

# Perspectives for precision tests with antihydrogen

Michael Doser  
CERN

Summary of results of precision tests with Antihydrogen:

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- 1) Motivation for precision studies of antihydrogen
- 2) Status of formation of antihydrogen
- 3) Attempts at trapping antihydrogen
- 4) Attempts at forming a beam of Antihydrogen
- 5) Related atomic physics topics
- 6) Outlook

# Why do precision measurements with Antihydrogen?

1) Precise comparison between matter and antimatter

test of fundamental symmetry (CPT)

2) Measurement of the gravitational behavior of antimatter

test of the Weak Equivalence Principle

# The ultimate fundamental symmetry: CPT

- C - charge conjugation      particle  $\Leftrightarrow$  antiparticle
- P - parity (space inversion)
- T - time reversal
- Consequences : particles/antiparticles have
  - same masses, lifetimes, g-factors, |charge|, etc.
- CPT invariance is a mathematical theorem:
  - consequence of Lorentz-invariance
  - local interactions
  - unitarity
    - point-like particles
      - Lüders, Pauli, Bell and Jost, 1955
- QED, standard model quantum field theories are all CPT invariant
  - Assumptions are invalid in string theory, quantum gravity

although CPT is part of the “standard model”,  
the SM can be extended to allow CPT violation

### *CPT* violation and the standard model

Phys. Rev. D 55, 6760–6774 (1997)

Don Colladay and V. Alan Kostelecký  
Department of Physics, Indiana University, Bloomington, Indiana 47405  
(Received 22 January 1997)

Modified Dirac eq. in SME

$$(i\gamma^\mu D_\mu - m_e - a_\mu^e \gamma^\mu - b_\mu^e \gamma_5 \gamma^\mu - \frac{1}{2} H_{\mu\nu}^e \sigma^{\mu\nu} + ic_{\mu\nu}^e \gamma^\mu D^\nu + id_{\mu\nu}^e \gamma_5 \gamma^\mu D^\nu) \psi = 0.$$

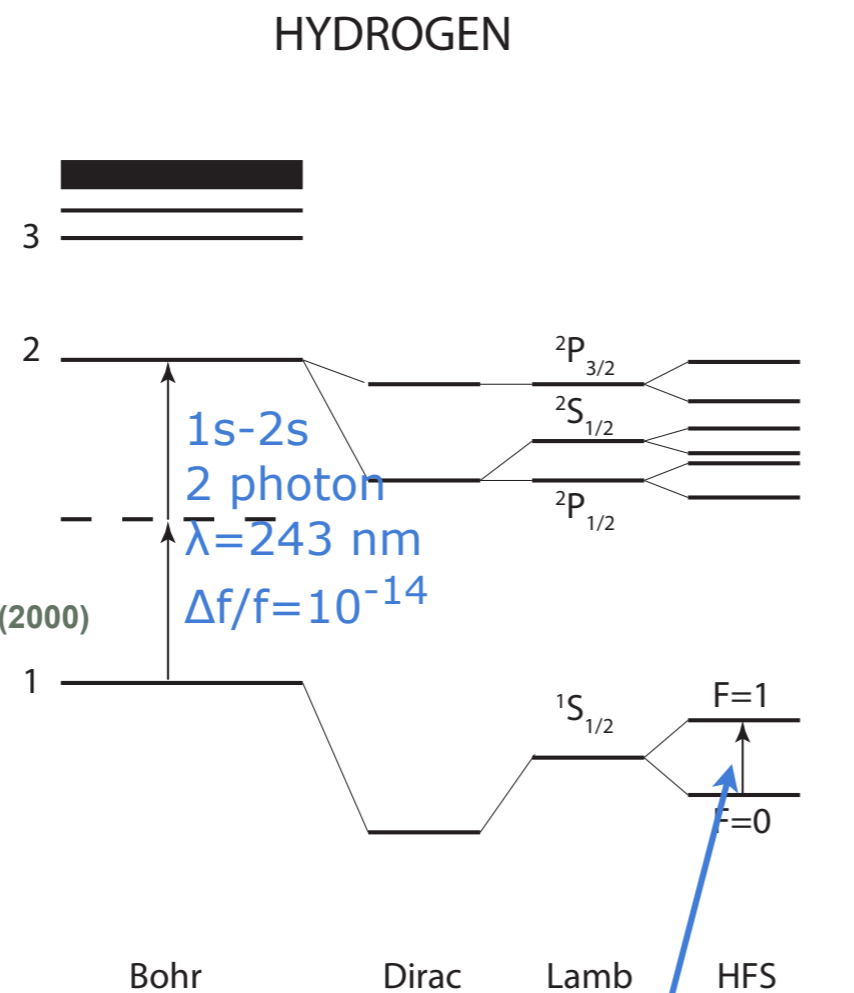
CPT & Lorentz violation

Lorentz violation

- Spontaneous Lorentz symmetry breaking by (exotic) string vacua
- Note: if there is a preferred frame, sidereal variation due to Earth's rotation might be detectable

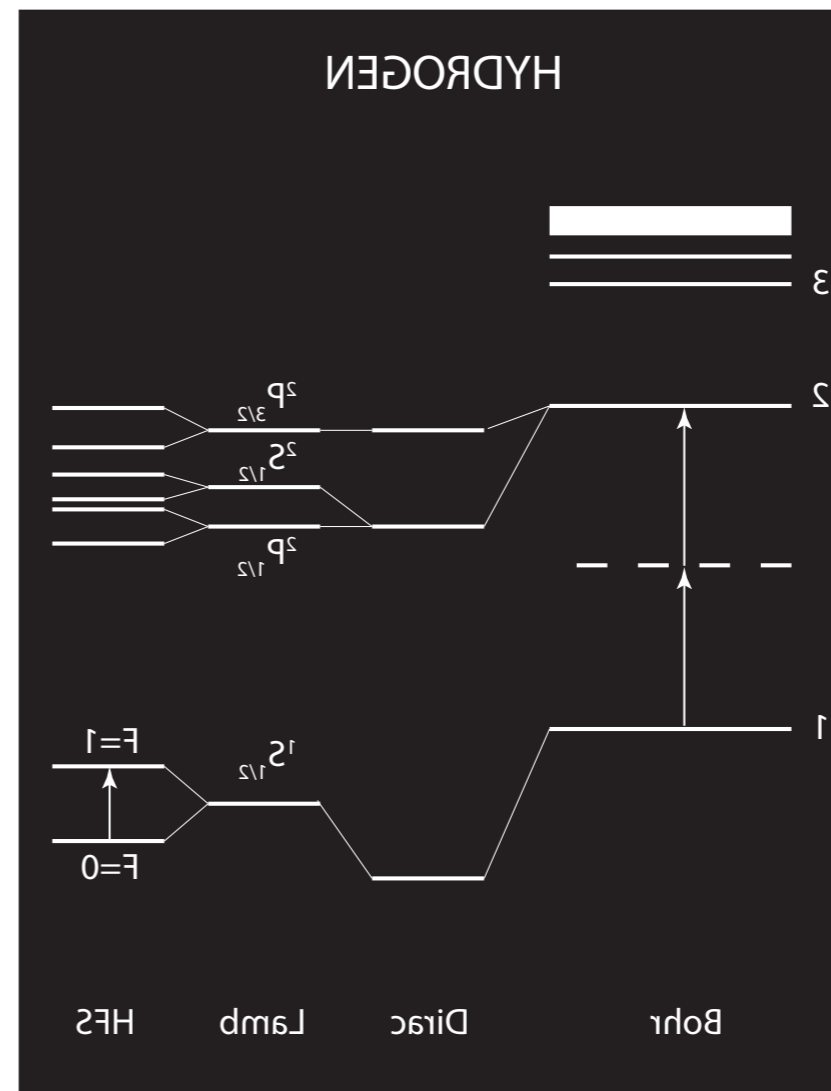
# Goal of comparative spectroscopy: test CPT symmetry

