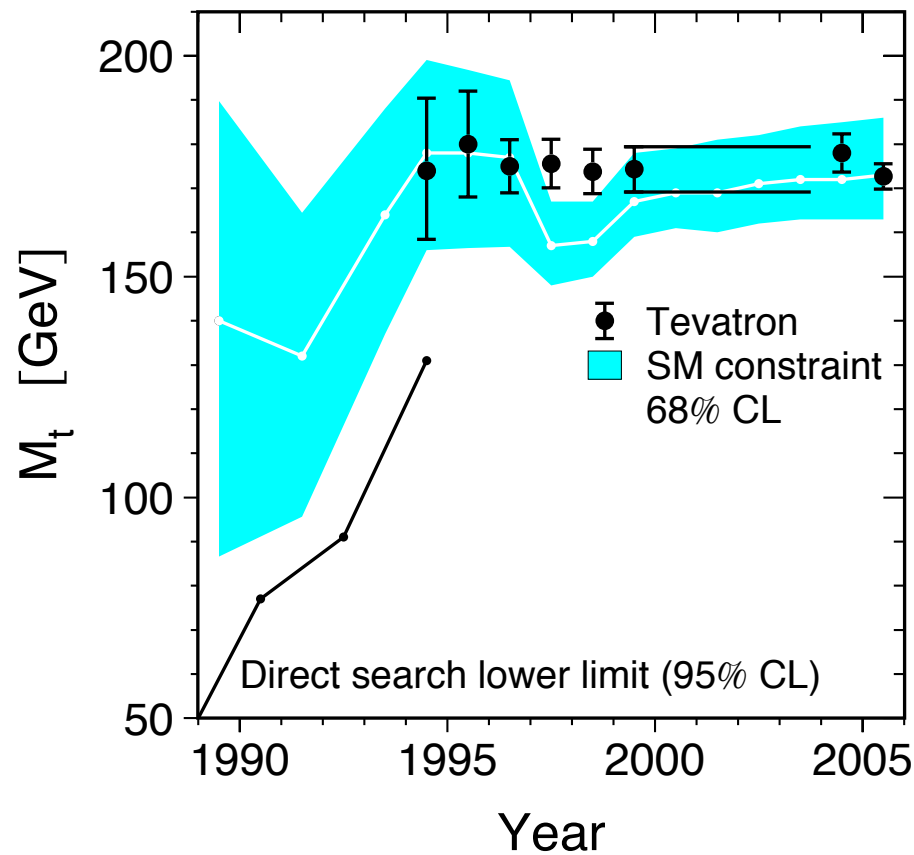
# $t\bar{t}H$ : Complete-NLO with resummation at NNLL

Combined scales			
Order	$\sigma$ [fb]		$A_C$ [%]
LO <sub>QCD</sub>	336.25(3)	+109.98(+32.7%) +7.42(+2.2%) -77.07(-22.9%) -7.42(-2.2%)	0
NLO <sub>QCD</sub>	467.96(5)	+45.57(+9.7%) +11.31(+2.4%) -53.98(-11.5%) -11.31(-2.4%)	0.88(1) +0.25(+28.9%) +0.04(+4.2%) -0.17(-19.2%) -0.04(-4.2%)
NLO	479.99(5)	+47.46(+9.9%) +11.45(+2.4%) -55.42(-11.5%) -11.45(-2.4%)	1.05(1) +0.27(+25.5%) +0.04(+4.0%) -0.18(-16.8%) -0.04(-4.0%)
nNLO <sub>QCD</sub>	490.27(6)	+18.56(+3.8%) +11.93(+2.4%) -9.50(-1.9%) -11.93(-2.4%)	0.87(4) +0.23(+26.4%) +0.04(+5.1%) -0.01(-1.5%) -0.04(-5.1%)
nNLO	502.31(6)	+20.32(+4.0%) +12.06(+2.4%) -10.95(-2.2%) -12.06(-2.4%)	1.03(4) +0.20(+19.5%) +0.05(+4.7%) -0.03(-2.6%) -0.05(-4.7%)
NLO <sub>QCD</sub> +NNLL	484.33(7)	+39.60(+8.2%) +11.78(+2.4%) -29.43(-6.1%) -11.78(-2.4%)	—
NLO+NNLL	496.36(7)	+38.64(+7.8%) +11.92(+2.4%) -29.35(-5.9%) -11.92(-2.4%)	—

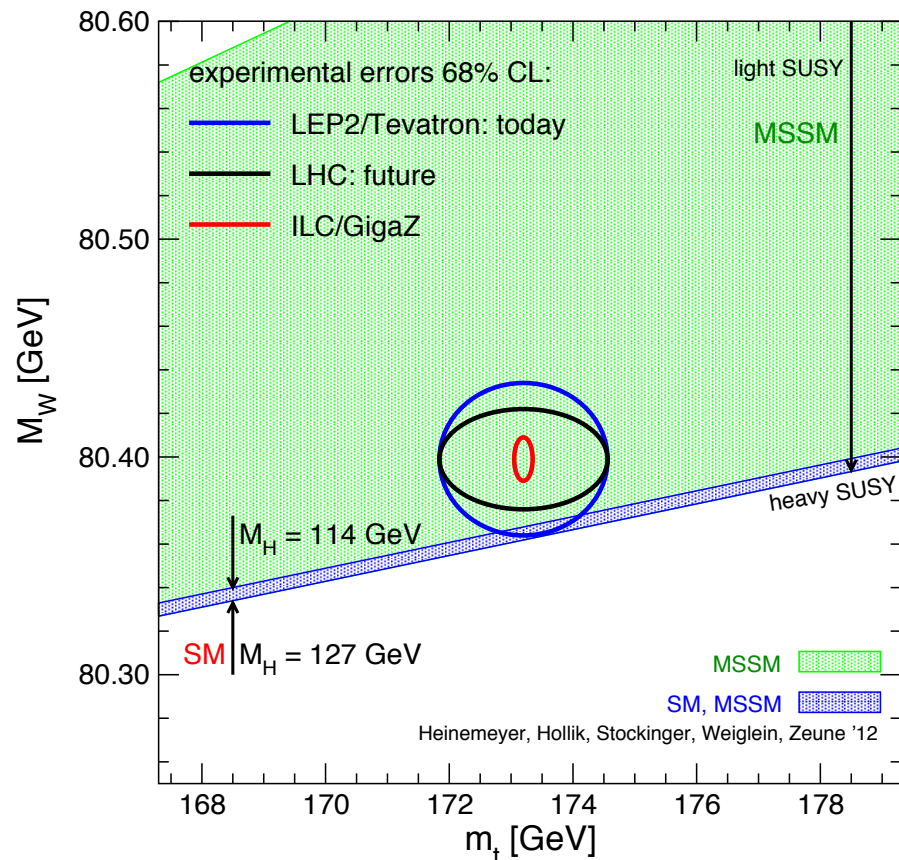
# $t\bar{t}Z$ : Complete-NLO with resummation at NNLL

Combined scales						
Order	$\sigma$ [fb]			$A_C$ [%]		
LO <sub>QCD</sub>	484.26(4)	+171.26(+35.4%) -117.32(-24.2%)	+11.05(+2.3%) -11.05(-2.3%)	0		
NLO <sub>QCD</sub>	751.2(1)	+111.1(+14.8%) -108.5(-14.4%)	+17.7(+2.4%) -17.7(-2.4%)	0.79(2)	+0.23(+29.0%) -0.15(-19.1%)	+0.05(+6.3%) -0.05(-6.3%)
NLO	759.5(1)	+110.1(+14.5%) -107.8(-14.2%)	+17.9(+2.4%) -17.9(-2.4%)	0.87(2)	+0.22(+25.0%) -0.14(-16.2%)	+0.05(+5.3%) -0.05(-5.3%)
nNLO <sub>QCD</sub>	817.1(1)	+42.3(+5.2%) -29.9(-3.7%)	+19.3(+2.4%) -19.3(-2.4%)	0.96(4)	+0.02(+1.7%) -0.07(-7.5%)	+0.06(+5.8%) -0.06(-5.8%)
nNLO	825.4(1)	+41.3(+5.0%) -29.3(-3.5%)	+19.5(+2.4%) -19.5(-2.4%)	1.03(4)	+0.01(+1.4%) -0.07(-6.3%)	+0.05(+5.2%) -0.05(-5.2%)
NLO <sub>QCD</sub> +NNLL	802.6(2)	+89.4(+11.1%) -78.1(-9.7%)	+19.0(+2.4%) -19.0(-2.4%)	—		
NLO+NNLL	810.9(2)	+89.2(+11.0%) -77.8(-9.6%)	+19.1(+2.4%) -19.1(-2.4%)	—		

# EWPO (past and future)



Precision Electroweak measurements on the Z resonance hep-ex/0509008

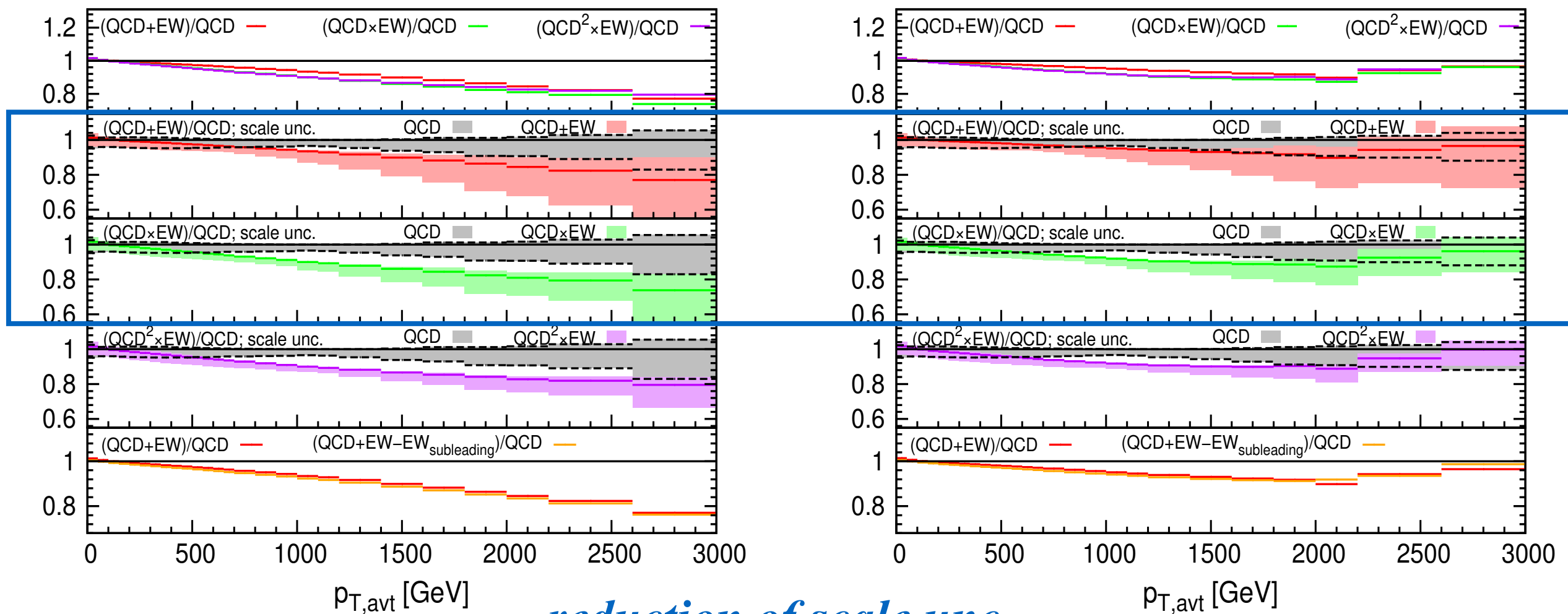


EWPO were crucial in order to constrain the H-boson and top-quark mass. Today EWPO can be used to check the internal consistency of the SM. In models where they can be calculated, as in the MSSM, EWPO can be used to constrain the parameter space.

