

(α, γ) & (α, n) key reaction studies
using
 $({}^7\text{Li}, t)$ alpha-transfer reactions

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Why studying (α,γ) & (α,n) reactions via α -transfer reactions?

- $^{12}\text{C}(\alpha,\gamma)^{16}\text{O}$ (massive stars), $^{14}\text{C}(\alpha,\gamma)^{18}\text{O}$ (AGB stars & ^{19}F)
- $^{13}\text{C}(\alpha,n)^{16}\text{O}$
- $^{22}\text{Ne}(\alpha,n)^{25}\text{Mg}$, $^{22}\text{Ne}(\alpha,\gamma)^{25}\text{Mg}$
- $^{17}\text{O}(\alpha,n)^{20}\text{Ne}$, $^{17}\text{O}(\alpha,\gamma)^{21}\text{Ne}$
- $^{15}\text{O}(\alpha,\gamma)^{19}\text{Ne}$ (Type I X-ray bursts)

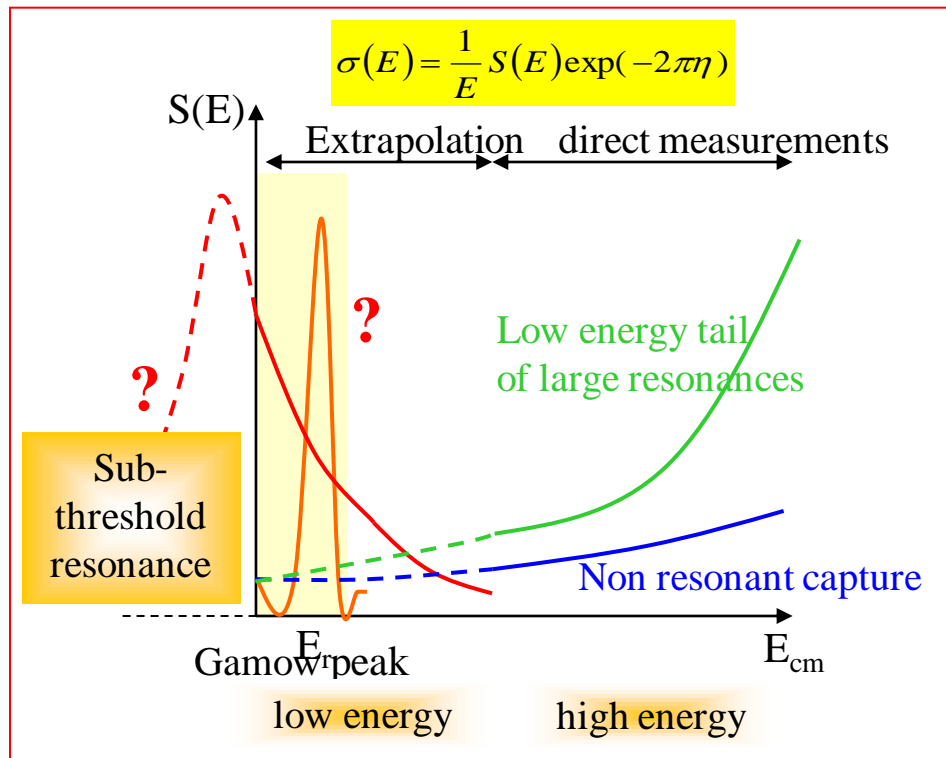
s-process in AGB
& massive stars

$T=0.1-1$ GK

→ hundreds keV- MeV $\ll E_C$

→ $\sigma(E)$ very weak (0.01 fb- ~100 pb)

→ Direct measurements are very challenging or impossible



➤ In case of stable nuclei:
Direct measurements of $\sigma(E)$ at high energies
then extrapolation at stellar energies

But:

Problems with extrapolation: resonances at very low energy, sub-threshold resonances

➤ In case of radioactive nuclei:
Low beam intensities ($\sim 10^5 - 10^7$ p/s)
→ direct measurements challenging

Resonant cross-sections & $N_a \langle \sigma v \rangle$ can be calculated if $(E_R, J^\pi, \Gamma_\alpha, \Gamma_n, \Gamma_\gamma, \Gamma_{\text{tot}})$ are known/constrained
 → ($^7\text{Li}, t$) or ($^6\text{Li}, d$) α -transfer reactions → $E_R, l_\alpha, S_\alpha \Rightarrow \gamma^2_\alpha, \Gamma_\alpha$

$^{12}\text{C}(\alpha,\gamma)^{16}\text{O}$: the challenge of Nuclear Astrophysics

→ Crucial for energetics, nucleosynthesis, final fate of the massive stars,...

• $^{12}\text{C}(\alpha,\gamma)^{16}\text{O}$ → 40% uncertainty

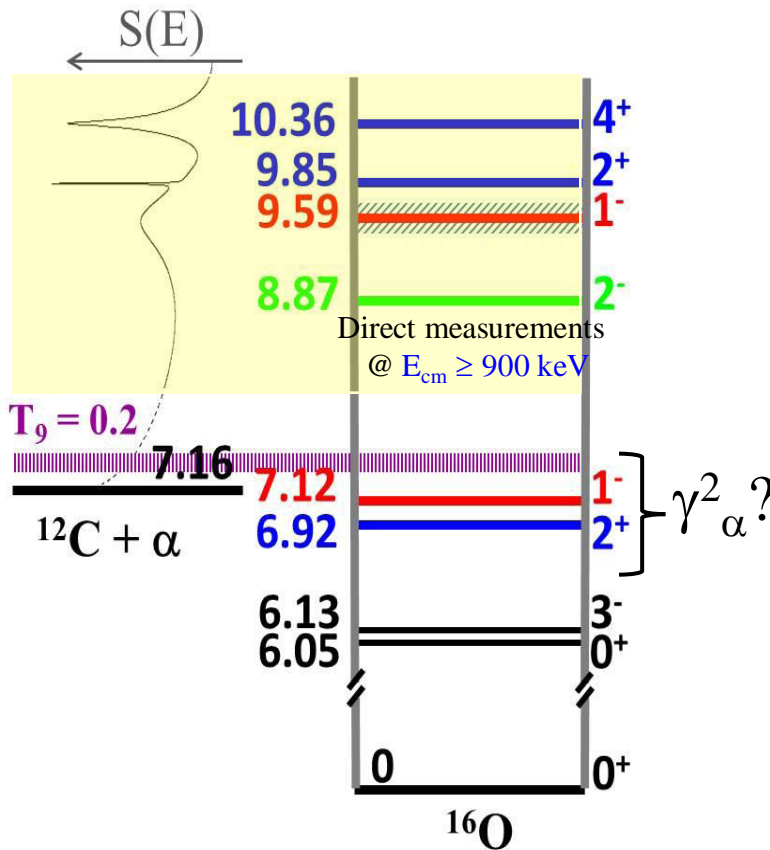
• $T=0.2$ GK Gamow peak ~ 300 keV, $\sigma(E_0) \sim 10^{-8}$ nb

Direct measurements @ 300 keV → impossible



Need of precise data at high energies
& extrapolation at 300 keV (R-matrix formalism)

BUT



Overlap of various contributions:

- E1 & E2 transitions to the gs:

Effect of the high energy tail of the 1^- & 2^+ sub-threshold resonances ($S_\alpha, \gamma^2_\alpha$?)

$$S_\alpha(1^-) \rightarrow 0.02-1.08 \text{ !?}$$

$$S_\alpha(2^+) \rightarrow 0.13-1.35 \text{ !?}$$

&

Interference effect & cascades ?

⇒ Study of 6.92 & 7.12 MeV states ^{16}O via the transfert reaction $^{12}\text{C}(^7\text{Li},t)^{16}\text{O}$

Study of ^{16}O states via $^{12}\text{C}(^7\text{Li},t)^{16}\text{O}$ α -transfer reaction