## Hydrogen and Antihydrogen



T. Hänsch et al.,  
Phys. Rev. Lett. 84, 5496–5499 (2000)

N. F. Ramsey,  
Physica Scripta T59, 323 (1995)



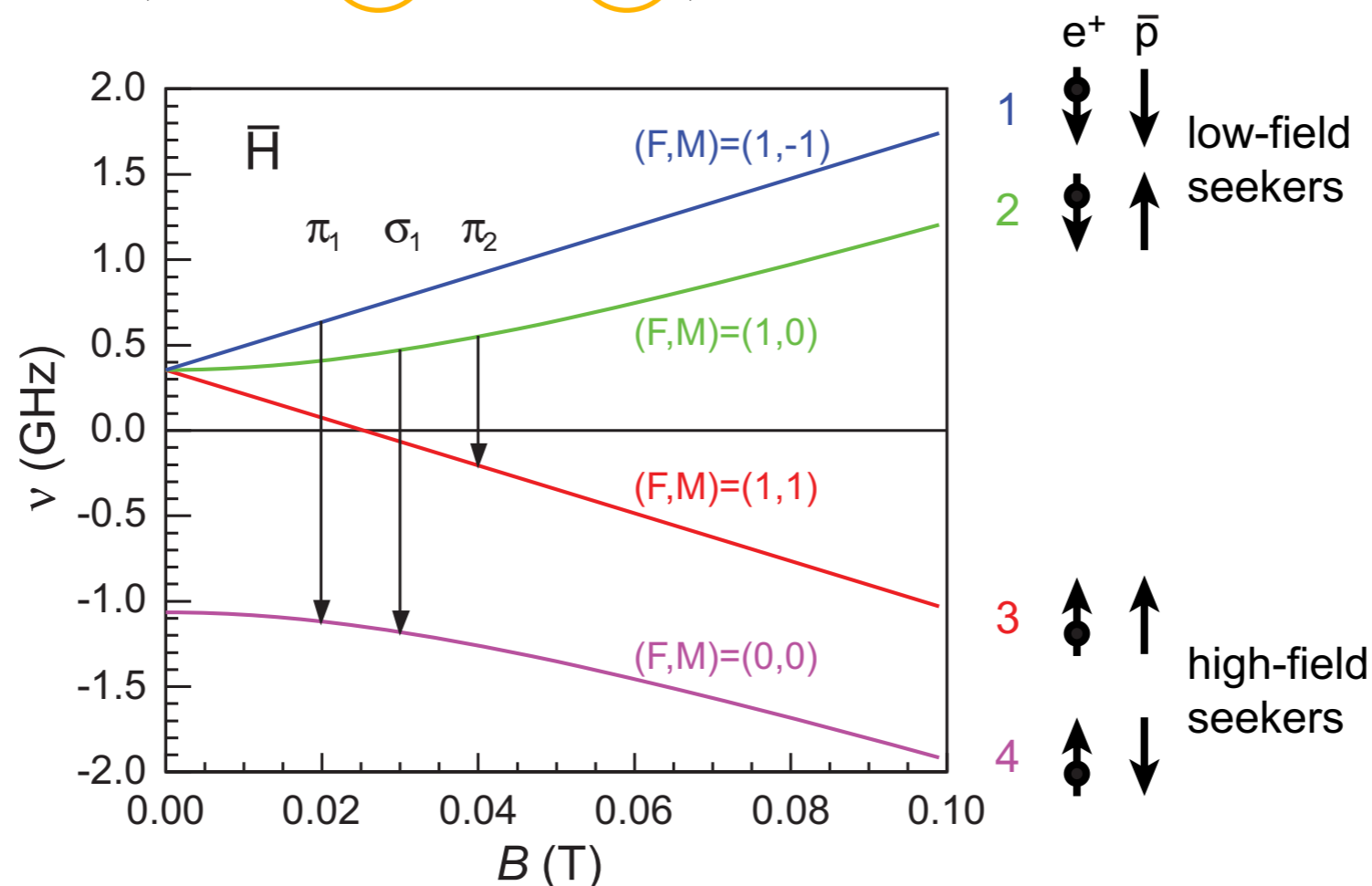
# HFS, CPT and SME

$$\nu_{\text{HFS}} = \frac{16}{3} \left( \frac{m_p}{m_p + m_e} \right)^3 \frac{m_e \mu_p}{m_p \mu_N} \alpha^2 c R_\infty (1 + \Delta) \quad \mu_{\bar{p}} \text{ only known to 0.3\%}$$

$$\begin{aligned} \Delta E^{\text{H}}(m_J, m_I) = & a_0^e + a_0^p - c_{00}^e m_e - c_{00}^p m_p \\ & + (-b_3^e + d_{30}^e m_e + H_{12}^e) m_J / |m_J| \\ & + (-b_3^p + d_{30}^p m_p + H_{12}^p) m_I / |m_I|, \end{aligned}$$

Bluhm, R., Kostelecký, V.A., Russell, N.: Phys. Rev. Lett. **82**, 2254 (1999)