**ADDITIVE**  
**MULTIPLICATIVE**

$t\bar{t}$ , LHC13, LUXqed

$t\bar{t}$ , LHC13, NNPDF3.0



LUXQED

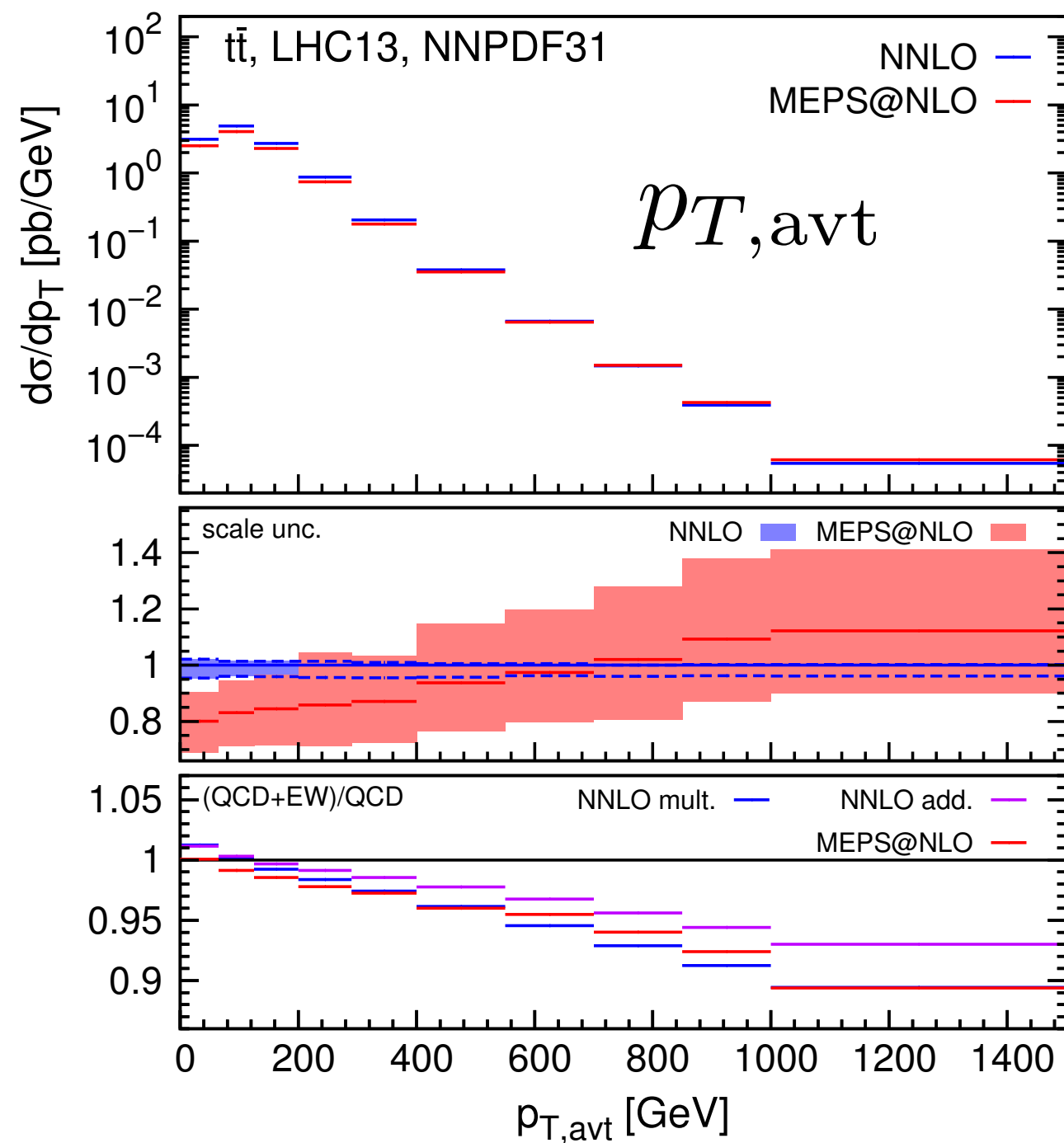
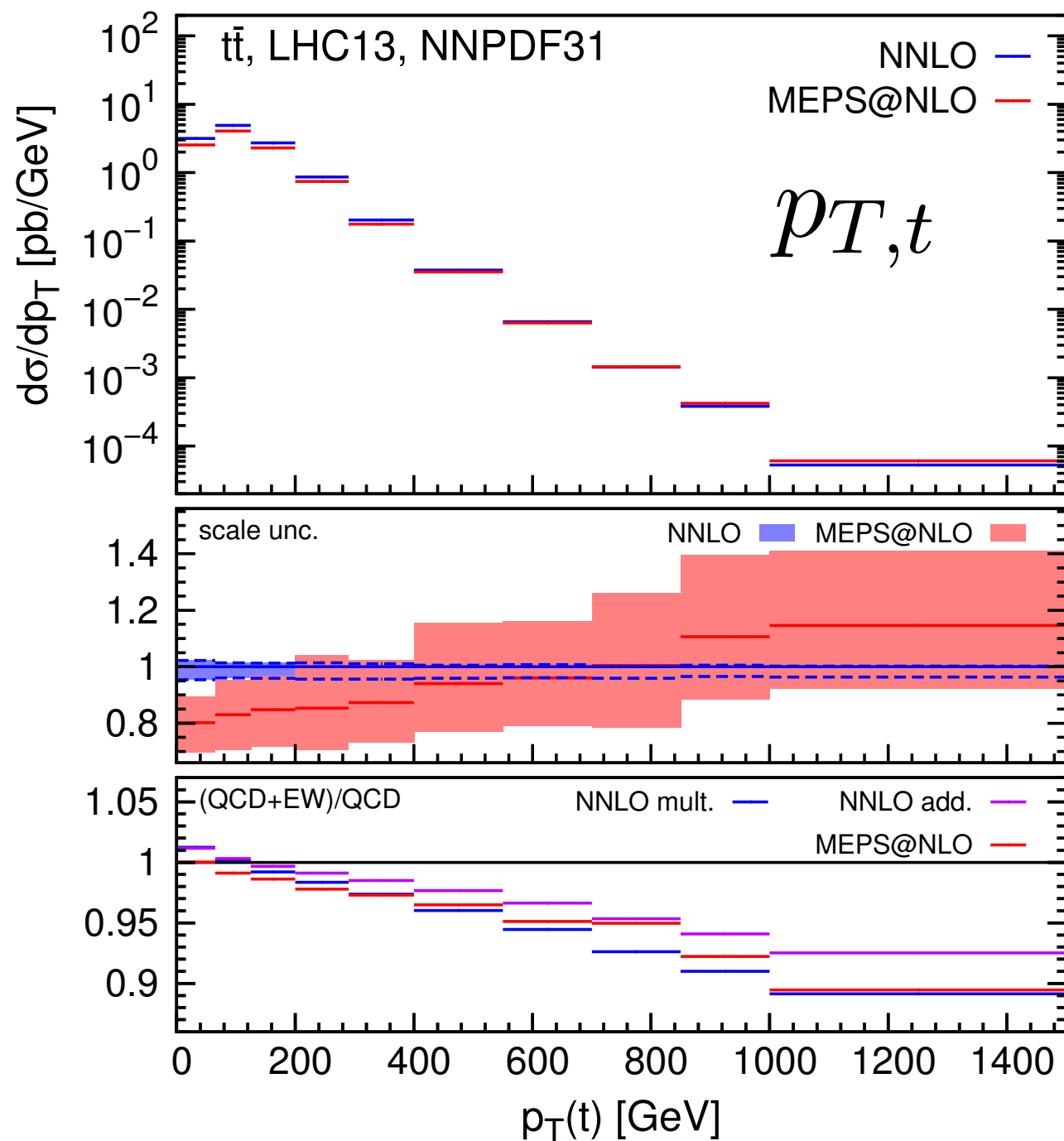
*reduction of scale unc.  
due to EW corrections,  
QCD and QCDxEW  
do not overlap  
(with LUXQED)*