Advantages

- multi-step effects less marked than in $(^6\text{Li},d)$ transfer reaction
Becchetti et al. (78), Cobern et al.(81), Keeley et al (06)
- less momentum mismatch ($L_\alpha=1$ in ^7Li)

$$\left. \frac{d\sigma}{d\Omega} \right|_{\text{exp}} = C^2 S'_\alpha S_\alpha \left. \frac{d\sigma}{d\Omega} \right|_{FR-DWBA}$$

$$S'_\alpha = \langle ^7\text{Li} | t \otimes \alpha \rangle = 1 \quad (\text{Kubo et al})$$

$$S_\alpha = \langle ^{16}\text{O} | ^{12}\text{C} \otimes \alpha \rangle$$

ANC

$$\tilde{C}^2 = S_\alpha \frac{r^2 |\varphi(r)|^2}{W(r)^2}$$

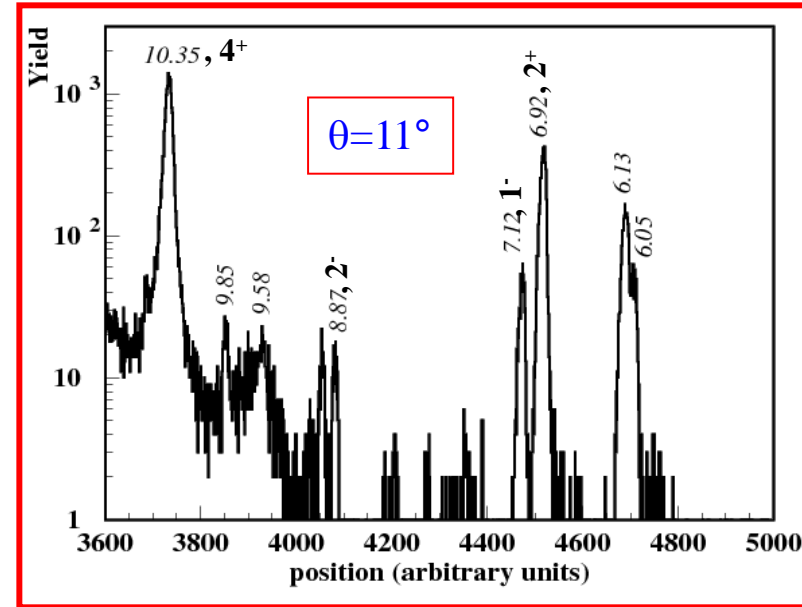
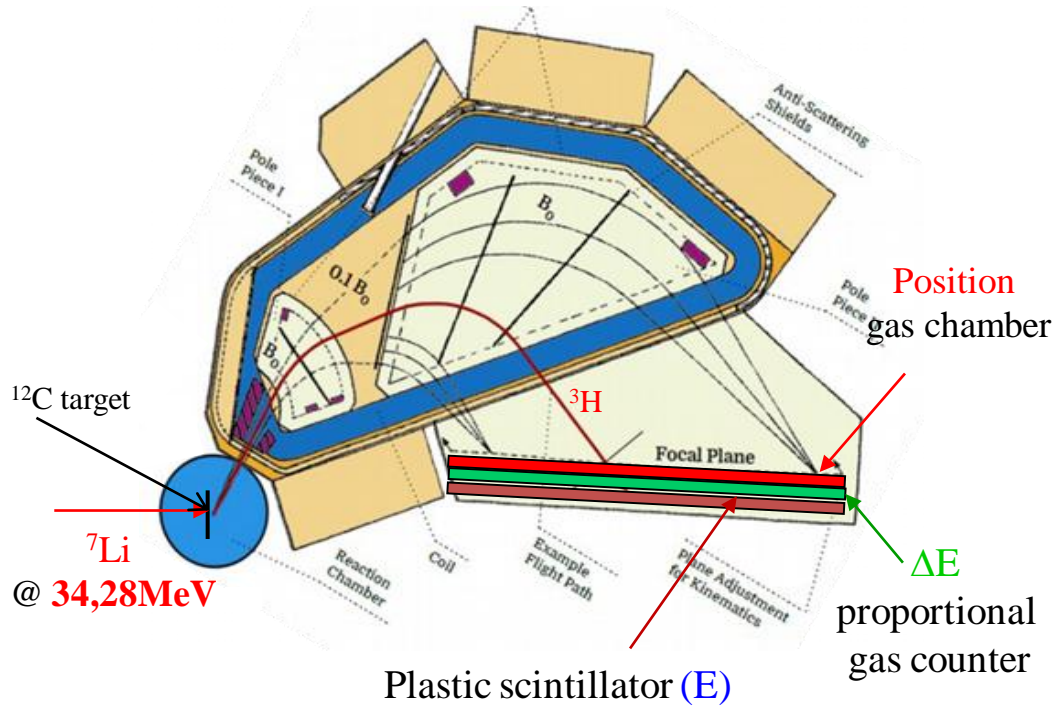
$$\gamma_\alpha^2 = \frac{\hbar^2 r}{2\mu} S_\alpha |\varphi(r)|^2$$

Detailed and elaborate finite-range DWBA analysis of the data is needed

Experimental Set-up

Split-Pole spectrometer (ALTO-Orsay)

- $\Delta\Omega \sim 1.7 \text{ msr}$
- $\Delta E/E \sim 5 \times 10^{-4}$

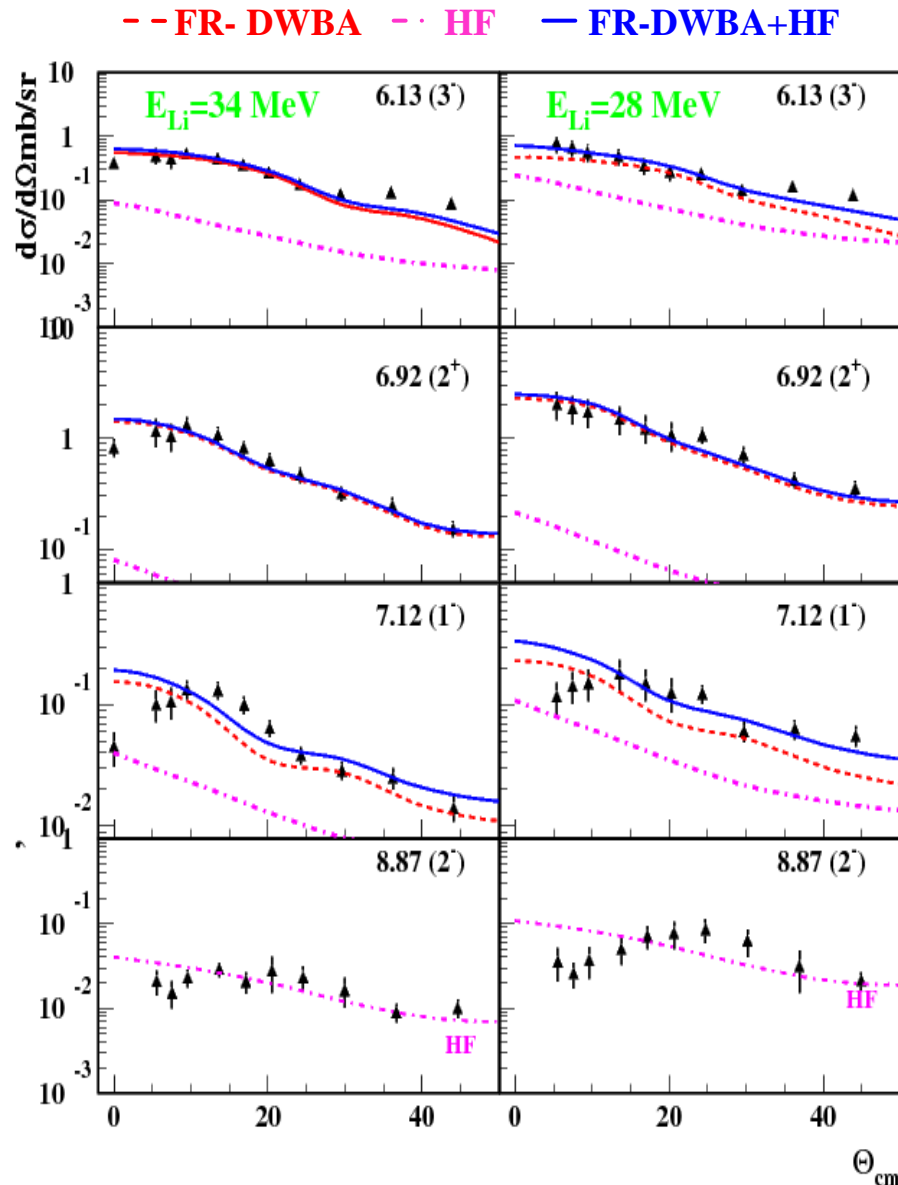


- $d\sigma/d\Omega$ measurements up to 45°

- Strong population of the α cluster 2^+ & 4^+ state \rightarrow direct transfer mechanism
- Population (weak) of the 2^- , 8.87 MeV state \rightarrow compound nucleus?