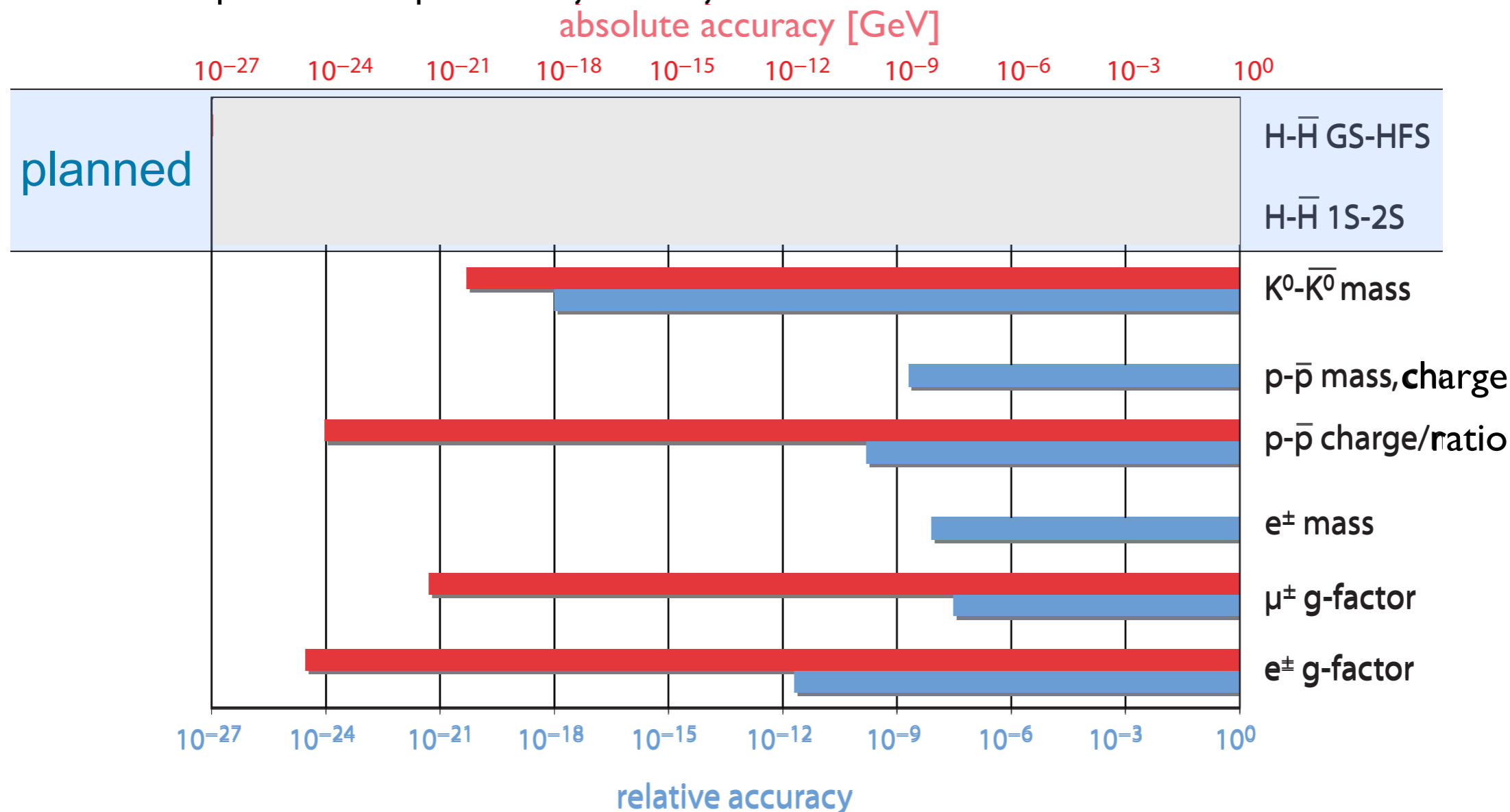
Transitions between HF levels are sensitive to CPTV, but not  $1s \rightarrow 2s$





# Verifications of CPT symmetry

Tests of particle/antiparticle symmetry (PDG)



Inconsistent definition of figure of merit: comparison difficult

Pattern of CPT violation unknown (P: weak interaction; CP: mesons)

Absolute energy scale: standard model extension (Kostelecky)

# Motivation

- General relativity is a classical (non quantum) theory;
- EEP violations may appear in some quantum theory
- New quantum scalar and vector fields are allowed in some models (Kaluza Klein ....)

Einstein field: tensor graviton (Spin 2, “Newtonian”)  
 + Gravi-vector (spin 1)  
 + Gravi-scalar (spin 0)

- These fields may mediate interactions violating the equivalence principle

M. Nieto and T. Goldman, Phys. Rep. 205, 5 221-281,(1992)

Scalar: “charge” of particle equal to “charge of antiparticle” : **attractive force**

Vector: “charge” of particle opposite to “charge of antiparticle”: **repulsive/attractive force**

$$V = - \frac{G_{\infty}}{r} m_1 m_2 \left( 1 \mp a e^{-r/v} + b e^{-r/s} \right) \quad \text{Phys. Rev. D 33 (2475) (1986)}$$

Cancellation effects in matter experiment if  $a \approx b$  and  $v \approx s$

# The reality

## Making Antihydrogen

### Plan A:

Trapping Antihydrogen

Cooling Antihydrogen

Boundary conditions (magnetic field, limited solid angle, \*low\* numbers of particles)