NNPDF3.0QED



# NNLO vs MEPS@NLO, including Complete NLO

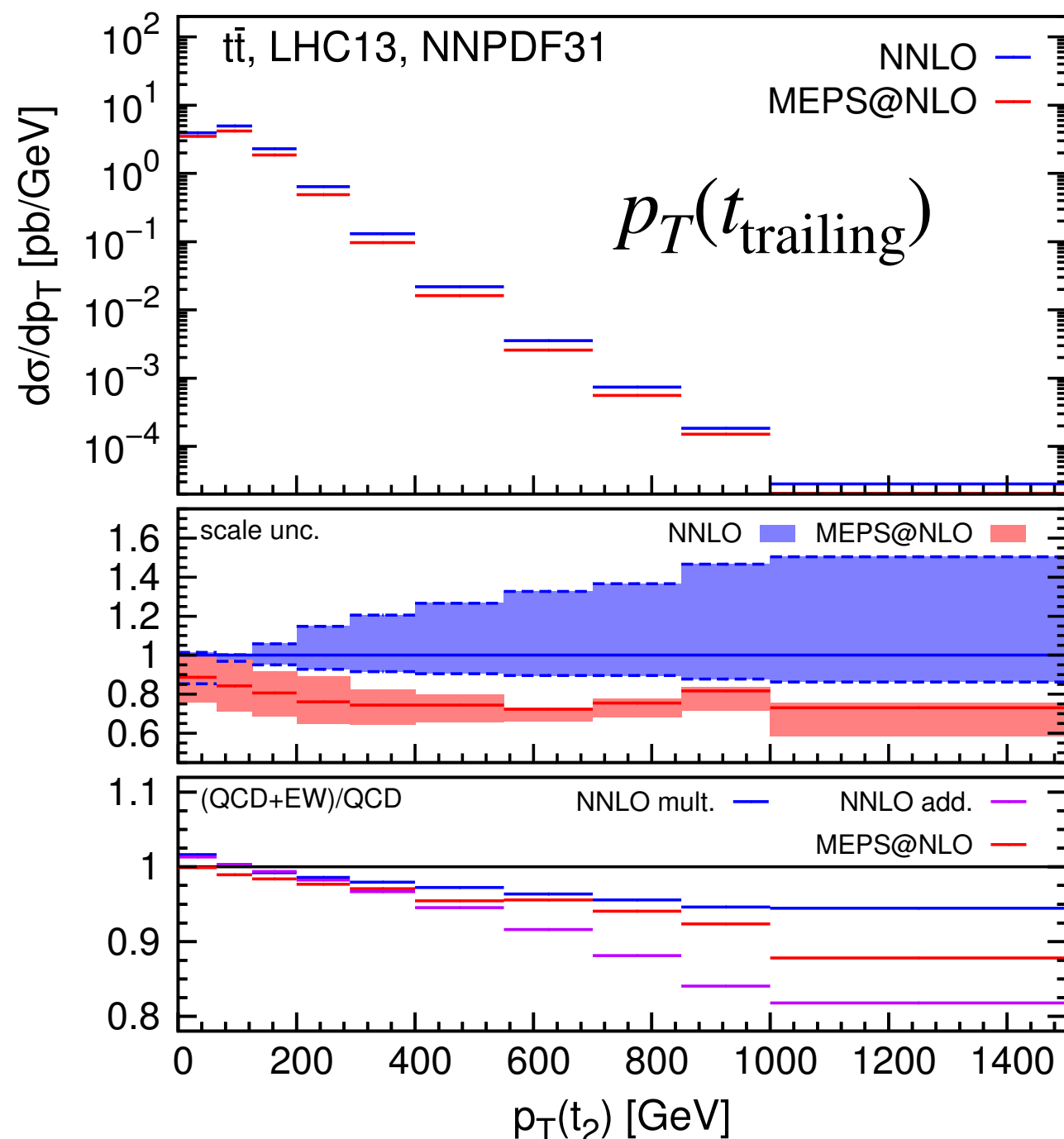
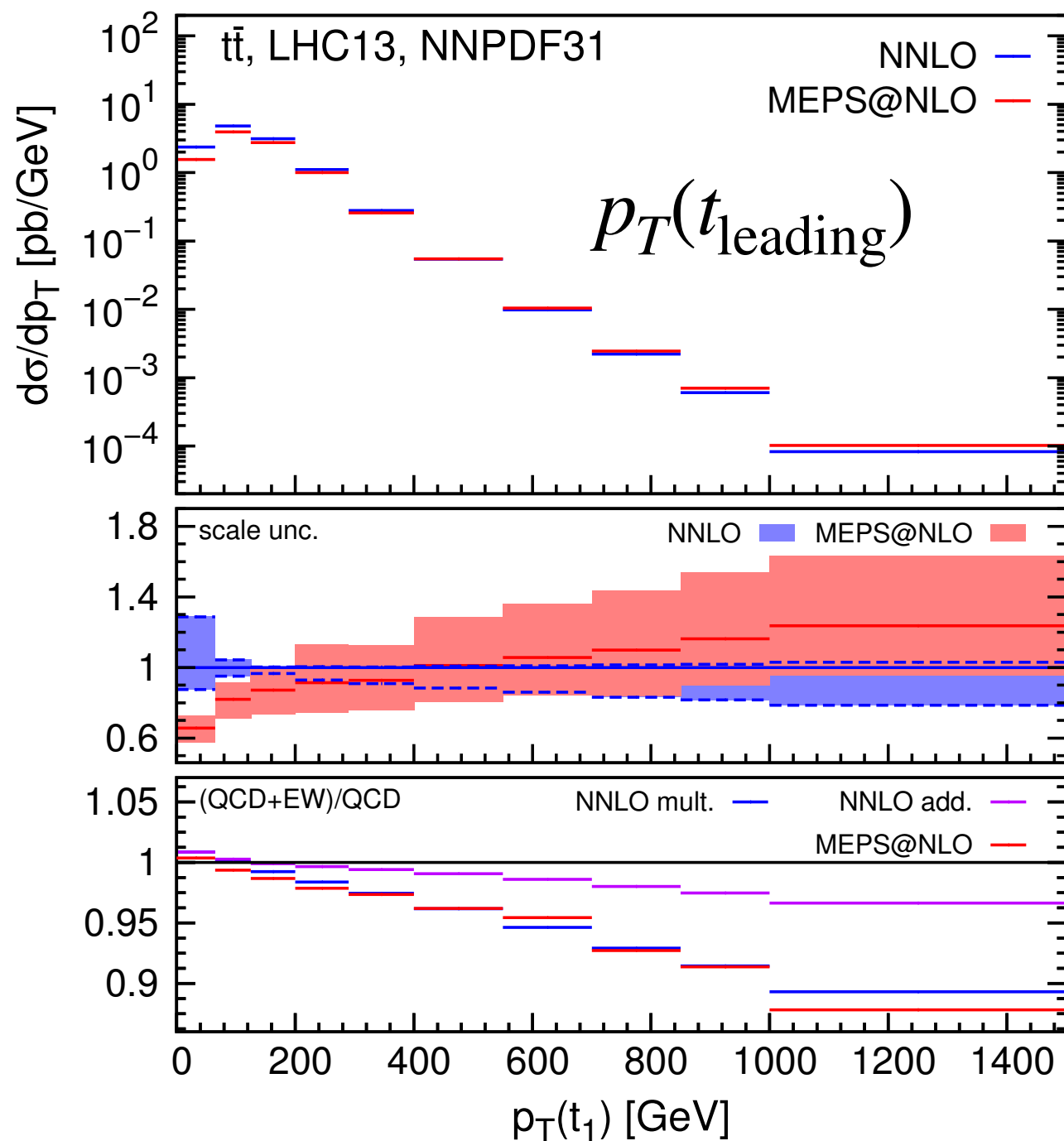
*Czakon, Gütschow, Lindert, Mitov, DP, Papanastasiou, Schönherr, Tsinikos, Zaro '19*



Predictions are **compatible**, with a **smaller scale unc.** for the **NNLO** case.  
**MEPS@NLO** further supports the **multiplicative** approach.

# NNLO vs MEPS@NLO, including Complete NLO

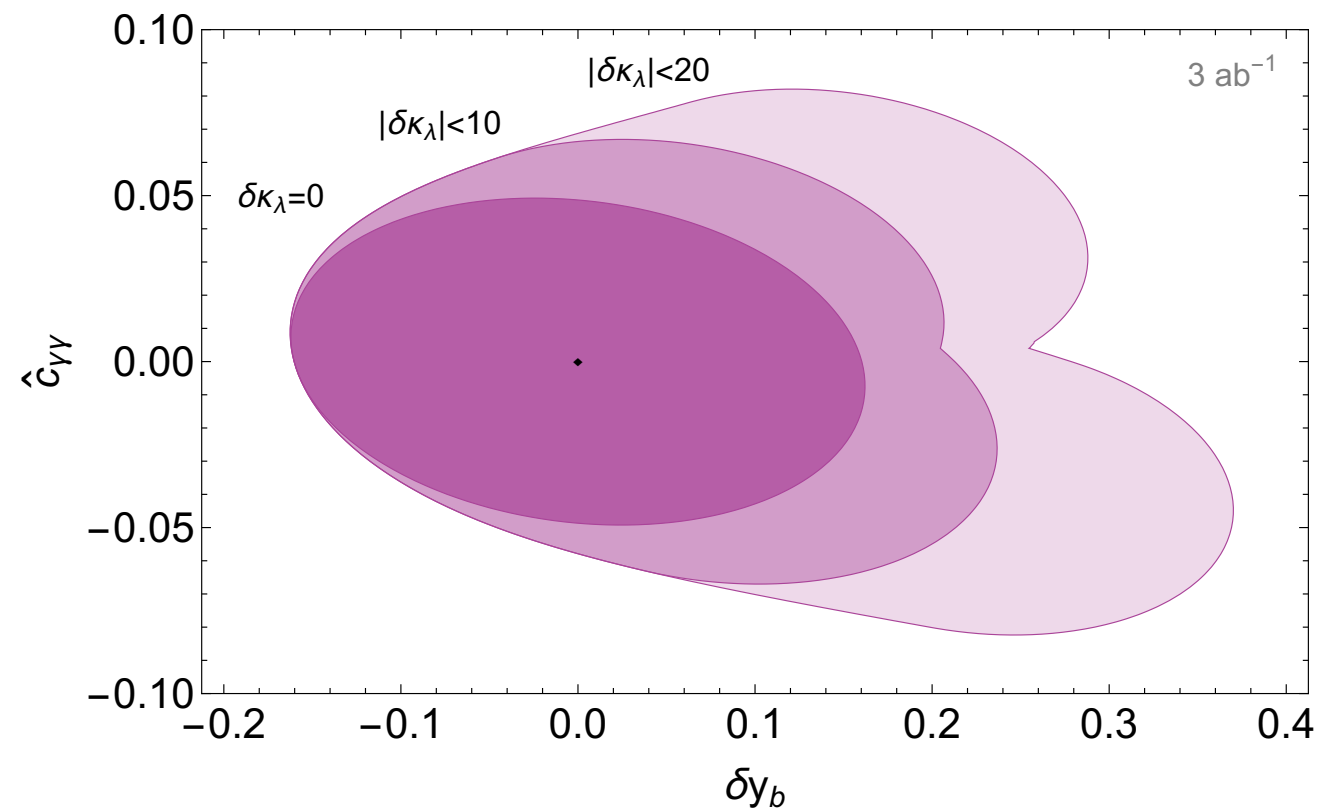
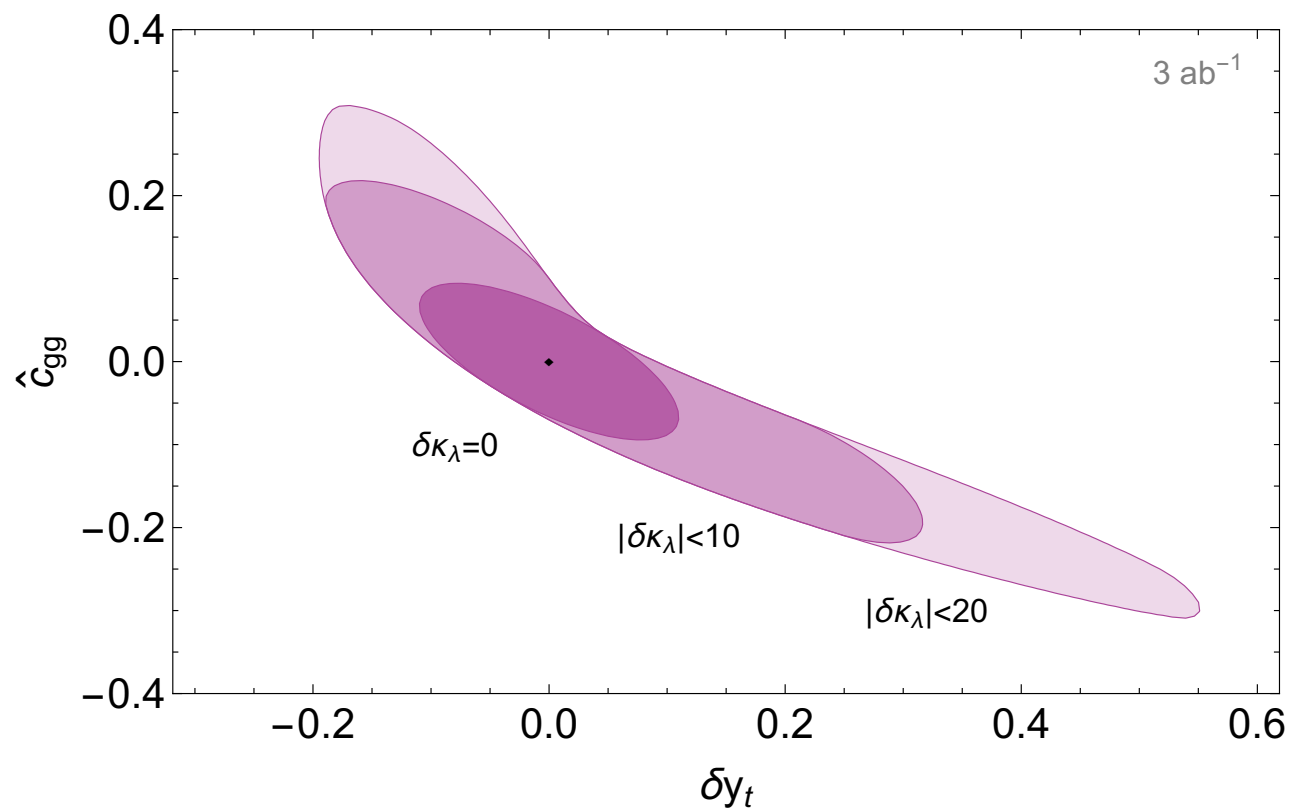
*Czakon, Gütschow, Lindert, Mitov, DP, Papanastasiou, Schönherr, Tsinikos, Zaro '19*