FR-DWBA
& HF calculations

Results: Comparison exp & calculations



→ Good description of the data by DWBA
(6.05, 6.13, 6.92, 7.12, 9.58 et 10.35 MeV)



Direct transfer mechanism

→ Disagreement at $\theta < 10^\circ$ for the 7.12 MeV



Multi-step transfer? → $d\sigma/d\Omega \searrow$



No (CDCC calculations of Keeley)

$$S_\alpha(2^+) = 0.15 \pm 0.05$$

$$S_\alpha(1^-) = 0.08 \pm 0.03$$

Main source of error



DWBA input parameters

R matrix calculations– E2 & E1 components

$$S_{\alpha}(6.92)=0.15\pm 0.05 \rightarrow \gamma_{\alpha}^2 = 27 \pm 10 \text{ keV}$$

$$S_{\alpha}(7.12)=0.08\pm 0.03 \rightarrow \gamma_{\alpha}^2 = 8 \pm 3 \text{ keV}$$

$r=6.5\text{fm}$ Asymptotic region

$$\tilde{C}^2(2^+) = (2.07 \pm 0.80) \times 10^{10} \text{ fm}^{-1}$$

$$\tilde{C}^2(1^-) = (4.00 \pm 1.38) \times 10^{28} \text{ fm}^{-1}$$

In agreement with ANC sub-coulomb experiments
Brune+2001, Avila+2014

Multi-level R-matrix analysis

P. Descouvemont DREAM Code

$$R_{CC'} = \sum_{\lambda} \frac{\gamma_{\lambda C} \gamma_{\lambda C'}}{E_{\lambda} - E}$$

➤ Fit E2 & E1 components separately

➤ Fit $^{12}\text{C}(\alpha,\gamma)^{16}\text{O}$ astrophysical S-factors (direct data)

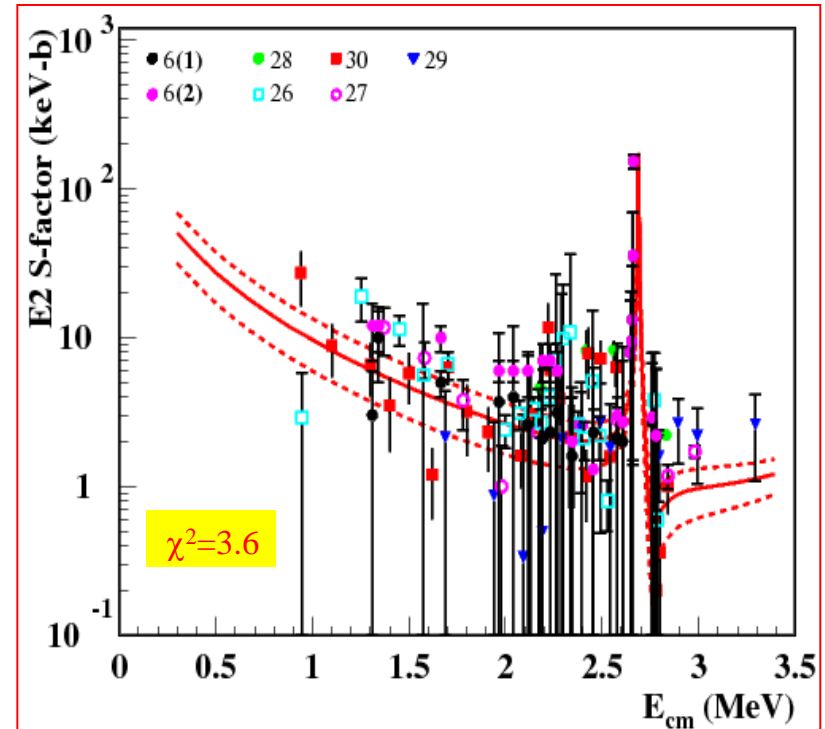
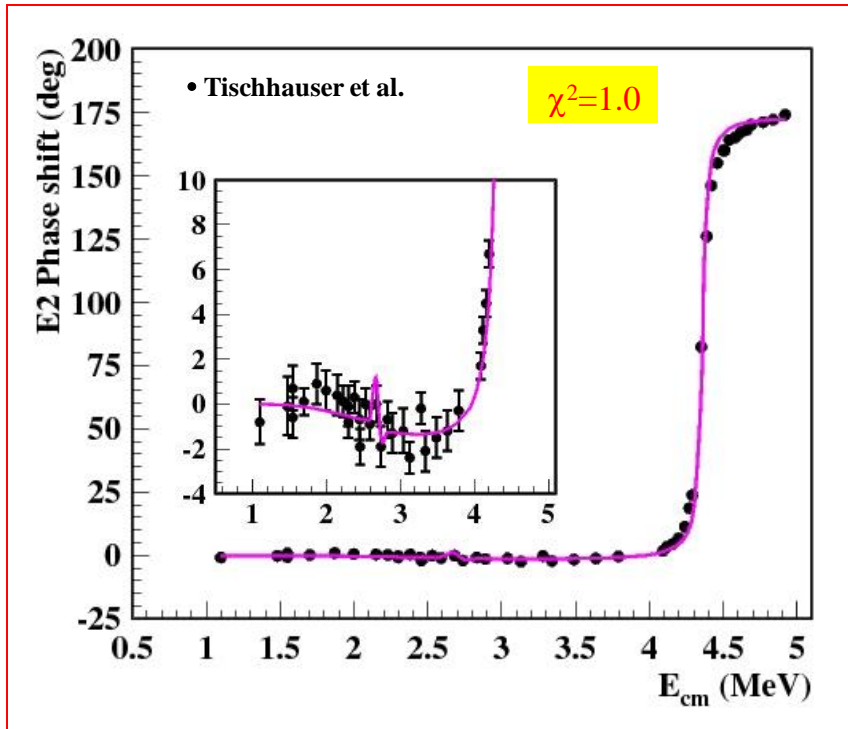
➤ Fit phase shifts data \rightarrow $^{12}\text{C}(\alpha,\alpha)^{12}\text{C}$ measurements

$S_{E2}(300 \text{ keV})$

$S_{E1}(300 \text{ keV})$

R matrix calculations– E2 component

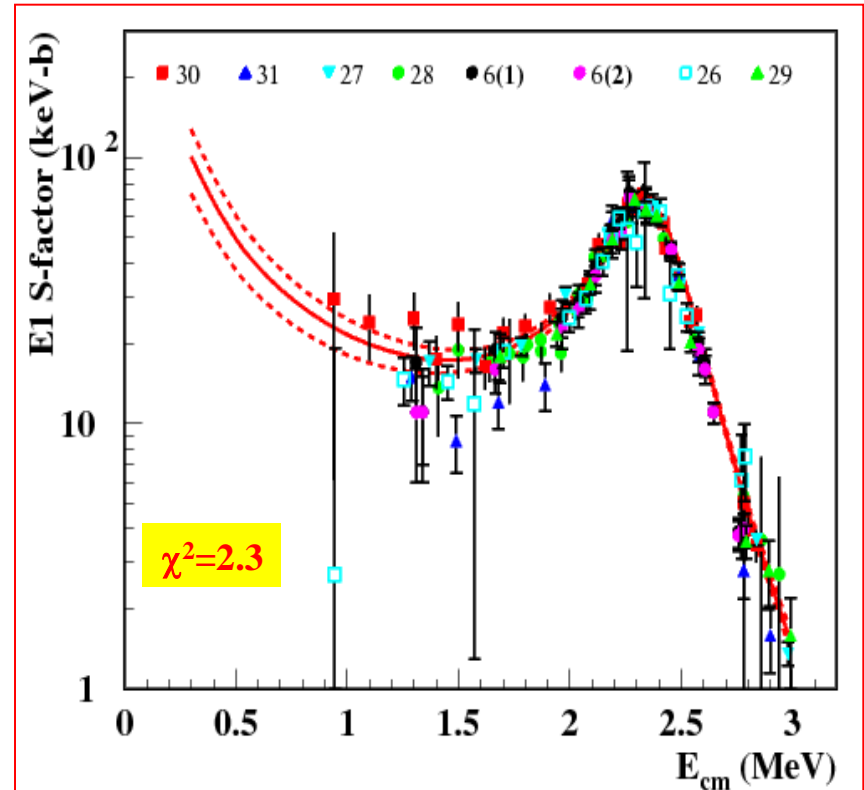
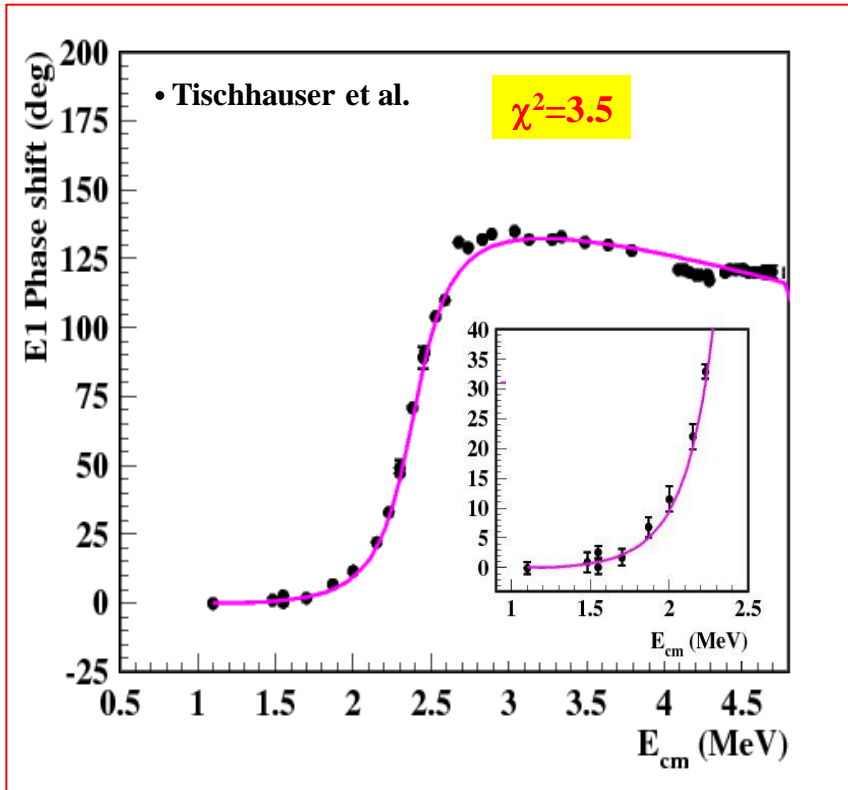
- E2 Component calculation → 4 states
- 6.92, 9.85, 11.52 MeV → fixed resonance parameters
- Background equivalent state ($E_{r4}, \Gamma_{\alpha4}, \Gamma_{\gamma4}$)