### Plan B:

Atomic beam

# Principle of antihydrogen production

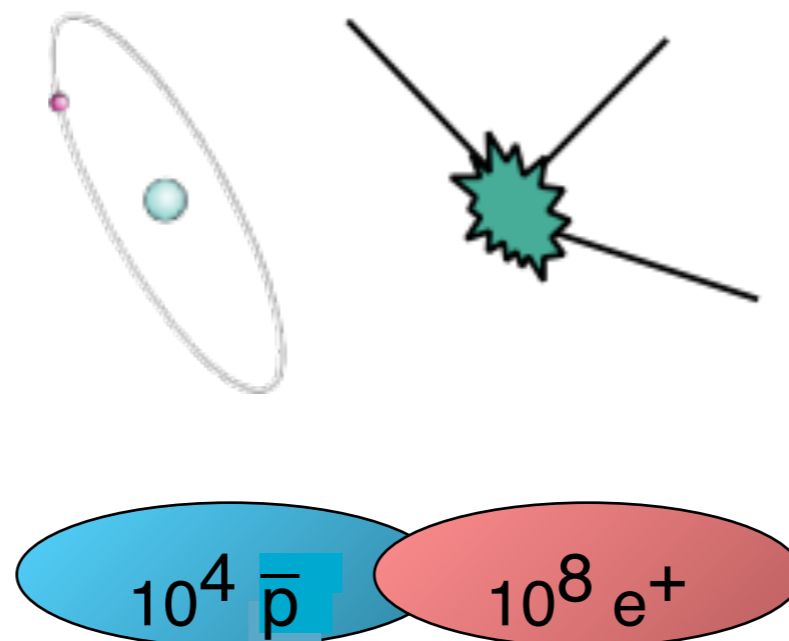
## Antiprotons

Production GeV

Deceleration MeV

Trapping keV

Cooling meV



## Positrons

Production MeV

Moderation

Accumulation eV

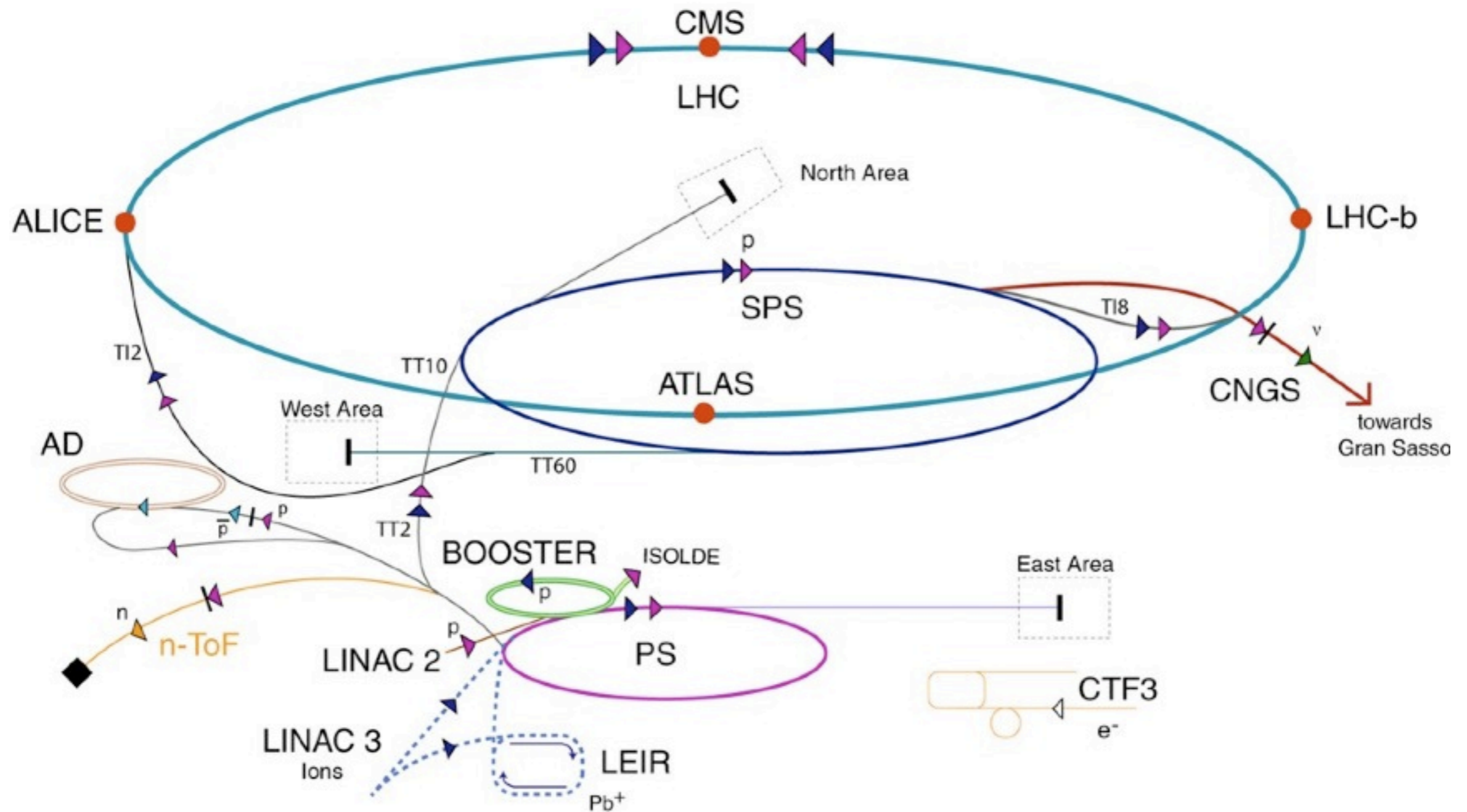
Mixing trap:

mixing and manipulation

## Antihydrogen formation

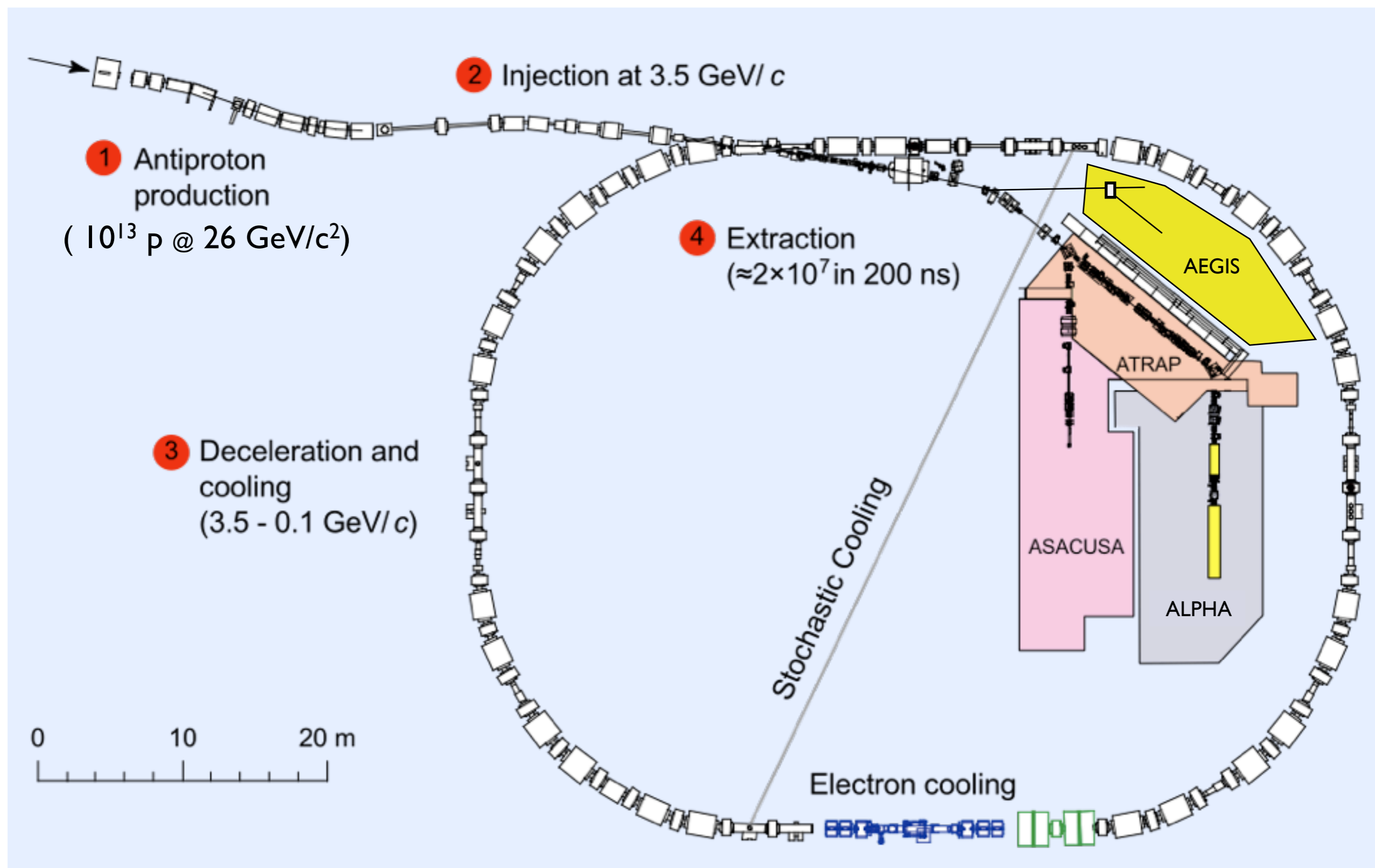
Detection of annihilation

# CERN Accelerator Complex



- |            |               |                              |                                |
|------------|---------------|------------------------------|--------------------------------|
| ▶ protons  | ▶ antiprotons | AD Antiproton Decelerator    | LHC Large Hadron Collider      |
| ▶ ions     | ▶ electrons   | PS Proton Synchrotron        | n-ToF Neutron Time of Flight   |
| ▶ neutrons | ▶ neutrinos   | SPS Super Proton Synchrotron | CNGS CERN Neutrinos Gran Sasso |
|            |               |                              | CTF3 CLIC Test Facility 3      |