The **pt distribution** for the **softest top** and the region with **small values** for the **hardest top** are **pathological** at fixed order: **MEPS@NLO** cures this problem.

# Combined fit with other EFT parameters

Incl. single Higgs data



Moreover, trilinear loop-induced contributions affect the precision in the determination of the other parameters entering at the tree level.

*Di Vita, Grojean, Panico, Riemann, Vantalon '17*

# The Master Formula

The term  $\Sigma_{\text{NLO}}$  is the prediction for a generic observable  $\Sigma$  including the effects induced by an anomalous  $\lambda_3 \equiv \kappa_\lambda \lambda_3^{\text{SM}}$ . LO is meant dressed by QCD corrections.

$$\Sigma_{\text{NLO}} = Z_H \Sigma_{\text{LO}} (1 + \kappa_\lambda C_1)$$

$$\Sigma_{\text{NLO}}^{\text{SM}} = \Sigma_{\text{LO}} (1 + C_1 + \delta Z_H)$$



$$\delta \Sigma_{\lambda_3} \equiv \frac{\Sigma_{\text{NLO}} - \Sigma_{\text{NLO}}^{\text{SM}}}{\Sigma_{\text{LO}}} = (\kappa_\lambda - 1) \boxed{C_1} + (\kappa_\lambda^2 - 1) \boxed{C_2} + \mathcal{O}(\kappa_\lambda^3 \alpha^2)$$

universal

Process and kinetic dependent

$$C_2 = \frac{\delta Z_H}{(1 - \kappa_\lambda^2 \delta Z_H)}$$

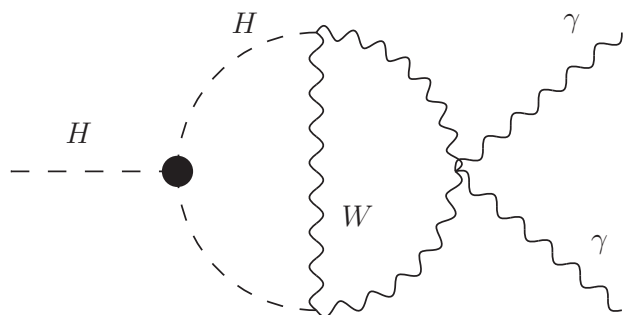
$$\mathcal{O}(\kappa_\lambda^3 \alpha^2) \simeq \kappa_\lambda^3 C_1 \delta Z_H \lesssim 10\% \quad \rightarrow \quad |\kappa_\lambda| \lesssim 20$$

# The Master Formula

The term  $\Sigma_{\text{NLO}}$  is the prediction for a generic observable  $\Sigma$  including the effects induced by an anomalous  $\lambda_3 \equiv \kappa_\lambda \lambda_3^{\text{SM}}$ . LO is meant dressed by QCD corrections.

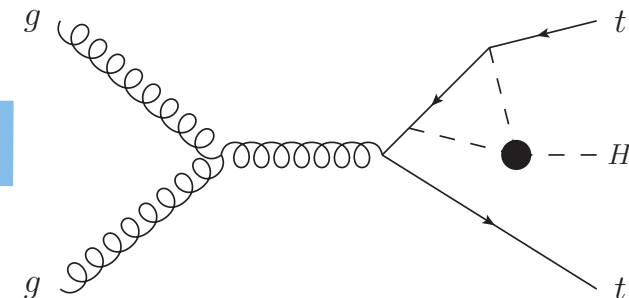
$$\Sigma_{\text{NLO}} = Z_H \Sigma_{\text{LO}} (1 + \kappa_\lambda \boxed{C_1})$$

$$C_1^\Gamma = \frac{\int d\Phi \, 2\Re \left( \mathcal{M}^{0*} \mathcal{M}_{\lambda_3^{\text{SM}}}^1 \right)}{\int d\Phi \, |\mathcal{M}^0|^2}$$



$$= \mathcal{M}_{\lambda_3^{\text{SM}}}^1 \sim \kappa_\lambda$$

$$C_1^\sigma = \frac{\sum_{i,j} \int dx_1 dx_2 f_i(x_1) f_j(x_2) \, 2\Re \left( \mathcal{M}_{ij}^{0*} \mathcal{M}_{\lambda_3^{\text{SM},ij}}^1 \right) d\Phi}{\sum_{i,j} \int dx_1 dx_2 f_i(x_1) f_j(x_2) \, |\mathcal{M}_{ij}^0|^2 d\Phi}$$



$$= \mathcal{M}_{\lambda_3^{\text{SM}}}^1 \sim \kappa_\lambda$$

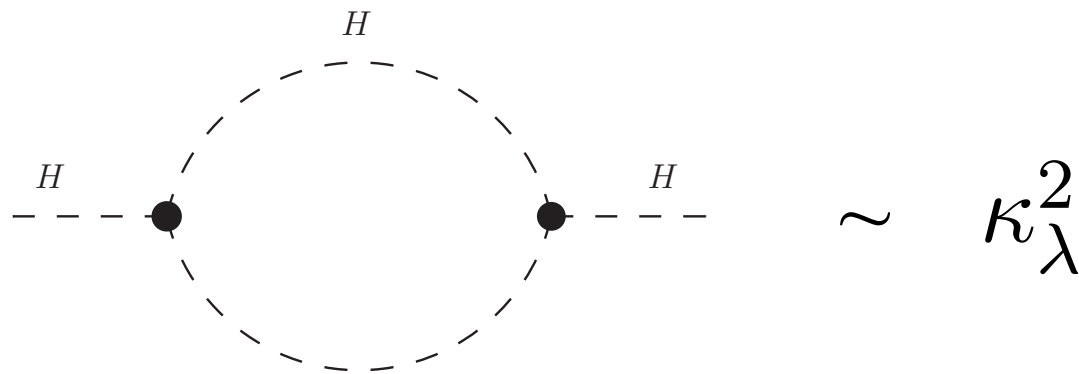
# The Master Formula

The term  $\Sigma_{\text{NLO}}$  is the prediction for a generic observable  $\Sigma$  including the effects induced by an anomalous  $\lambda_3 \equiv \kappa_\lambda \lambda_3^{\text{SM}}$ . LO is meant dressed by QCD corrections.

$$\Sigma_{\text{NLO}} = \boxed{Z_H} \Sigma_{\text{LO}} (1 + \kappa_\lambda C_1)$$

$$Z_H = \frac{1}{1 - \kappa_\lambda^2 \delta Z_H}$$

$$\delta Z_H = -\frac{9}{16} \frac{2(\lambda_3^{\text{SM}})^2}{m_H^2 \pi^2} \left( \frac{2\pi}{3\sqrt{3}} - 1 \right)$$



The wave-function normalization receives corrections that depend quadratically on  $\lambda_3$ .

For large  $\kappa_\lambda$ , the result cannot be linearized and must be resummed.

$$\kappa_\lambda^2 \delta Z_H \lesssim 1 \quad \rightarrow \quad |\kappa_\lambda| \lesssim 25$$

For a sensible resummation

# NLO EW and anomalous couplings

If we modify a SM coupling via  $c_i^{\text{SM}} \rightarrow c_i \equiv \kappa_i c_i^{\text{SM}}$ , do higher-order computations *remain in general finite* (UV cancellation)? **NO**

## Exceptions

The renormalization of  $c_i$   
does not involve EW corrections



Standard “kappa framework”  
(No EW corrections possible)

Double Higgs dependence on  $\kappa_\lambda$   
(No EW corrections possible)

$c_i$  is involved in the renormalization  
of other couplings, but it is not renormalized



Sensitivity of  $t\bar{t}$  production on  $K_t$   
(NLO EW effect)

*Kühn et al. '13; Beneke et al. '15*

Sensitivity of single Higgs  
production on  $\kappa_\lambda$   
(NLO EW effect)

# NLO EW and anomalous couplings

If we modify a SM coupling via  $c_i^{\text{SM}} \rightarrow c_i \equiv \kappa_i c_i^{\text{SM}}$ , do higher-order computations *remain in general finite* (UV cancellation)? **NO**

## Exceptions

The renormalization of  $c_i$  does not involve EW corrections

$c_i$  is involved in the renormalization of other couplings, but it is not renormalized



In all cases,  $\Lambda_{\text{NP}}$  has to be assumed to be not too large in order to have higher-order corrections under control.

