

# Intrinsic $k_T$ and soft gluons in Monte Carlo generators

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# Branching phase space

If using the DGLAP scheme with  $\alpha_s(\mu')$ , every branching is perturbative

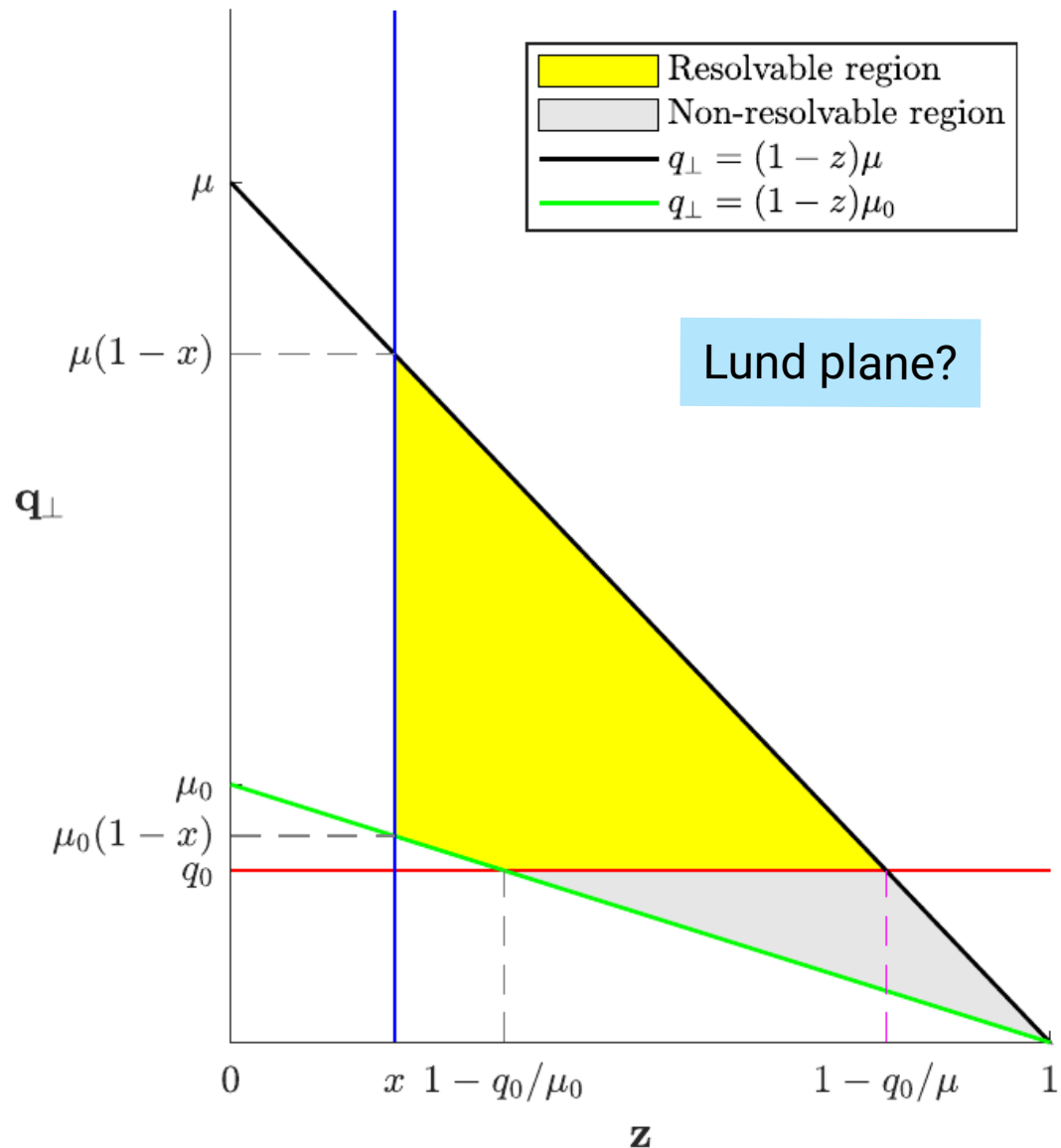
With angular ordering, we use

$$\alpha_s(q_T) = \alpha_s(\mu'^2(1-z)^2)$$

so in some regions of  $q_T$  this is may not be perturbative

Question:

Why not using the DGLAP scheme?