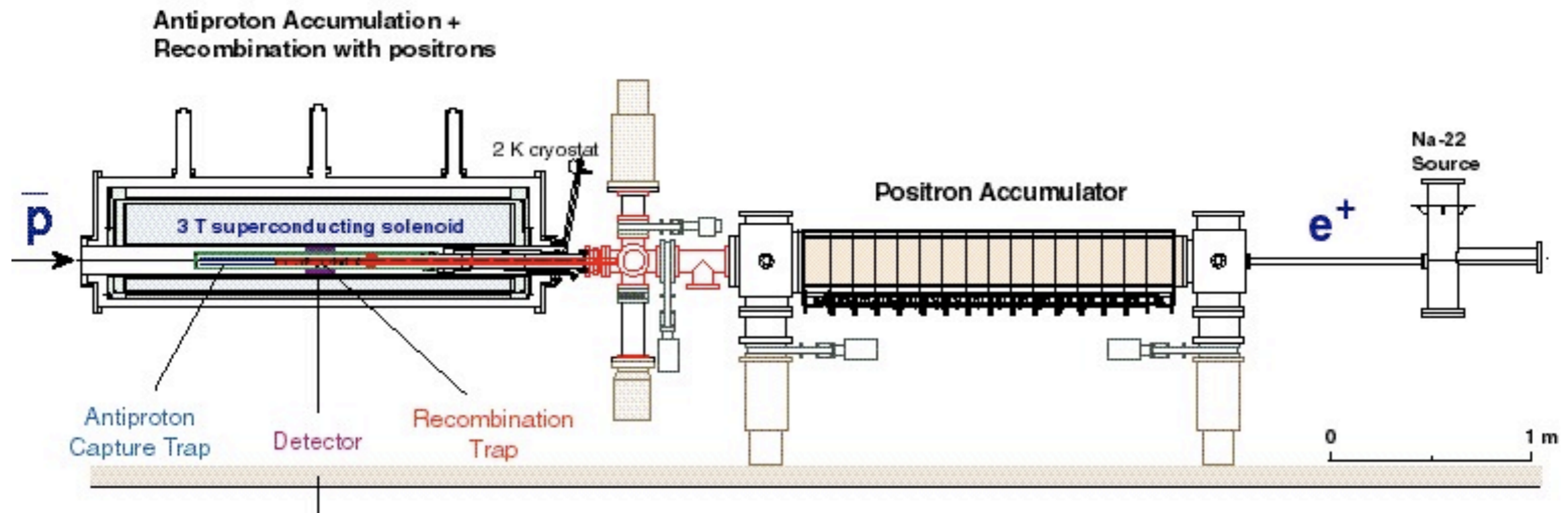
# Antiproton decelerator

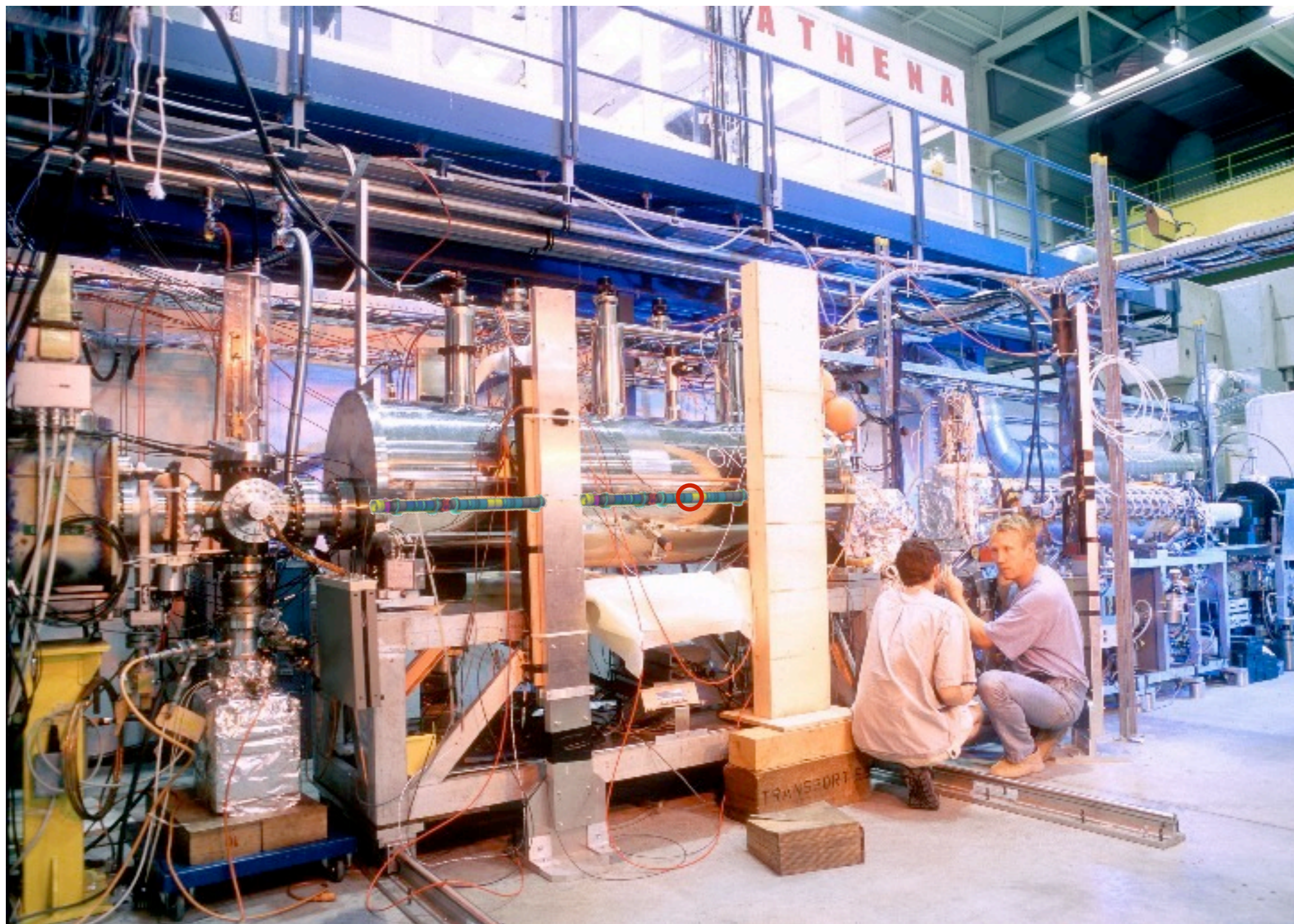


# Typical Antihydrogen Experiment

- Capture, trap, cool antiprotons  $10^7$  (AD)  $\rightsquigarrow 10^5$  (trapped)
- Capture, trap, cool positrons  $1.5 \text{ GBq } ^{22}\text{Na} \rightsquigarrow 10^8$  (trapped)
- Merge and recombine  $1\text{-}10^3 \text{ Hz}$

## ATHENA / AD-1 : Antihydrogen Production and Spectroscopy

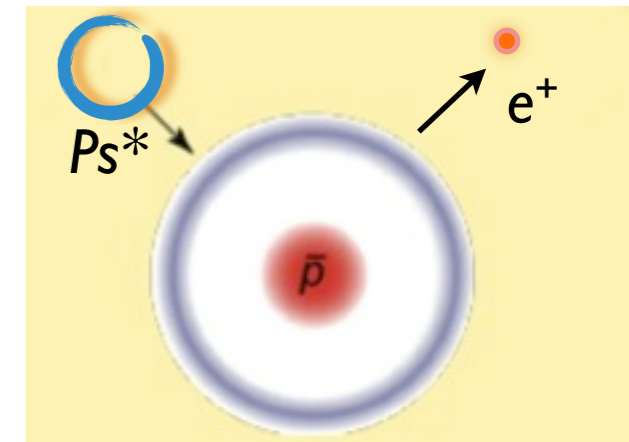
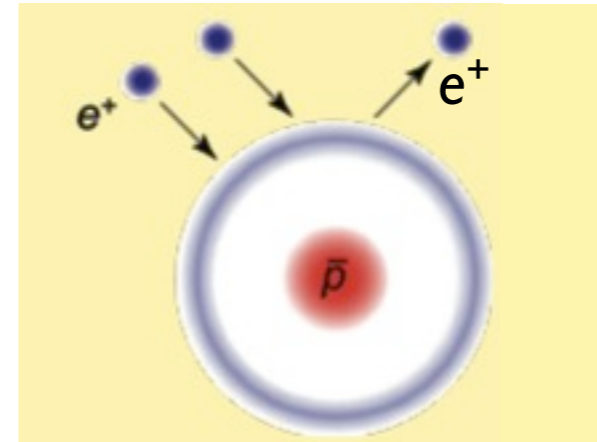
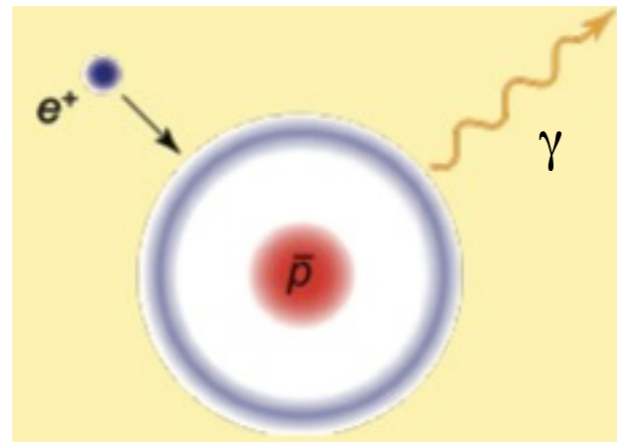