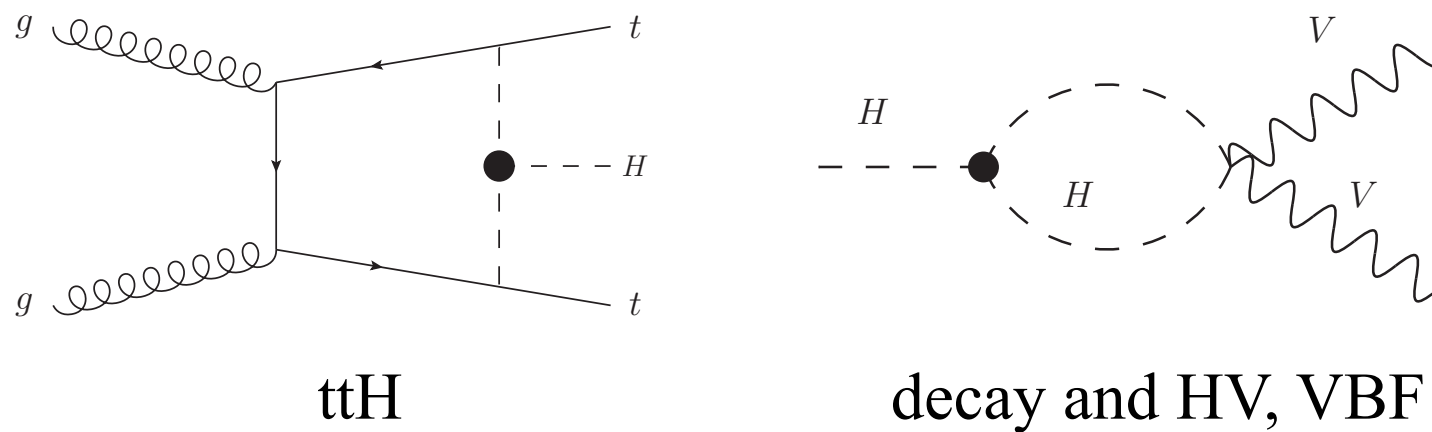
In our case, linear EFT (c6) and anomalous coupling ( $\kappa_\lambda$ ) are equivalent at NLO EW.

(NLO EW effect)



# Calculation of $C_1$ coefficients

## 1 Loop Case : *FeynArts, FormCalc, FeynCalc*

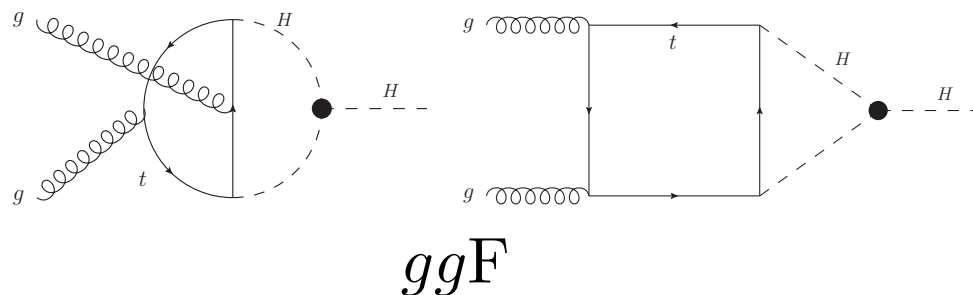


Cannot be expressed via

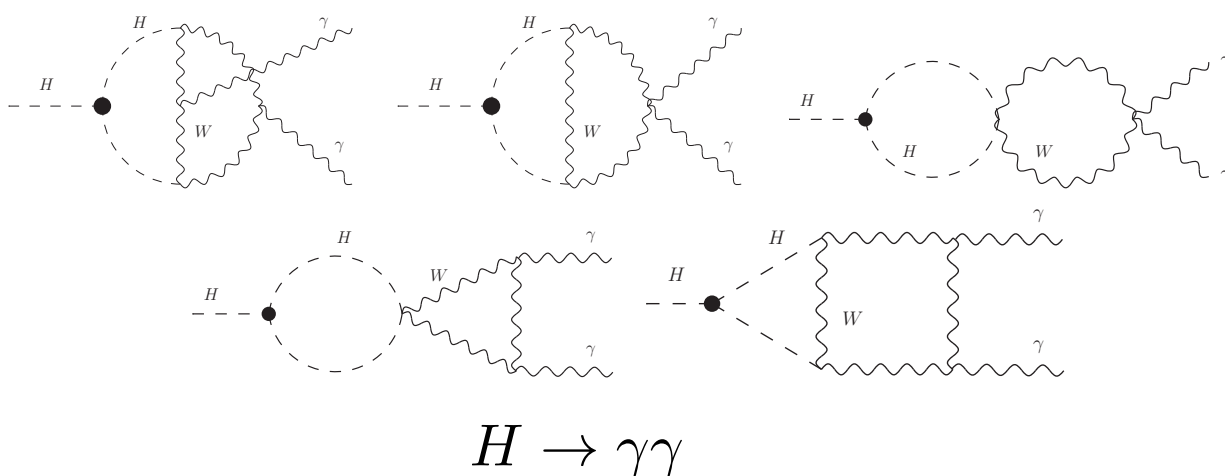
$$K_t \quad K_Z, K_W$$

Standard “kappa framework” does not capture the full effect

## 2 Loop Case : *FeynArts and expansions*



Large top-mass expansion with terms up to  $\mathcal{O}(m_H^6/m_t^6)$



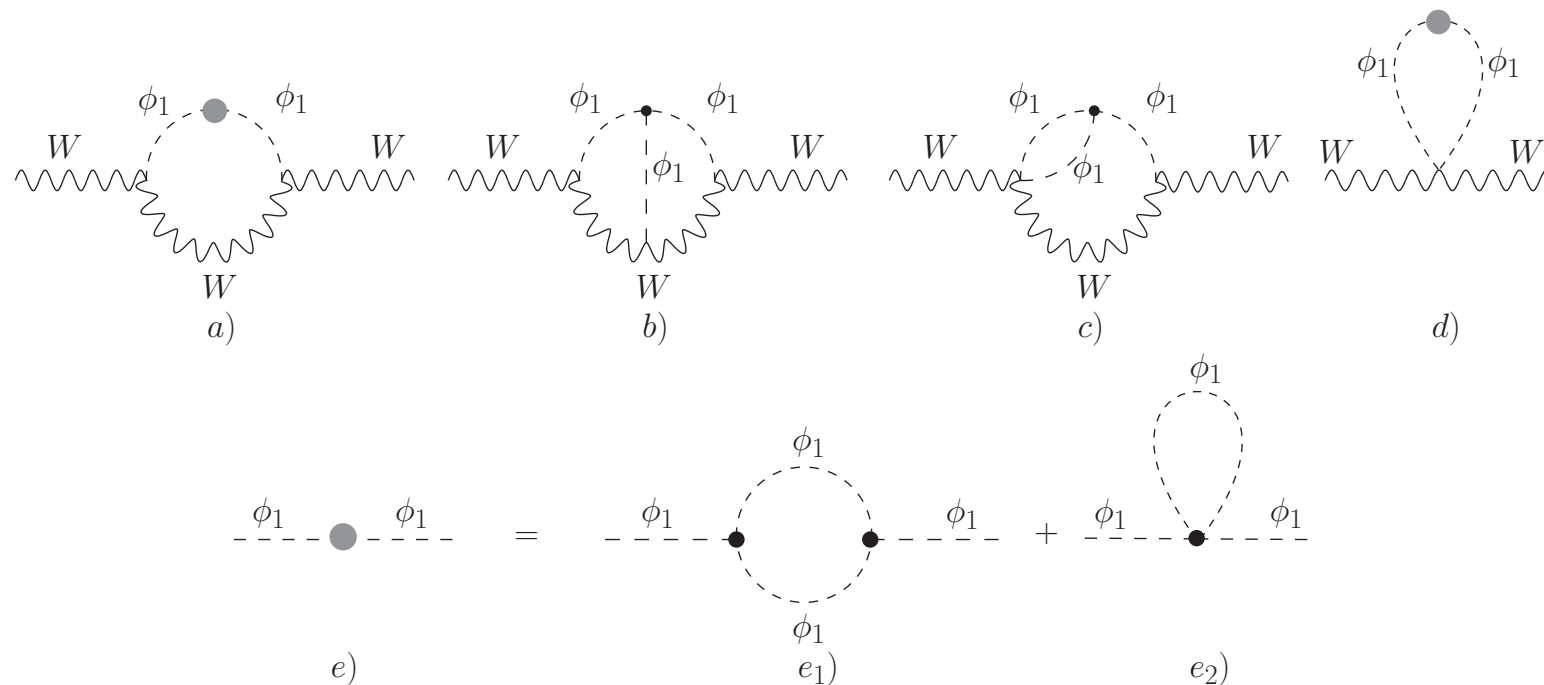
Taylor expansion in  $q^2/(4m_W^2)$ ,  $q^2/(4m_H^2)$  up to  $\mathcal{O}(q^6/m^6)$

Calculation performed in unitary gauge in order to identify genuine  $\lambda_3$ -dependence and keep only kinematic  $m_H$ -dependence

# EWPO: dependence on the Higgs self coupling

The trilinear coupling enters the two-loop relations among  $m_W$  and  $\sin^2 \theta_{\text{eff}}^{\text{lep}}$  and the EW input parameters. At two-loop, there is not dependence on the quadrilinear coupling.