$$S_{E2}(300 \text{ keV}) = 50 \pm 19 \text{ keV-barn}$$

R matrix calculations– E1 component

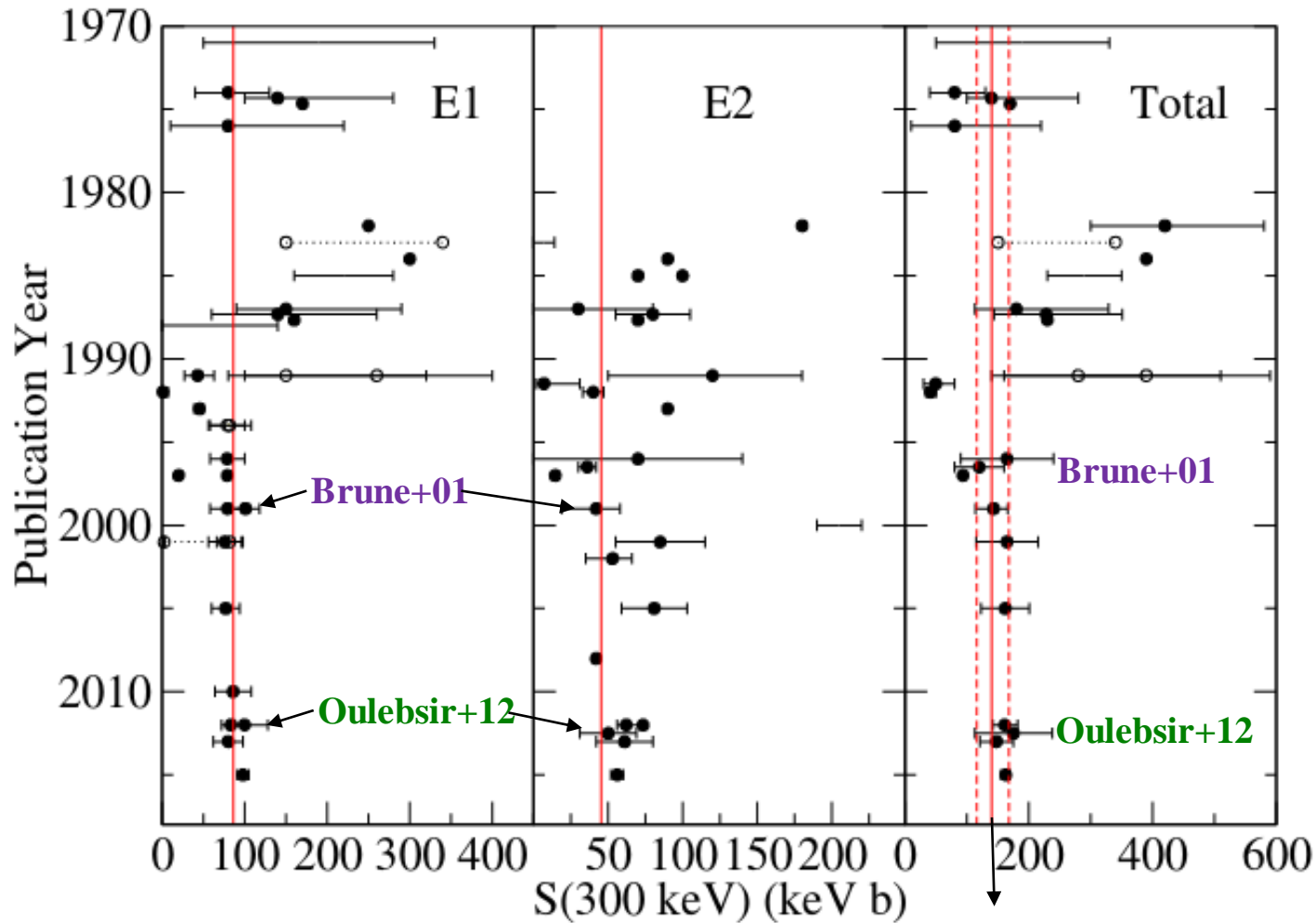
- E1 Component calculation → 3 states
- 7.12, 9.58 → fixed resonance parameters
- Background equivalent state ($E_{r3}, \Gamma_{\alpha3}, \Gamma_{\gamma3}$)



$$S_{E1}(300 \text{ keV}) = 100 \pm 28 \text{ keV-barn}$$

$S_{E1}(0.3 \text{ MeV})$, $S_{E2}(0.3 \text{ MeV})$ & $S_{\text{tot}}(0.3 \text{ MeV})$ over time

Credits: **deBoer+17**



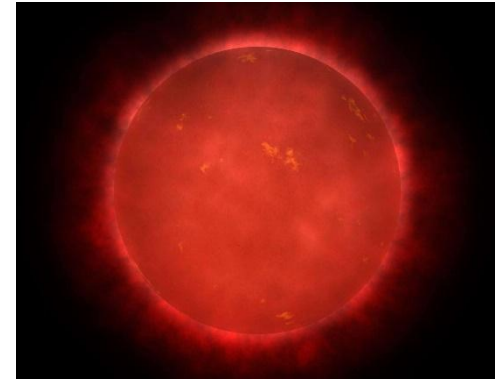
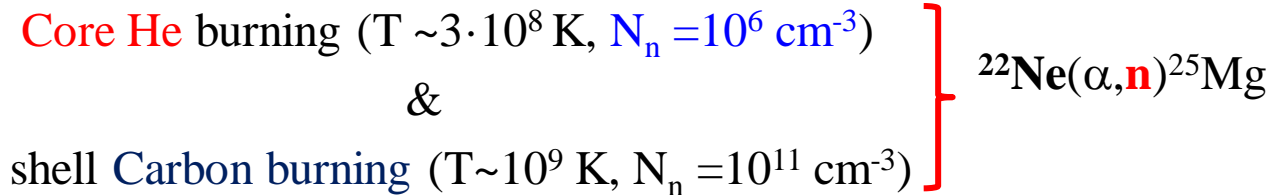
$S_{\text{tot}} = 140 \pm 21 \text{ keV-b}$

→ From MC analysis of all existing data including ANC's from transfer reactions (**deBoer+17**)

s-process in rotating metal-poor massive stars

- *s*-process nucleosynthesis → half of the abundance of heavy elements in Universe

- $60 < A < 90$ (weak *s*-process component) → massive stars $M > 8M_{\odot}$



- **Metal-poor** massive stars → **negligible** *s*-process production (low ^{22}Ne & Fe seed abundance)

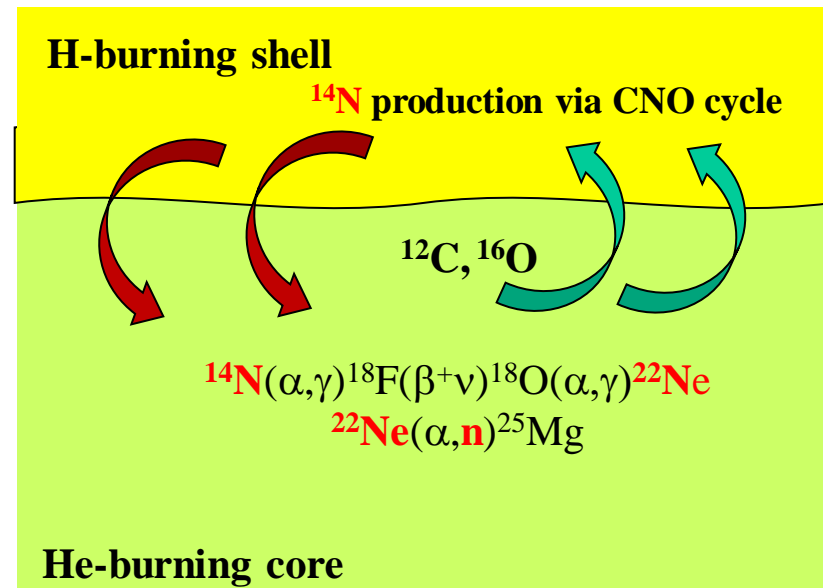
With **fast rotation induced mixing**
 Nishimura+16, Choplin+18