## Recombination processes

Principle



Temperature dependence

$$\propto T^{-2/3}$$

$$\propto T^{-2/3}$$

$$\propto T^{-x}$$

e<sup>+</sup> density dependence

$$\propto n_e$$

$$\propto n_e^2$$

Cross section at 1K

$$10^{-16} \text{ cm}^2$$

$$10^{-7} \text{ cm}^2$$

$$10^{-9} \text{ cm}^2$$

Final internal states

$$n < 10$$

$$n \gg 10$$

$$f(n_{Ps})$$

Expected rates

few Hz

high

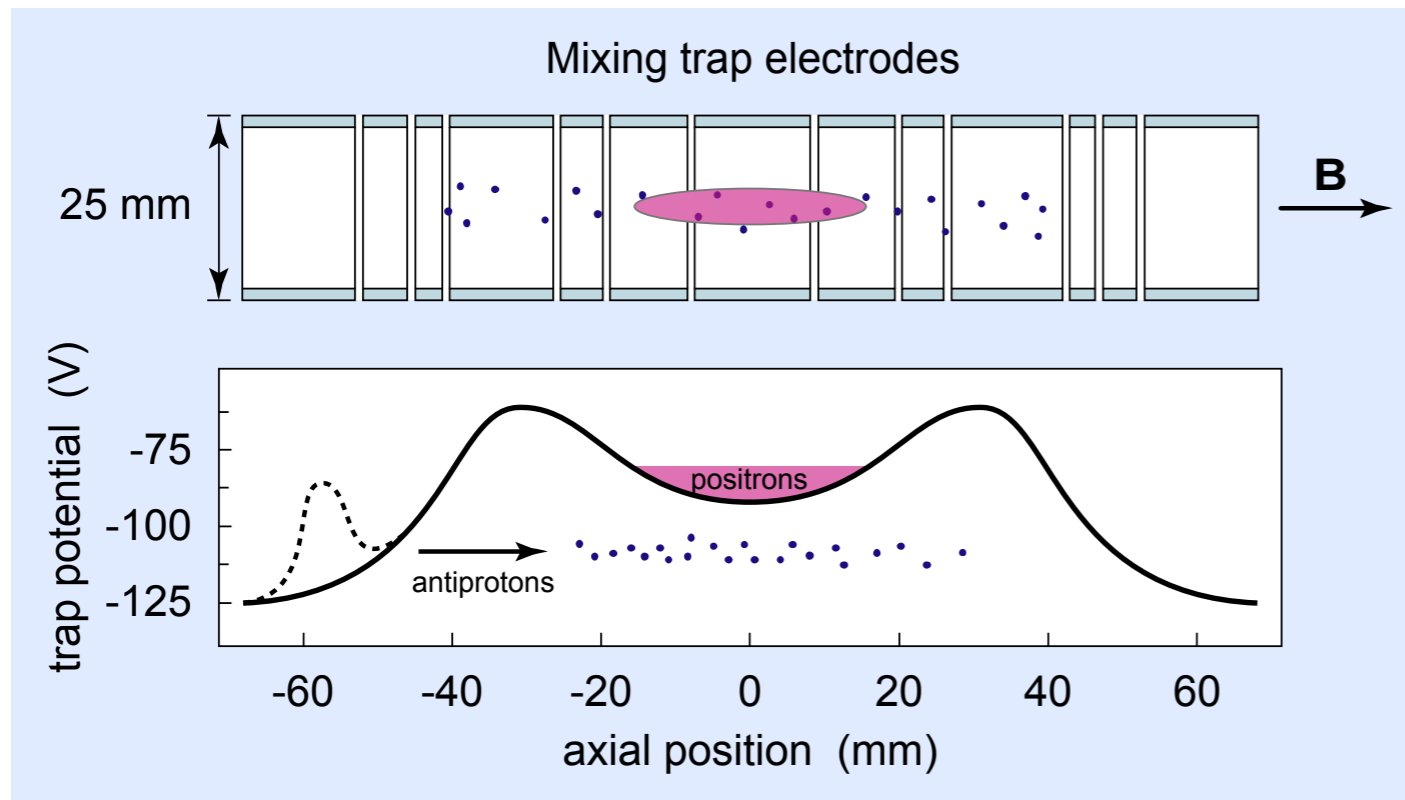
1 Hz (?)

but: B, interactions in e<sup>+</sup> plasma can't be neglected!

# Antihydrogen production (I)

Formation

Nested-well technique: Penning trap for  $\bar{p}$ ,  $e^+$  :  $B=IT$  (plasma stability)



ATHENA

$$e^+ \quad N \approx 5 \times 10^7 \quad n \approx 2 \times 10^8 \text{ cm}^{-3}$$

$$\bar{p} \quad N \approx 10^4$$

ATRAP

$$e^+ \quad N \approx 2 \times 10^6$$

$$\bar{p} \quad N \approx 10^5$$

[G. Gabrielse *et al.*,  
Phys. Lett. A **129** (1988) 38]

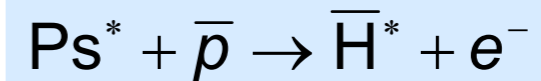
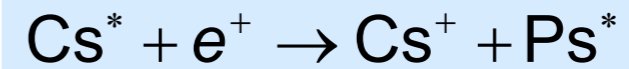
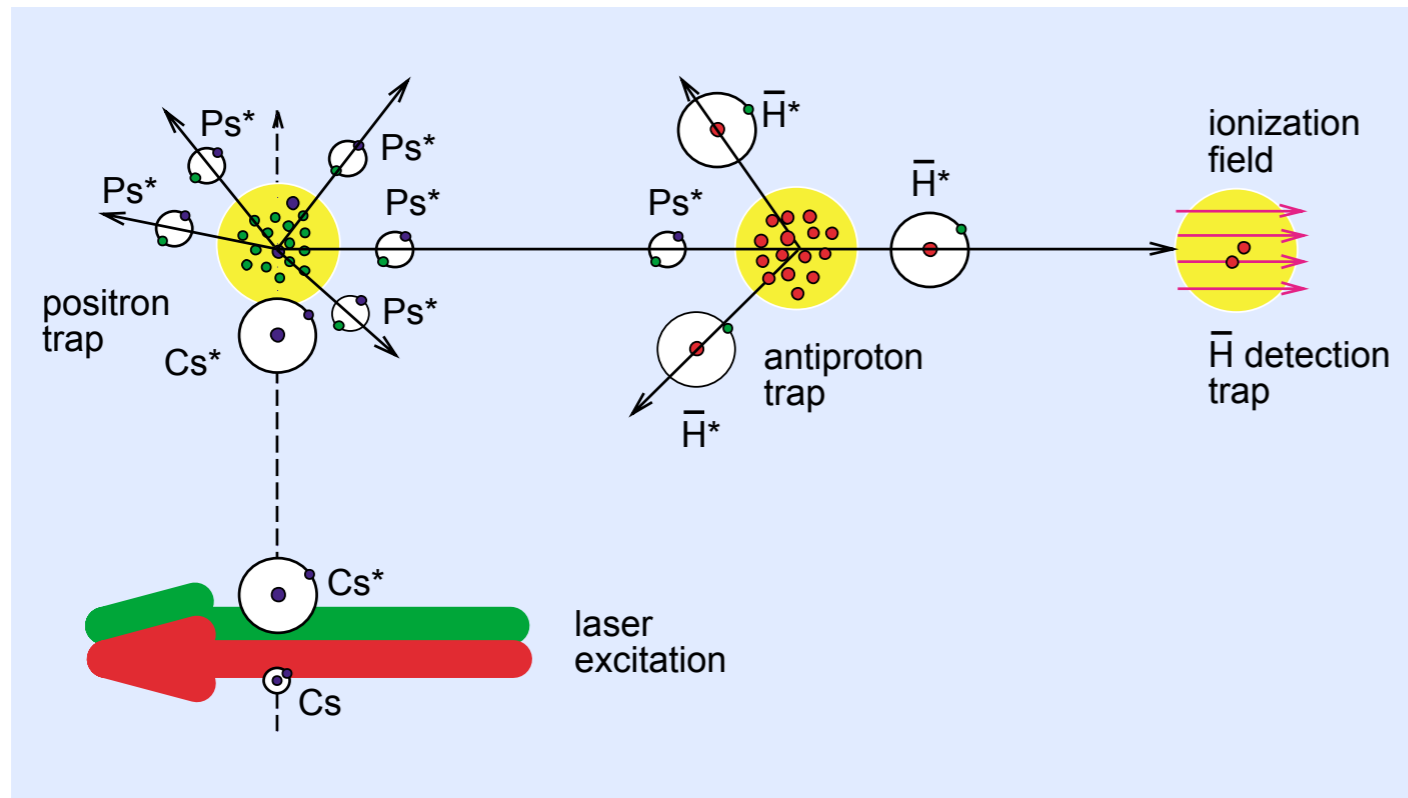
- Positrons cool by emission of synchrotron radiation
- Antiprotons launched into pre-cooled positrons
- $\bar{H}$  production sets in spontaneously at high rates
- Disadvantage:

plasma temperature, re-ionization, high-n states

[G. Gabrielse *et al.*, Phys. Rev. Lett. **93** (2004) 073401;  
N. Madsen *et al.* (ATHENA), Phys. Rev. Lett. **94** (2005) 033403]