*Degrassi, Fedele, Giardino '17*



$$m_W^2 = \frac{\hat{\rho} m_Z^2}{2} \left\{ 1 + \left[ 1 - \frac{4\hat{A}^2}{m_Z^2 \hat{\rho}} (1 + \Delta \hat{r}_W) \right]^{1/2} \right\}$$

$$\sin^2 \theta_{\text{eff}}^{\text{lep}} = \hat{k}_\ell(m_Z^2) \hat{s}^2, \quad \hat{k}_\ell(m_Z^2) = 1 + \delta \hat{k}_\ell(m_Z^2)$$

$$\hat{A} = (\pi \hat{\alpha}(m_Z) / (\sqrt{2} G_\mu))^{1/2}$$

$$\hat{s}^2 = \frac{1}{2} \left\{ 1 - \left[ 1 - \frac{4\hat{A}^2}{m_Z^2 \hat{\rho}} (1 + \Delta \hat{r}_W) \right]^{1/2} \right\}$$

$$\hat{\rho} \equiv \frac{m_W^2}{m_Z^2 \hat{c}^2} = \frac{1}{1 - \boxed{Y_{MS}}}$$

Terms  
affected  
by  $\kappa$

$$\frac{G_\mu}{\sqrt{2}} = \frac{\pi \hat{\alpha}(m_Z)}{2 m_W^2 \hat{s}^2} (1 + \boxed{\Delta \hat{r}_W})$$

# EWPO: dependence on the Higgs self coupling

Denoting as  $O$  either  $m_W$  or  $\sin^2 \theta_{\text{eff}}^{\text{lep}}$  one can write

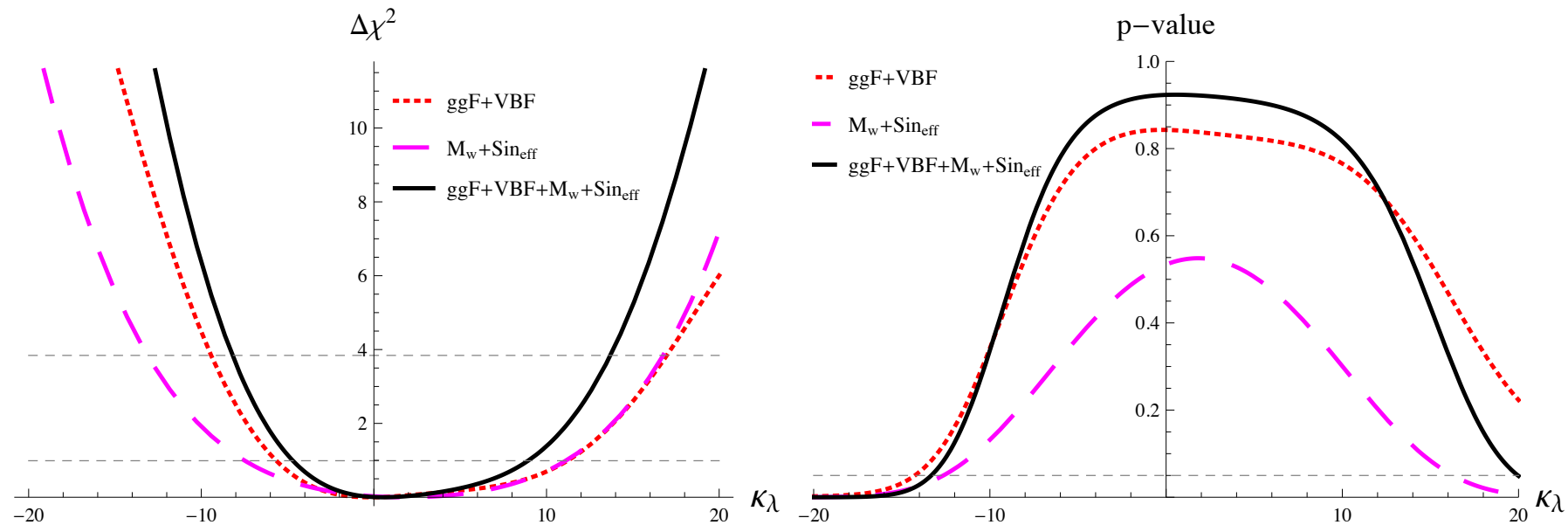
$$O = O^{\text{SM}} [1 + (\kappa_\lambda - 1)C_1 + (\kappa_\lambda^2 - 1)C_2]$$

	$C_1$	$C_2$
$m_W$	$6.27 \times 10^{-6}$	$-1.72 \times 10^{-6}$
$\sin^2 \theta_{\text{eff}}^{\text{lep}}$	$-1.56 \times 10^{-5}$	$4.55 \times 10^{-6}$

*Degrassi, Fedele, Giardino '17*

$$m_W = 80.370 \pm 0.019 \text{ GeV}$$

$$\sin^2 \theta_{\text{eff}}^{\text{lep}} = 0.23185 \pm 0.00035$$



## ggF+VBF (8TeV)

$$\kappa_\lambda^{\text{best}} = -0.24, \quad \kappa_\lambda^{1\sigma} = [-5.6, 11.2], \quad \kappa_\lambda^{2\sigma} = [-9.4, 17.0]$$

## ggF+VBF (8TeV) + EWPO

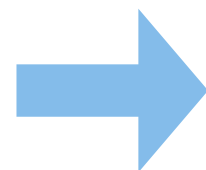
$$\kappa_\lambda^{\text{best}} = 0.5, \quad \kappa_\lambda^{1\sigma} = [-4.7, 8.9], \quad \kappa_\lambda^{2\sigma}_{93} = [-8.2, 13.7]$$

# EWPO: dependence on the Higgs self coupling

Equivalent results can be also found looking at S and T oblique parameters.

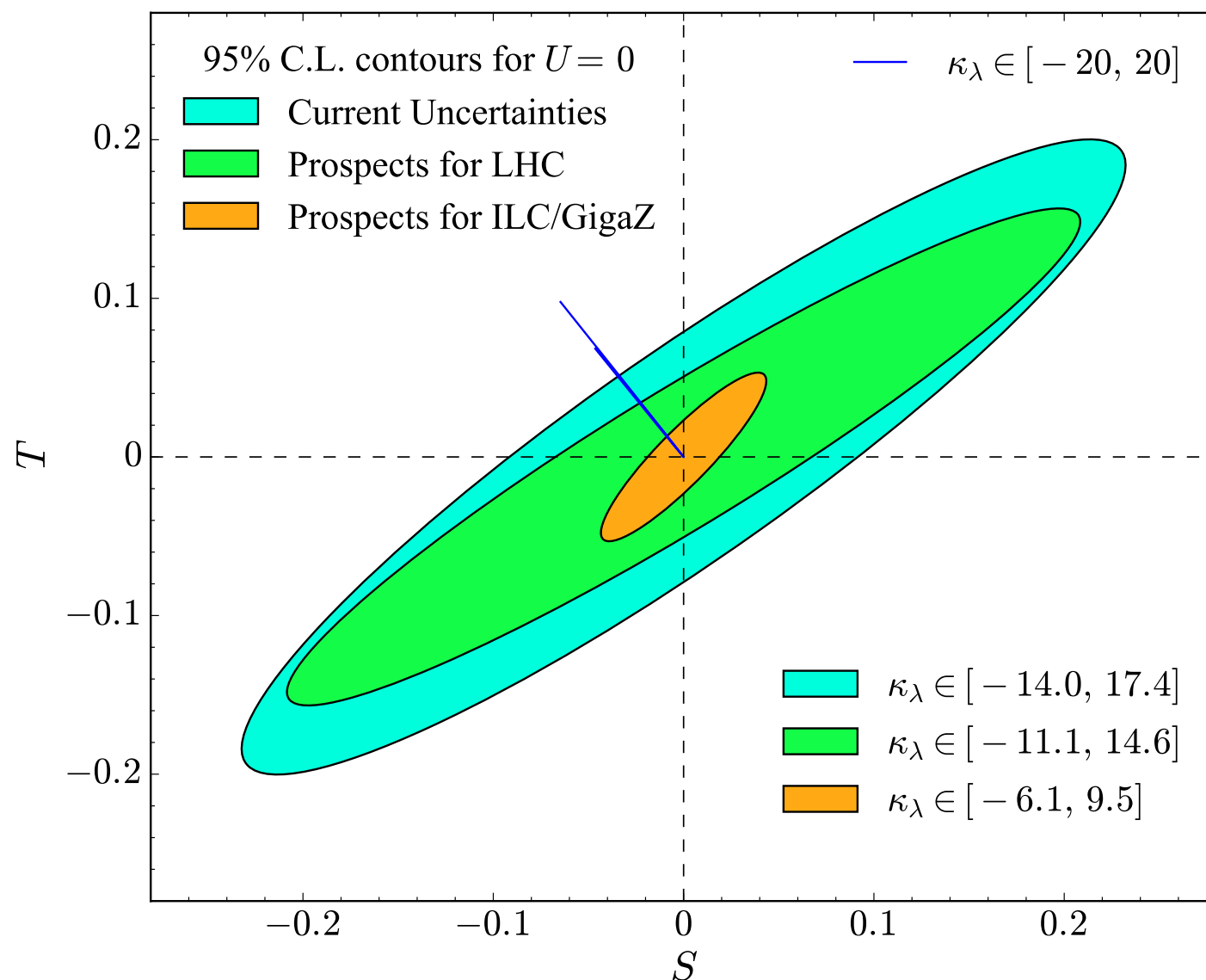
$$S = -0.000138 (\kappa_\lambda^2 - 1) + 0.000456 (\kappa_\lambda - 1)$$

$$T = 0.000206 (\kappa_\lambda^2 - 1) - 0.000736 (\kappa_\lambda - 1)$$



$$-14.0 \leq \kappa_\lambda \leq 17.4$$

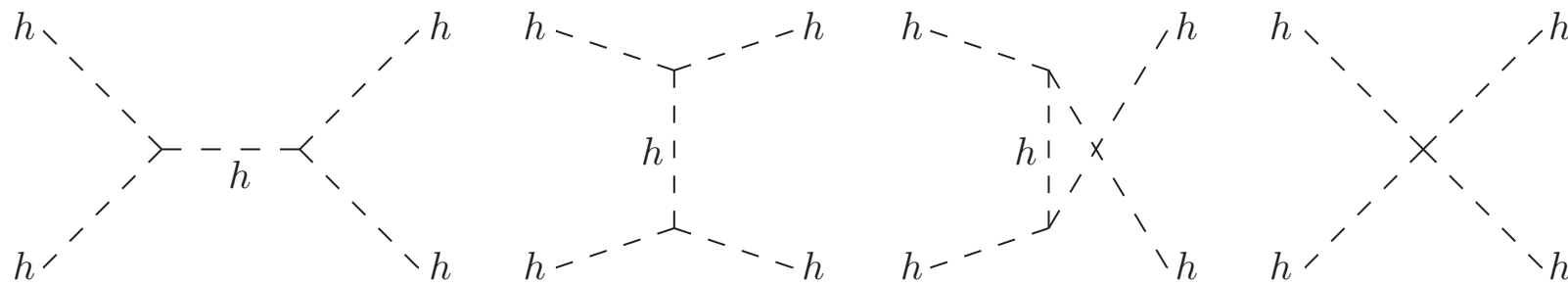
*Kribs, Maier, Rzehak, Spannowsky, Waite '17*



# How large can be the self couplings?

*Di Luzio, Gröber, Spannowsky '17*

- EFT is not the right framework for extracting bounds on Higgs self couplings from the stability of the vacuum.
- General bounds can be extracted from **perturbativiy arguments**.