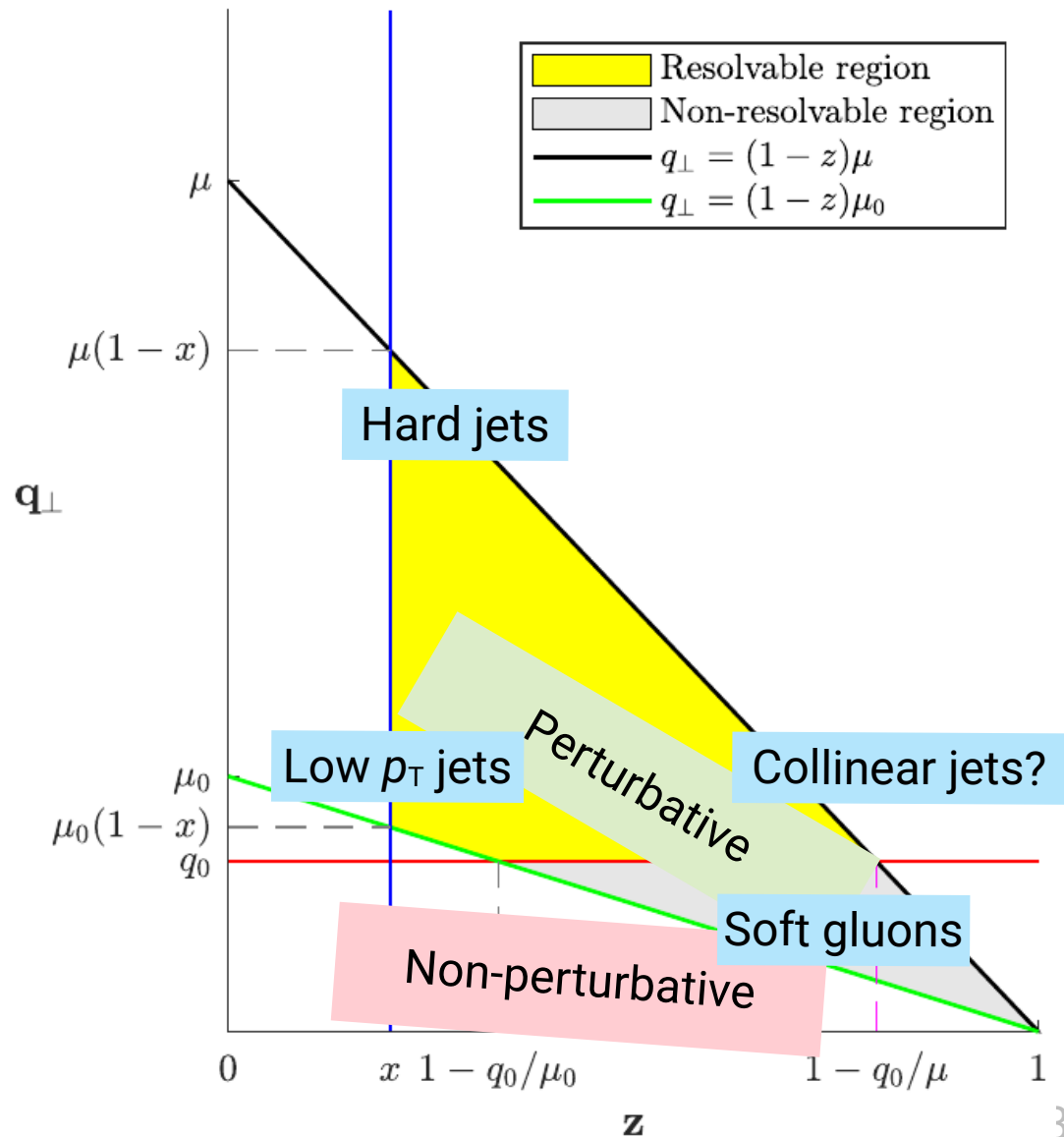
# Branching phase space

First things first...