⇒ ^{22}Ne production in He core strongly enhanced



large production of *s*-elements between
 Strontium & Barium

$90 < A < 140$

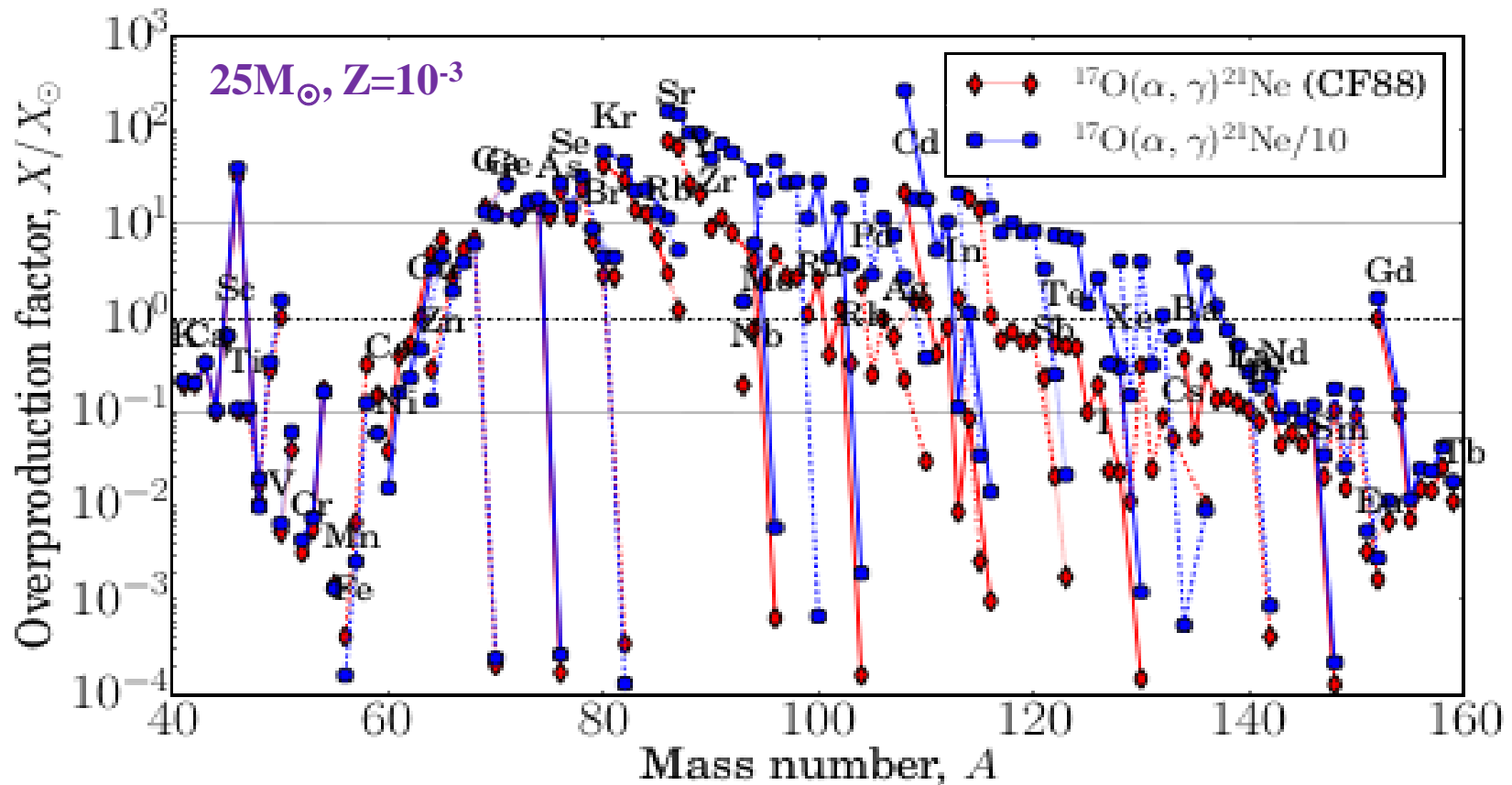


s-process in rotating metal-poor massive stars

But the final abundances of the enhanced weak s-process strongly depends on:

$^{16}\text{O}(n,\gamma)^{17}\text{O}$ neutron poison effect & $^{17}\text{O}(\alpha,n)/^{17}\text{O}(\alpha,\gamma)$ reaction rate ratio

→ neutron recycling efficiency



Calculation with $^{17}\text{O}(\alpha,n)^{20}\text{Ne}$ Nacre adopted rate & $^{17}\text{O}(\alpha,\gamma)^{22}\text{Ne}$ CF88 rate

Present status on $^{17}\text{O}(\alpha, n)^{20}\text{Ne}$ and $^{17}\text{O}(\alpha, \gamma)^{21}\text{Ne}$

- Core He burning: $T \sim 0.2\text{-}0.3 \text{ GK} \rightarrow E_{\text{c.m.}} \sim 0.297\text{-}0.646 \text{ MeV} \rightarrow E_x = 7.62\text{-}8.00$ in ^{21}Ne
- Shell Carbon burning: $T \sim 1 \text{ GK} \rightarrow E_{\text{c.m.}} \sim 0.783\text{-}1.5 \text{ MeV} \rightarrow E_x = 8.13\text{-}8.85$ in ^{21}Ne

$^{17}\text{O}(\alpha, n)^{20}\text{Ne}$ & $^{17}\text{O}(\alpha, \gamma)^{21}\text{Ne}$ direct measurements:

- Denker+1994, Best+2013 $\rightarrow 0.63 \leq E_{\text{cm}} \leq 1.8 \text{ MeV}$
- Best +2011, Taggart+2019 $\rightarrow 0.63 \leq E_{\text{cm}} \leq 1.33 \text{ MeV}$
- Williams+2022

- No direct measurements @ $E_{\text{cm}} < 0.63 \text{ MeV}$ (Core He burning)

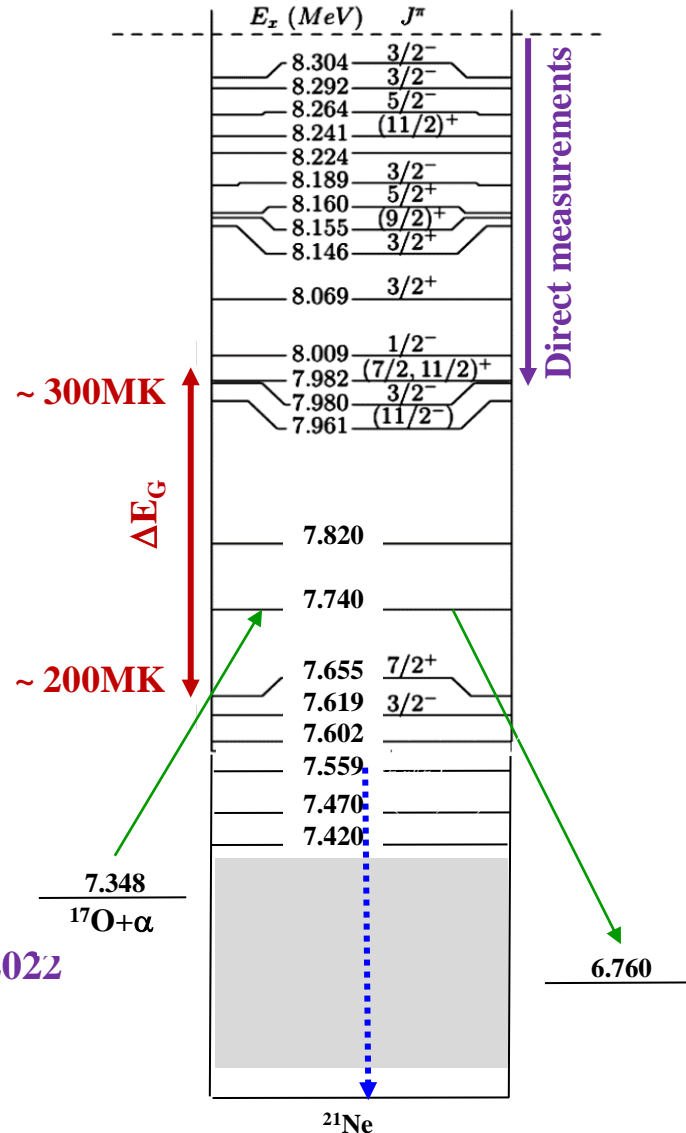
- Spectroscopy of ^{21}Ne : E_x , S_α or Γ_α , J^π , $\Gamma_\gamma/\Gamma_{\text{tot}}$, Γ_n