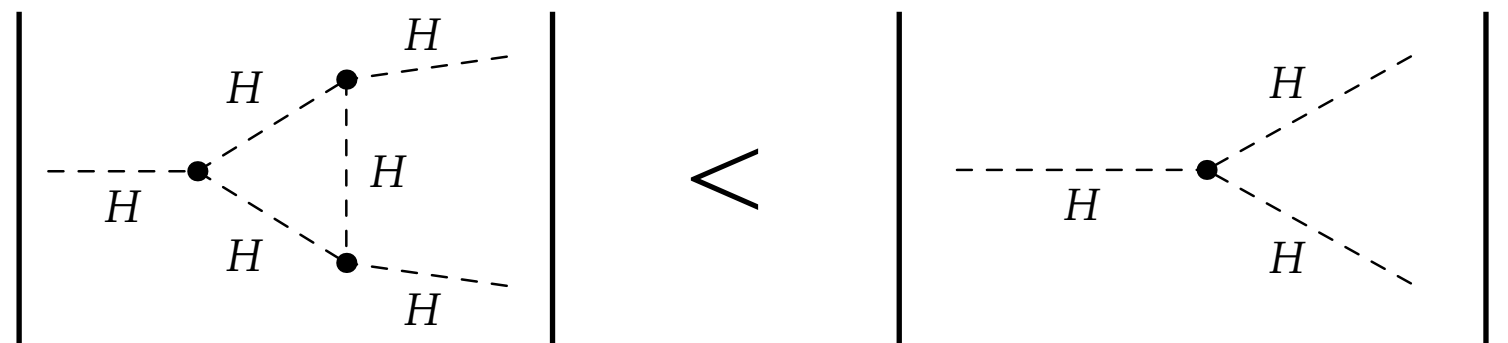


The  $J = 0$  partial wave is found to be

$$a_{hh \rightarrow hh}^0 = -\frac{1}{2} \frac{\sqrt{s(s-4m_h^2)}}{16\pi s} \left[ \lambda_{hhh}^2 \left( \frac{1}{s-m_h^2} - 2 \frac{\log \frac{s-3m_h^2}{m_h^2}}{s-4m_h^2} \right) + \lambda_{hhhh} \right]$$

$$|\text{Re } a_{hh \rightarrow hh}^0| < 1/2 \quad \longrightarrow \quad |\lambda_{hhh}/\lambda_{hhh}^{\text{SM}}| \lesssim 6.5 \quad \text{and} \quad |\lambda_{hhhh}/\lambda_{hhhh}^{\text{SM}}| \lesssim 65$$

Similar bounds on the trilinear by requiring for any external momenta:



# Combined fit with others EFT parameters

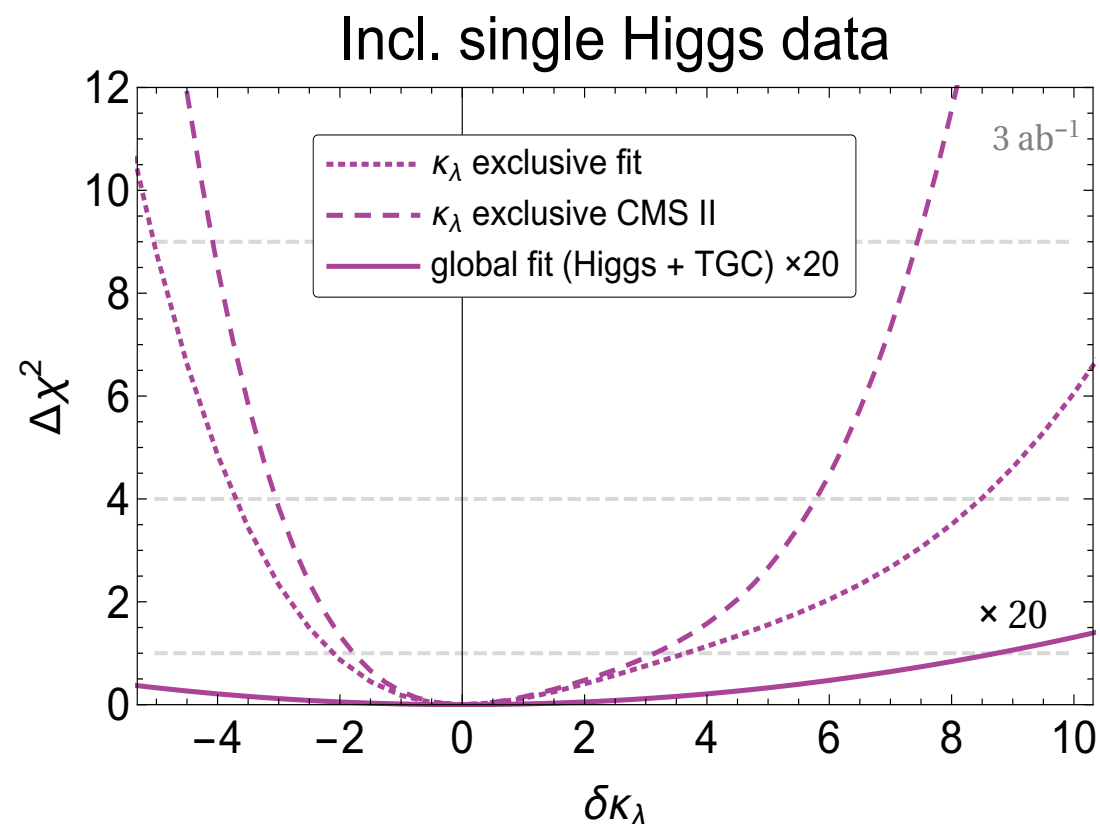
How are limits on  $\kappa_\lambda$  affected by lifting the condition that Higgs interactions with the other particle are SM-like? *Di Vita, Grojean, Panico, Riembau, Vantalon '17*

## Assumptions:

- Consider **all** the possible EFT dimension-6 operators that enter **only** in single Higgs production and decay (**10** independent parameters).

*tree-level:*  $\{\delta c_z, c_{zz}, c_{z\Box}, \hat{c}_{z\gamma}, \hat{c}_{\gamma\gamma}, \hat{c}_{gg}, \delta y_t, \delta y_b, \delta y_\tau$  *loop:*  $\kappa_\lambda$

- Consider **only inclusive** single-Higgs observable (**9** independent constraints)



**10** parameters vs **9** constraints  $\longrightarrow$  1 flat direction so no constraints for the weakest:  $\kappa_\lambda$

We moved from **1** to **10**: **no Physics in the middle?**

Effect of top chromo-dipole operators (**11**)?

**9** constraints can become **10** (Higgs plus jet, **Double Higgs** ..), or **many** (look at **distributions**)

# Combined fit with others EFT parameters

$$\begin{aligned}
 \mathcal{L} \supset & \frac{h}{v} \left[ \delta c_w \frac{g^2 v^2}{2} W_\mu^+ W^{-\mu} + \delta c_z \frac{(g^2 + g'^2) v^2}{4} Z_\mu Z^\mu \right. \\
 & + c_{ww} \frac{g^2}{2} W_{\mu\nu}^+ W_{-\mu\nu} + c_{w\Box} g^2 (W_\mu^+ \partial_\nu W_{+\mu\nu} + \text{h.c.}) + \hat{c}_{\gamma\gamma} \frac{e^2}{4\pi^2} A_{\mu\nu} A^{\mu\nu} \\
 & \left. + c_{z\Box} g^2 Z_\mu \partial_\nu Z^{\mu\nu} + c_{\gamma\Box} g g' Z_\mu \partial_\nu A^{\mu\nu} + c_{zz} \frac{g^2 + g'^2}{4} Z_{\mu\nu} Z^{\mu\nu} + \hat{c}_{z\gamma} \frac{e\sqrt{g^2 + g'^2}}{2\pi^2} Z_{\mu\nu} A^{\mu\nu} \right] \\
 & + \frac{g_s^2}{48\pi^2} \left( \hat{c}_{gg} \frac{h}{v} + \hat{c}_{gg}^{(2)} \frac{h^2}{2v^2} \right) G_{\mu\nu} G^{\mu\nu} - \sum_f \left[ m_f \left( \delta y_f \frac{h}{v} + \delta y_f^{(2)} \frac{h^2}{2v^2} \right) \bar{f}_R f_L + \text{h.c.} \right] \\
 & - (\kappa_\lambda - 1) \lambda_3^{SM} v h^3, \tag{2.5}
 \end{aligned}$$

*Di Vita, Grojean, Panico, Riemann, Vantalon '17*

$$\delta c_w = \delta c_z,$$

$$c_{ww} = c_{zz} + 2 \frac{\pi^2 g'^2}{g^2 + g'^2} \hat{c}_{z\gamma} + \frac{9\pi^2 g'^4}{2(g^2 + g'^2)^2} \hat{c}_{\gamma\gamma},$$

$$c_{w\Box} = \frac{1}{g^2 - g'^2} \left[ g^2 c_{z\Box} + g'^2 c_{zz} - e^2 \frac{\pi^2 g'^2}{g^2 + g'^2} \hat{c}_{\gamma\gamma} - (g^2 - g'^2) \frac{\pi^2 g'^2}{g^2 + g'^2} \hat{c}_{z\gamma} \right],$$