There is a perturbative region defined by  $\mu > 1$  GeV (roughly)

Everything perturbative is part of the shower

Everything non-perturbative is free to be parameterized in the TMD ( $q_s$  etc)



## Traditional $z_{\max}$

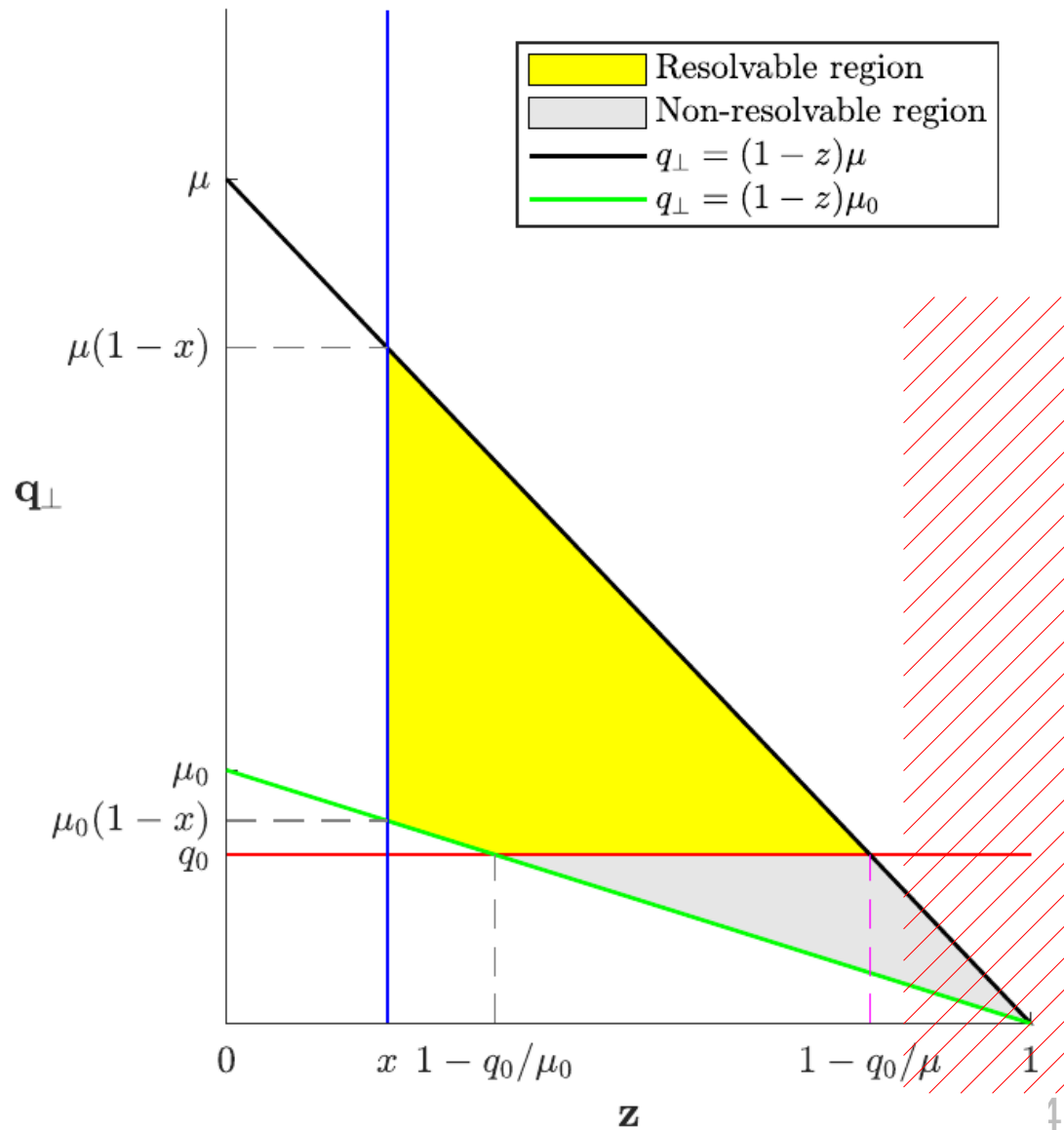
Traditional  $z_{\max}$  cuts off everything with  $1 - z < 10^{-3}$  or so

Questions:

Is this region fully neglected?

Included in a Sudakov?

Parameterized?