\rightarrow Unknown or poorly known S_α (Γ_α) & Γ_n , $\Gamma_\gamma/\Gamma_{\text{tot}}$

\rightarrow Few have spin-parity assignments

- Neutron transfer reaction $\rightarrow S_n \rightarrow \Gamma_n$ Frost-Schenk+MNRAS2022

- α -transfer reaction $\rightarrow S_\alpha \rightarrow \Gamma_\alpha$ (present work/MLL-exp)



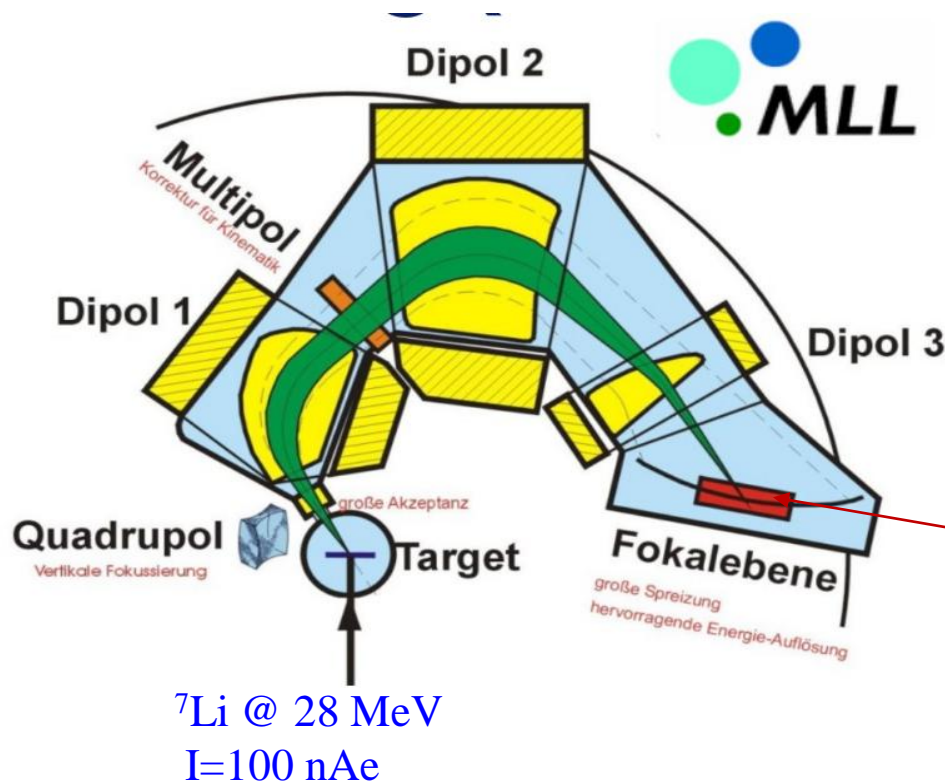
Study of ^{21}Ne states via $^{17}\text{O}(^7\text{Li},t)^{21}\text{Ne}$ α -transfer reaction

Q3D spectrometer (MLL)

- $\Delta\Omega \sim 6$ to 12.4 msr
- $\Delta E/E \sim 2 \times 10^{-4}$

➤ Targets (manufactured at LNS Catania):

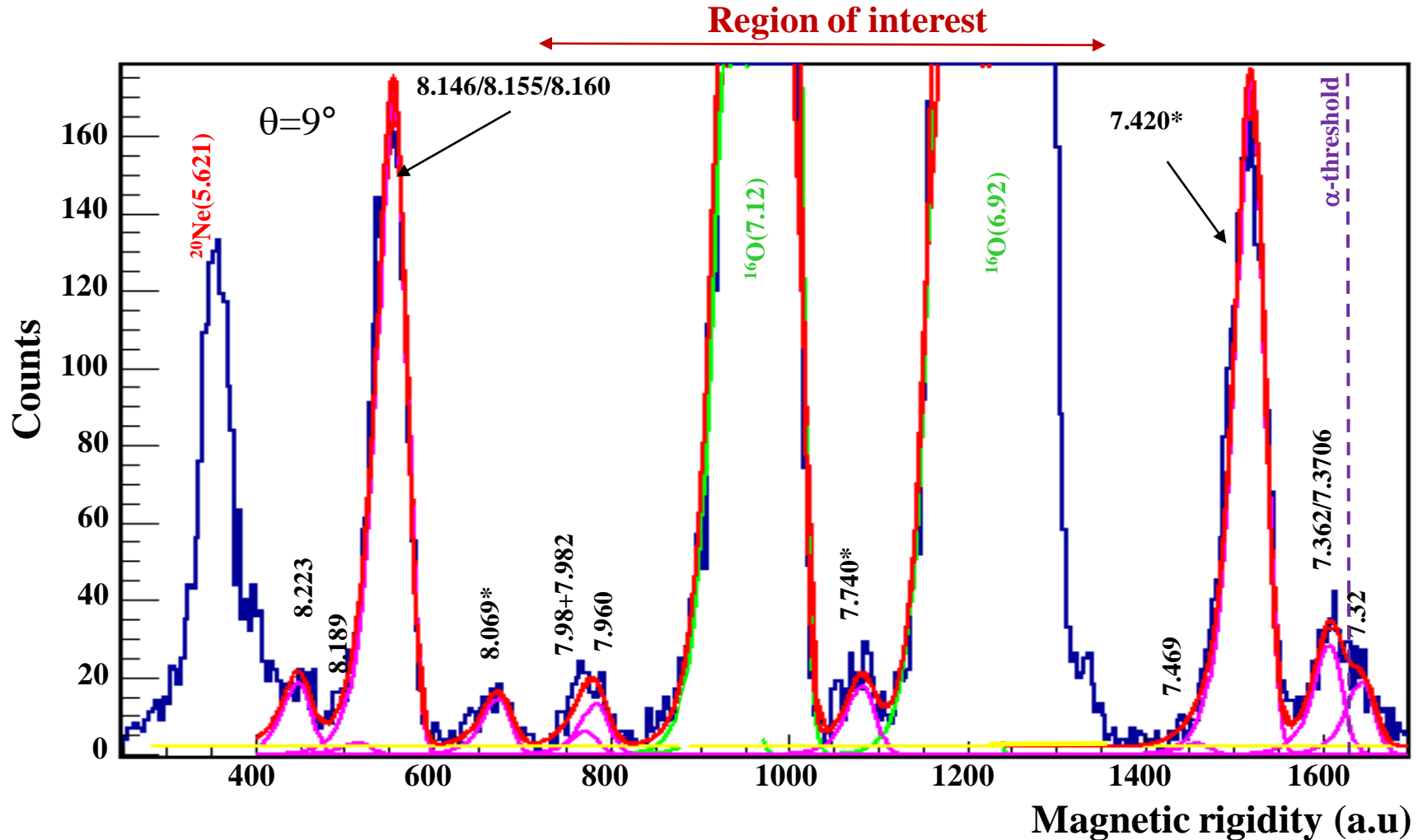
- $41 \mu\text{g}/\text{cm}^2$ ^{17}O enriched (35%) WO_3 target on $^{\text{nat}}\text{C}$
- $39 \mu\text{g}/\text{cm}^2$ natural WO_3 target on $^{\text{nat}}\text{C}$



Pos, $\Delta E_1, \Delta E_2, E$
2 proportional gas counter
& plastic scintillator

➤ $d\sigma/d\Omega$ measurements @ $\theta_{\text{lab}} = 6^\circ - 36^\circ \Rightarrow \theta_{\text{cm}} \rightarrow 7.5^\circ - 45^\circ$ on enriched target & on natural target for calibration & background evaluation