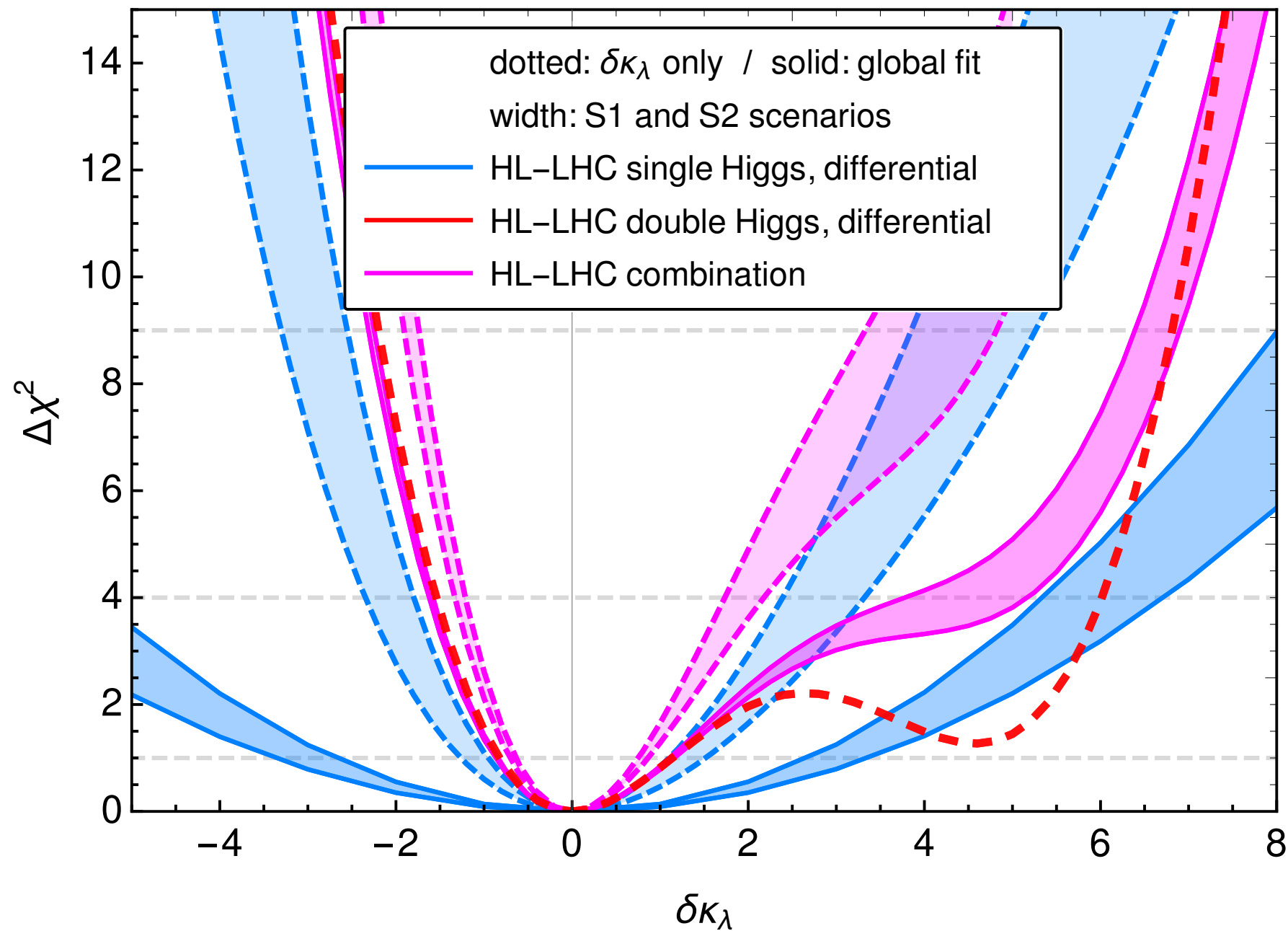
$$c_{\gamma\Box} = \frac{1}{g^2 - g'^2} \left[ 2g^2 c_{z\Box} + (g^2 + g'^2) c_{zz} - \pi^2 e^2 \hat{c}_{\gamma\gamma} - \pi^2 (g^2 - g'^2) \hat{c}_{z\gamma} \right],$$

$$\hat{c}_{gg}^{(2)} = \hat{c}_{gg},$$

$$\delta y_f^{(2)} = 3\delta y_f - \delta c_z.$$

# Combined fit with others EFT parameters

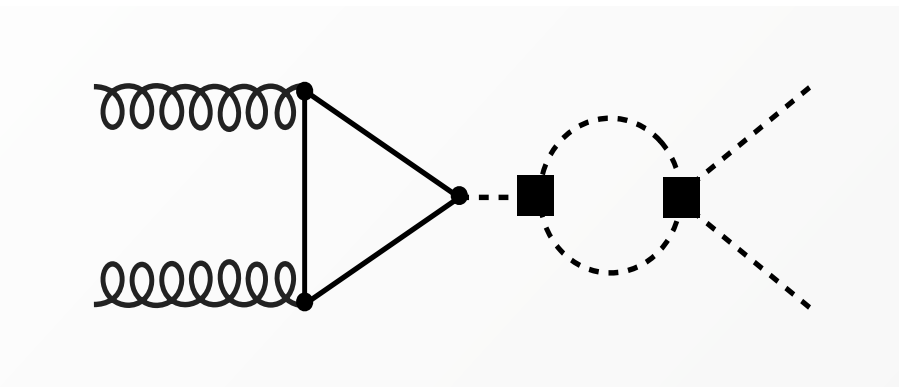
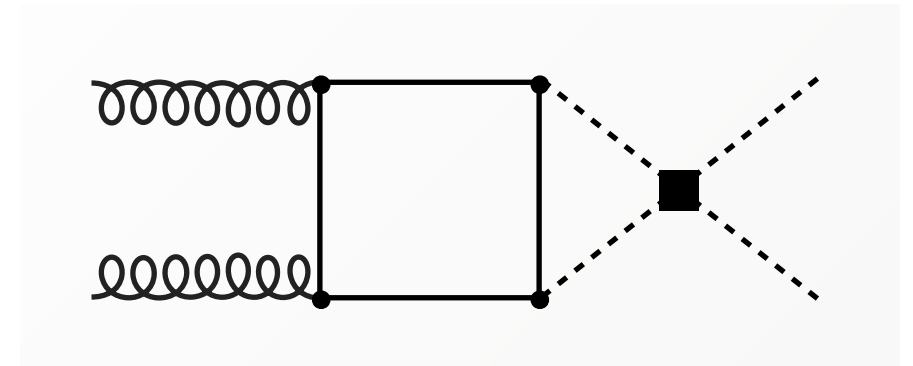
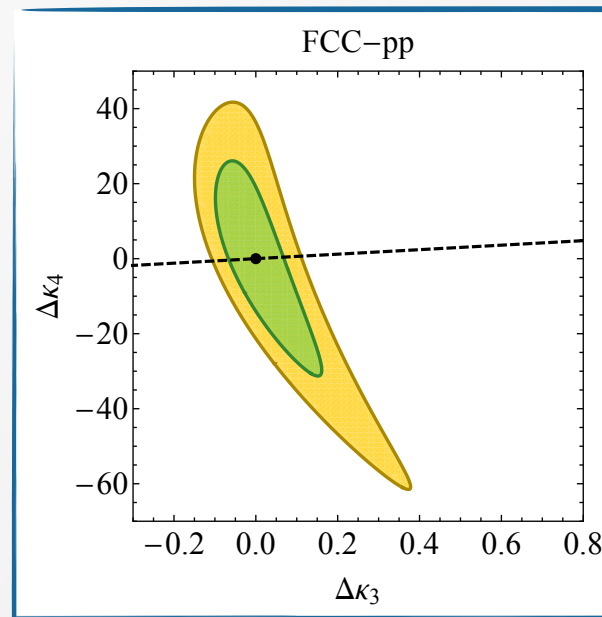
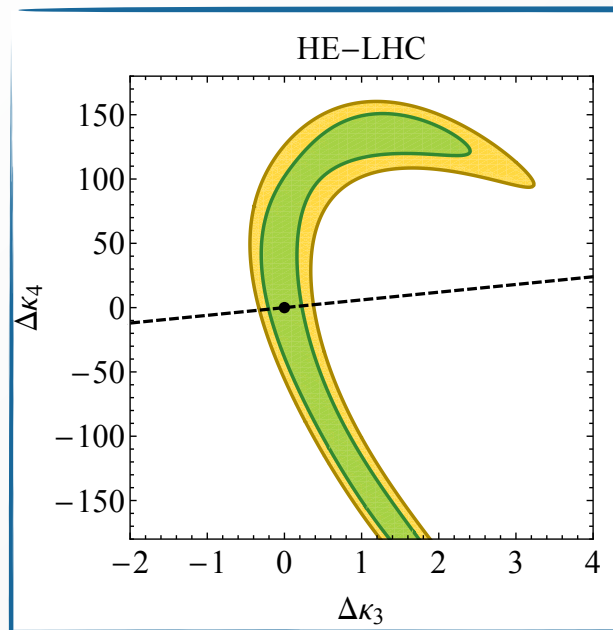
Combination with Double Higgs at HL-LHC.



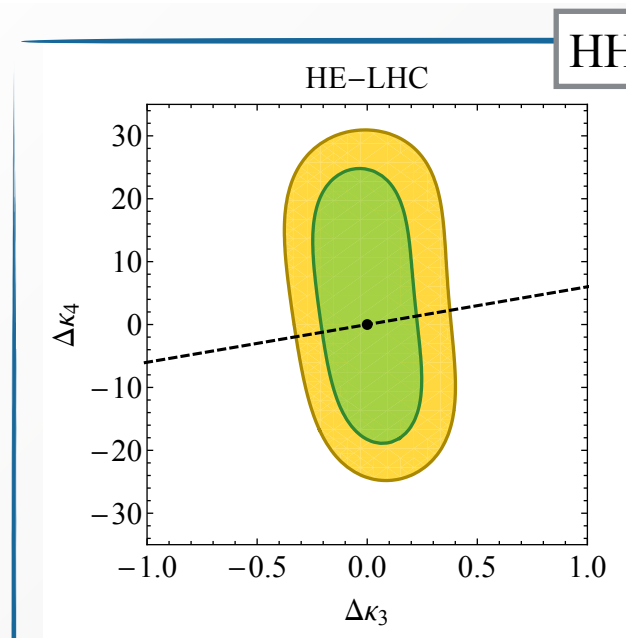
*HL- HE-LHC Report WG2*



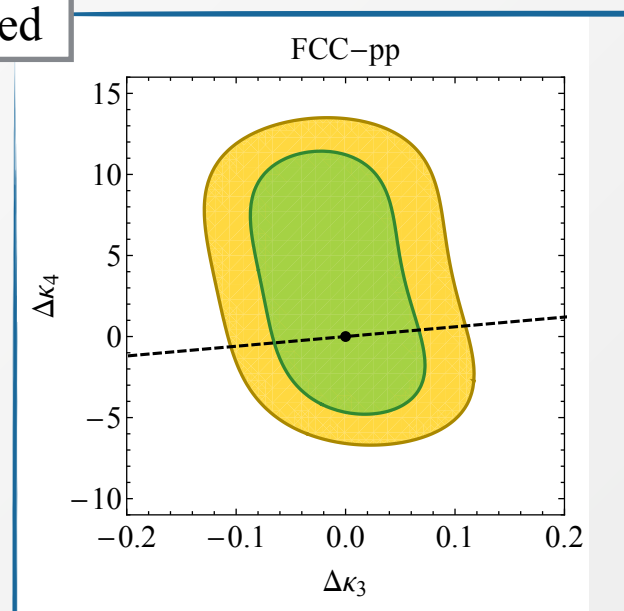
# Quartic coupling at hadron colliders: first estimate



*from talk of Luca Rottoli*



HHH included



$\kappa_3 = 1$        $\kappa_4 \in [-20, 29]$

Profiling over  $\kappa_3$        $\kappa_4 \in [-17, 25]$

$\kappa_3 = 1$        $\kappa_4 \in [-5, 13]$

Profiling over  $\kappa_3$        $\kappa_4 \in [-4, 12]$

The  $m(\text{HH})$  distribution is e in the analysis.

*Bizon, Haisch, Rottoli '18*

$\kappa_3 \sim 1 \rightarrow |\kappa_4| \lesssim 31$   
for sensible results  
(perturbativity)