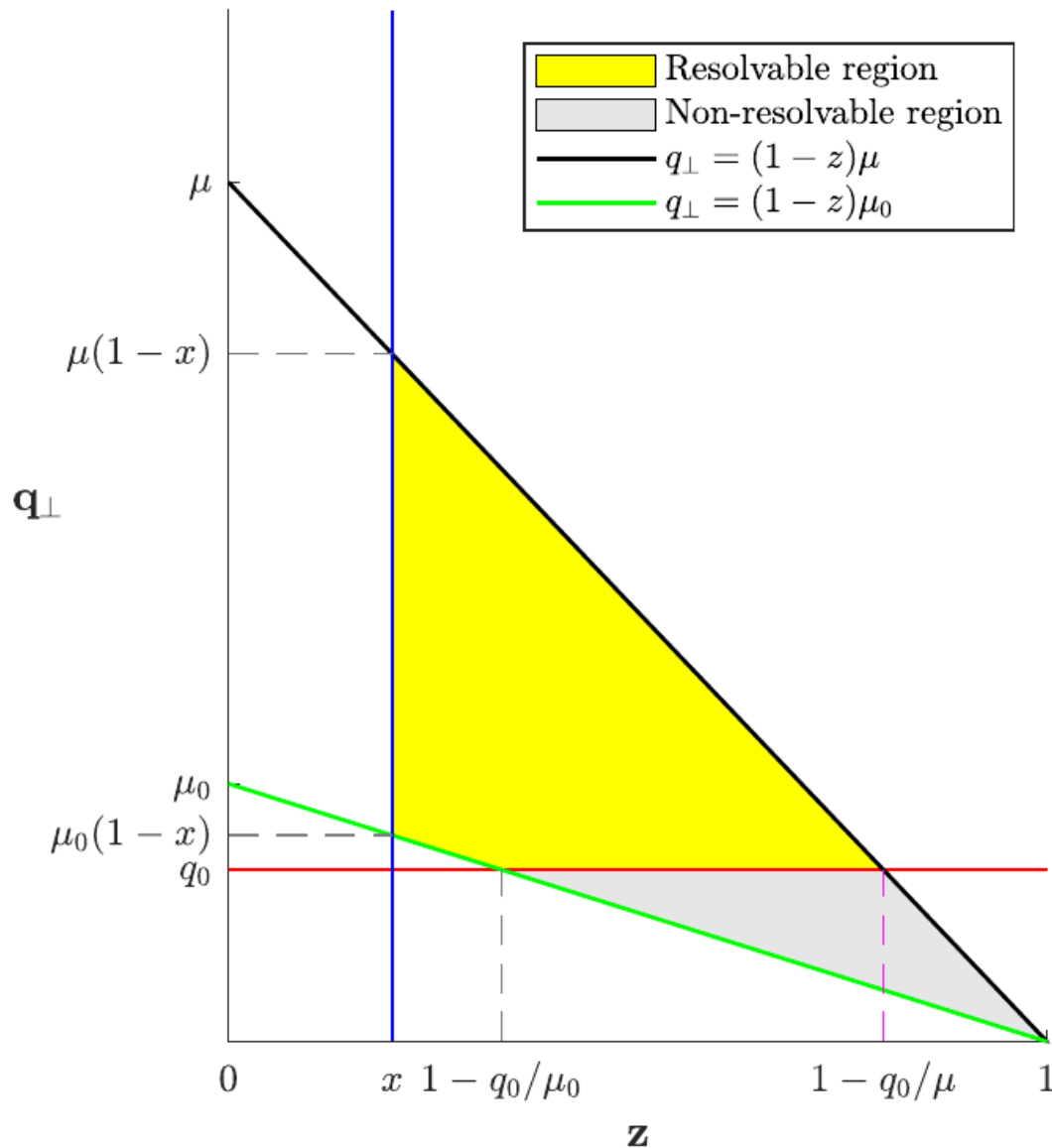
## Dynamic $z_{\max}$

Traditional  $z_{\max}$  cuts off everything with  $1 - z < 10^{-3}$  or so

Dynamic  $z_{\max}$  cuts off the grey area, because:

- $\alpha_s(q_T)$  is getting large (can also cap it to  $\alpha_s(q_0)$ )
- $q_T$  is too small for the gluon to be seen anyway (not resolvable)  $\simeq$  rapidity factorization in CSS

How do we handle the grey region?  
Move it to the TMD?



# Master formula

Sudakovs

$$A_a(x, \mathbf{k}, \mu^2) = \Delta_a(\mu^2, \mu_0^2) A_a(x, \mathbf{k}, \mu_0^2) \\ + \sum_b \int \frac{d^2 \boldsymbol{\mu}'}{\pi \mu'^2} \int^{z_{\max}} dz \mathcal{E}_{ab}[\Delta; P^{(R)}; \Theta] A_b(x/z, \mathbf{k} + a(z) \boldsymbol{\mu}', \mu'^2)$$

Where else does  $z_{\max}$  appear?