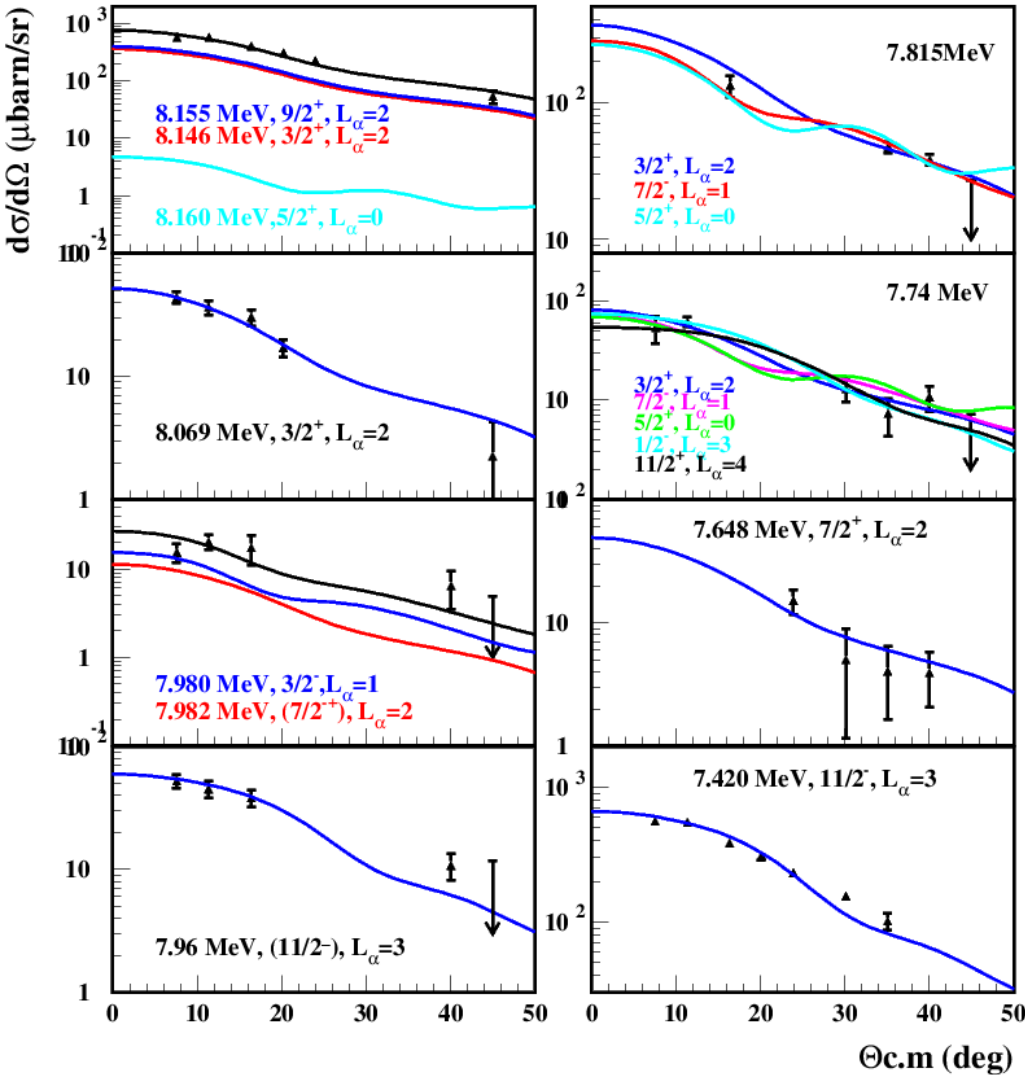
Excitation energy spectrum of ^{21}Ne



- Fit with multiple skewed Gaussians with common width & exponential factor

Experimental energy resolution (FWHM) : ~ 30 keV (6°) - 71 keV (36°)

FR-DWBA calculations



- Good description of the data by DWBA



Direct transfer mechanism

- Triplet 8.160/8.155/8.146:
Fit with 3 components → S_α of 8.146 & 8.160 MeV derived from Γ_α **Best+2013**
⇒ $S_\alpha(8.155 \text{ MeV}) = 0.15$ (present work)
- Doublet 7.980/7.982 MeV
Fit with 2 components → S_α of 7.98 MeV deduced using $\omega\gamma(\alpha, n)$ **Denker+94**
⇒ $S_\alpha(7.982 \text{ MeV}) = 0.005$ (present work)
- 7.815 MeV
→ Best χ^2 for $L_\alpha = 0, 1$ & good for $L_\alpha = 2$
→ $L_\alpha = 0 \rightarrow S_\alpha = 0.66$ (unlikely)

$$S_\alpha \rightarrow \Gamma_\alpha = 2P_l \frac{\hbar^2 R}{2\mu} S_\alpha |\phi(R)|^2$$

- Γ_α uncertainty: 3- 40% (stat), 35% (optical pot)

$^{17}\text{O}(\alpha,n)$ & $^{17}\text{O}(\alpha,\gamma)$ reaction rates $(\alpha,n)/(\alpha,\gamma)$ rate ratio

Rates calculations:

RateMC code **Longland+13**

□ For $E_r < 721$ keV & $E_r=807$ keV :
 → Γ_α (**present work**)

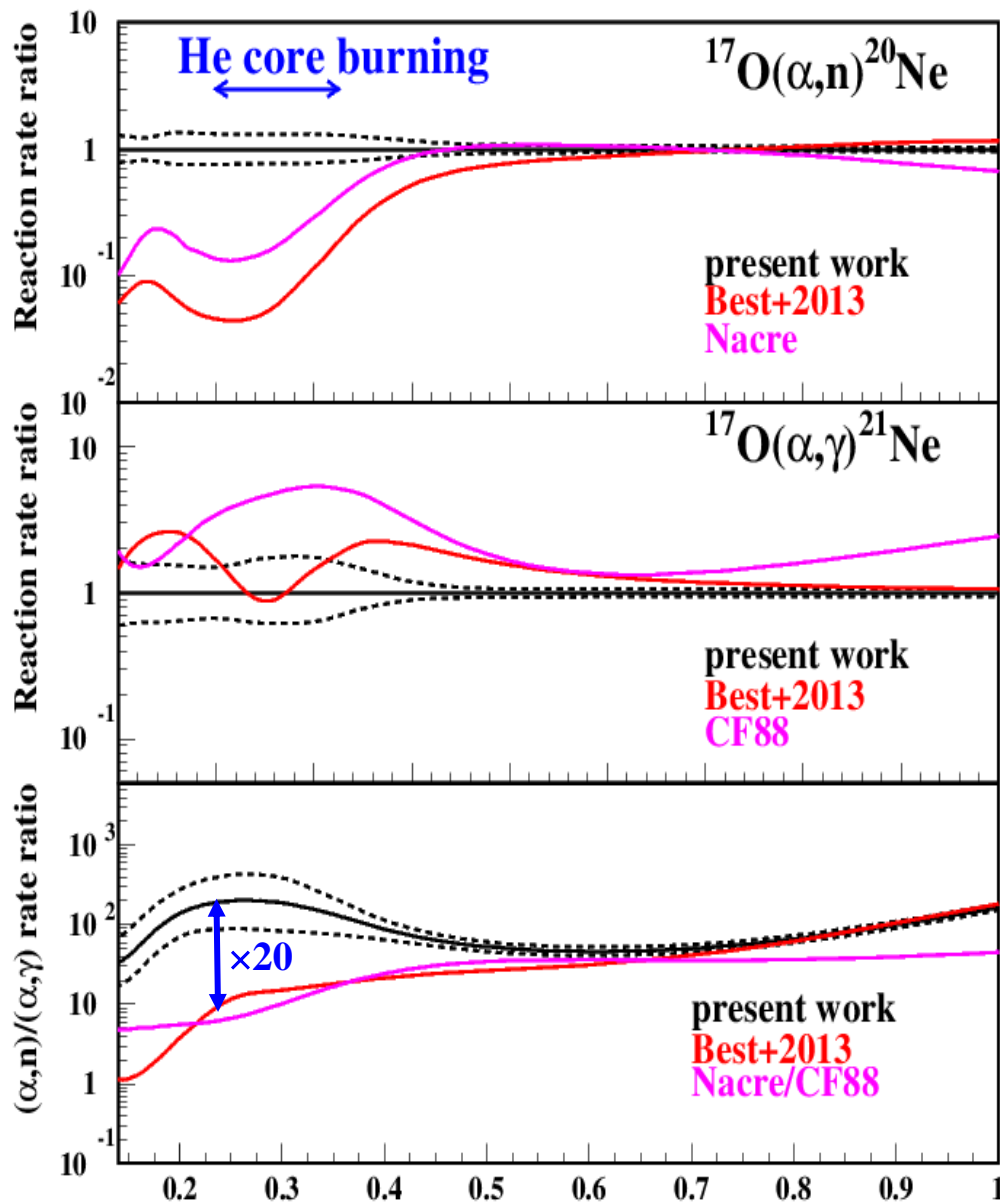
$\Gamma_\alpha(7.81\text{MeV})$ determined with $L_\alpha=1$
 $\Gamma_\alpha(7.74\text{MeV})$ determined with $L_\alpha=0$

→ Γ_n **Frost-Schenk+2022**

□ For $E_r \geq 721$ keV : Γ_α & Γ_n (**Best+2013** direct measurement)

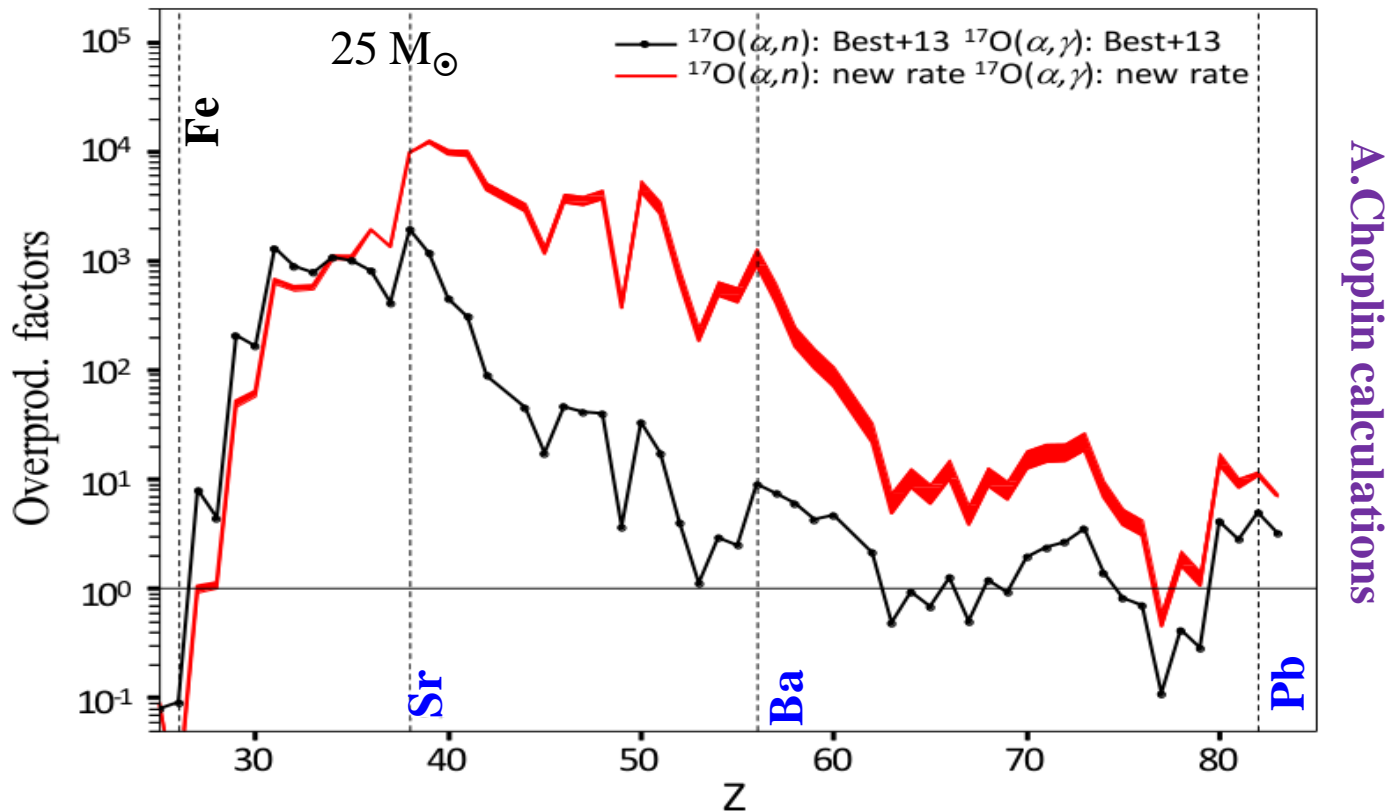
□ Γ_γ from:
 → systematics of $\langle\tau\rangle_{\text{meas}}$ (**Rolfs+72**)
 → $\omega\gamma(\alpha,\gamma)$ **Williams+2022** combined with present Γ_α & Γ_n (**Frost-Schenk+22**)

→ **Better neutron efficiency recycling** with a factor of about **20** with the **present recommended rates** than **Best+13** rates



Impact on the s-process in rotating poor-metal massive stars

- One-zone nucleosynthesis calculation mimicking the core He-burning phase of a low metallicity rotating massive star ($Z=0.001$)



→ **Large enhancement** (>1.5 dex) of elements $40 < Z < 60$ with the present **new rates** in comparison to **Best+13** rates

→ **Two order** of magnitude on **Barium**: largest effect

Collaboration

$^{12}\text{C}(^7\text{Li,t})^{16}\text{O}$ experiment

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L. Gaudefroy **(GANIL-Caen)**

$^{17}\text{O}(^7\text{Li,t})^{21}\text{Ne}$ experiment

F.H., S. Harrouz, N. de Séréville, A. Meyer
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(Ithemba)

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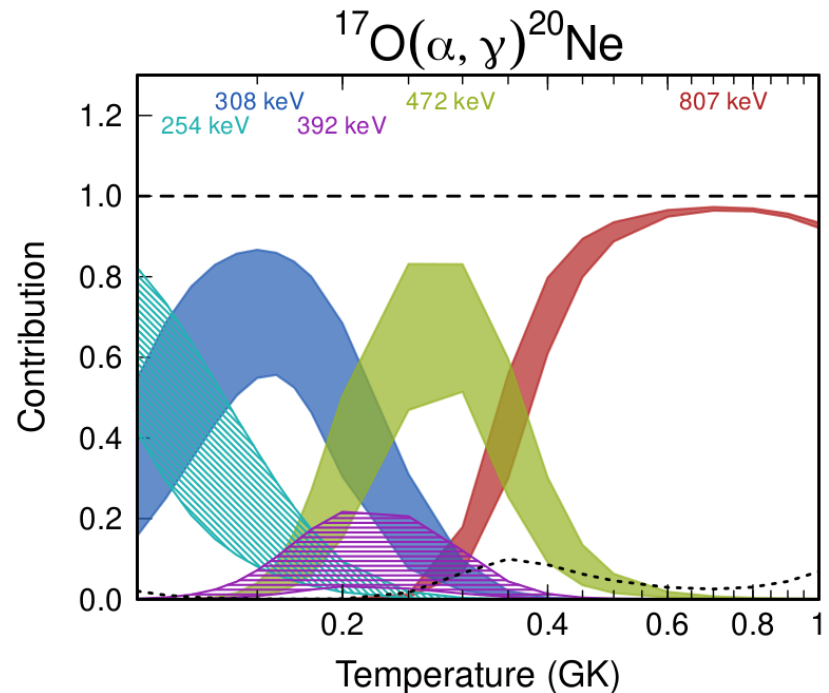
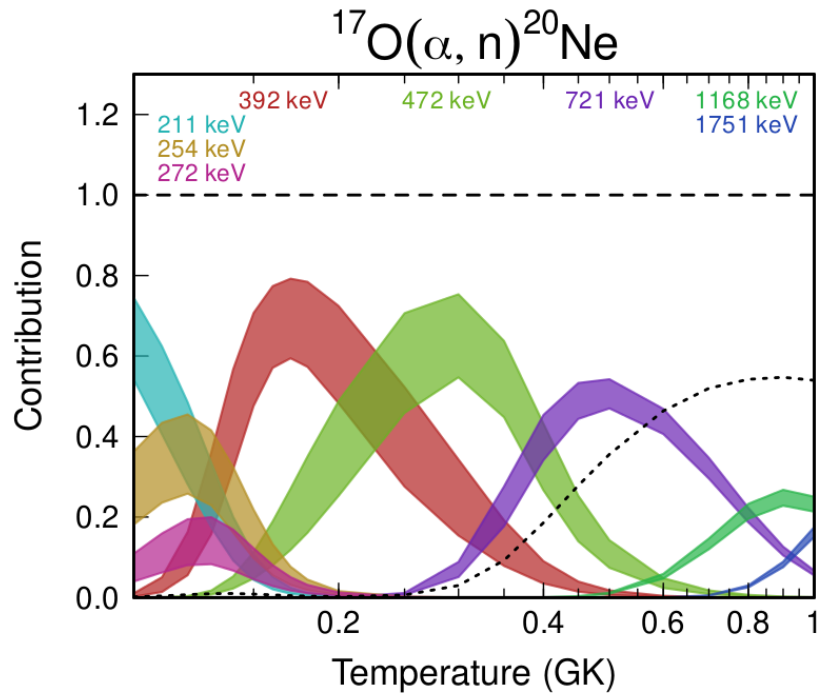
B. Bastin, F. De Oliveira, C. Fougères
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T. Faestermann, H.F Wirth, R. Hertenberger
(MLL)

S. Palmerini
(Perugia-university)

Thanks

Resonances contribution to the rates



- Er=392 (Ex=7.74 MeV) & 472 keV (Ex=7.82 MeV) contribute the most to the (α, n) rate
- Er=308 keV (Ex=7.655 MeV) & 472 keV (Ex=7.82 MeV) contribute the most to the (α, γ) rate

→ **Ex=7.74 MeV** unknown L_α & J^π

→ **Ex=7.82 MeV** $L_\alpha = 0, 1, 2$ & $L_n = 2, 3 \Rightarrow J^\pi = 5/2^+, 7/2^-, 3/2^+$

Key resonances

$^{17}\text{O}(\alpha,n)$ & $^{17}\text{O}(\alpha,\gamma)$ reaction rates $(\alpha,n)/(\alpha,\gamma)$ rate ratio

Worst case: 7.810 MeV $l_\alpha=2 \rightarrow 3/2^+$ or $7/2^+$ & no 7.74 MeV