# Antihydrogen production (II)

## Cesium charge exchange technique:



### ATRAP

$$e^+ \quad N \approx 1.4 \times 10^6$$

$$\bar{p} \quad N \approx 2.4 \times 10^5$$

densities not given

[C. Storry *et al.* (ATRAP),  
Phys. Rev. Lett. **93** (2004) 263401]

- Two-stage resonant charge exchange
- $\bar{\text{H}}$  produced at well-defined quantum state and (presumably) at the temperature of  $\bar{p}$  prior to recombination
- Disadvantage:

Small solid angle  $\Rightarrow$  low rates

# First “Cold” Antihydrogen 2002 @ AD

advance online publication

## Production and detection of cold antihydrogen atoms

M. Amoretti<sup>\*</sup>, C. Anslert<sup>†</sup>, G. Bonomi<sup>‡§</sup>, A. Bouchta<sup>‡</sup>, P. Bowe<sup>||</sup>, C. Carraro<sup>†</sup>, C. L. Cesar<sup>¶</sup>, M. Charlton<sup>‡</sup>, M. J. T. Collier<sup>‡</sup>, M. Doser<sup>‡</sup>, V. Filippini<sup>⊙</sup>, K. S. Fine<sup>‡</sup>, A. Fontana<sup>⊙\*\*</sup>, M. C. Fujiwara<sup>††</sup>, R. Funakoshi<sup>††</sup>, P. Genova<sup>⊙\*\*</sup>, J. S. Hangst<sup>||</sup>, R. S. Hayano<sup>††</sup>, M. H. Holzscheller<sup>‡</sup>, L. V. Jorgensen<sup>‡</sup>, V. Lagomarsino<sup>††‡</sup>, R. Landua<sup>‡</sup>, D. Lindelöf<sup>†</sup>, E. Lodi Rizzini<sup>⊙</sup>, M. Macri<sup>†</sup>, N. Madsen<sup>†</sup>, G. Manuzio<sup>††‡</sup>, M. Marchesotti<sup>⊙</sup>, P. Montagna<sup>⊙\*\*</sup>, H. Pruys<sup>†</sup>, C. Regenfus<sup>†</sup>, P. Riedler<sup>‡</sup>, J. Rochet<sup>†‡</sup>, A. Rotondi<sup>⊙\*\*</sup>, G. Rouleau<sup>‡‡</sup>, G. Testera<sup>†</sup>, A. Variola<sup>†</sup>, T. L. Watson<sup>‡</sup> & D. P. van der Werf<sup>‡</sup>

ATHENA  
Nature 419  
(2002) 456

VOLUME 89, NUMBER 21

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## Background-Free Observation of Cold Antihydrogen with Field-Ionization Analysis of Its States

G. Gabrielse,<sup>1,\*</sup> N.S. Bowden,<sup>1</sup> P. Oxley,<sup>1</sup> A. Speck,<sup>1</sup> C.H. Storry,<sup>1</sup> J.N. Tan,<sup>1</sup> M. Wessels,<sup>1</sup> D. Grzonka,<sup>2</sup> W. Oelert,<sup>2</sup> G. Schepers,<sup>2</sup> T. Seifick,<sup>2</sup> J. Walz,<sup>3</sup> H. Pittner,<sup>4</sup> T.W. Hänsch,<sup>4,5</sup> and E. A. Hessels<sup>6</sup>

(ATRAP Collaboration)

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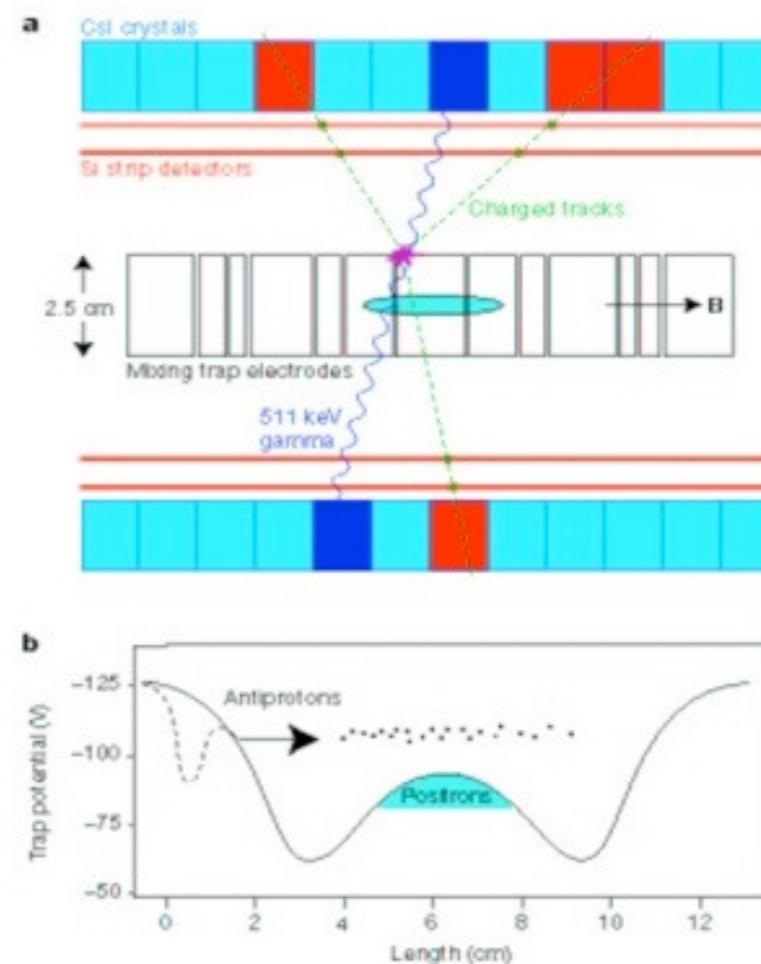
<sup>5</sup>Ludwig-Maximilians-Universität München, Schellingstrasse 4/III, 80799 München, Germany

<sup>6</sup>York University, Department of Physics and Astronomy, Toronto, Ontario, Canada M3J 1P3

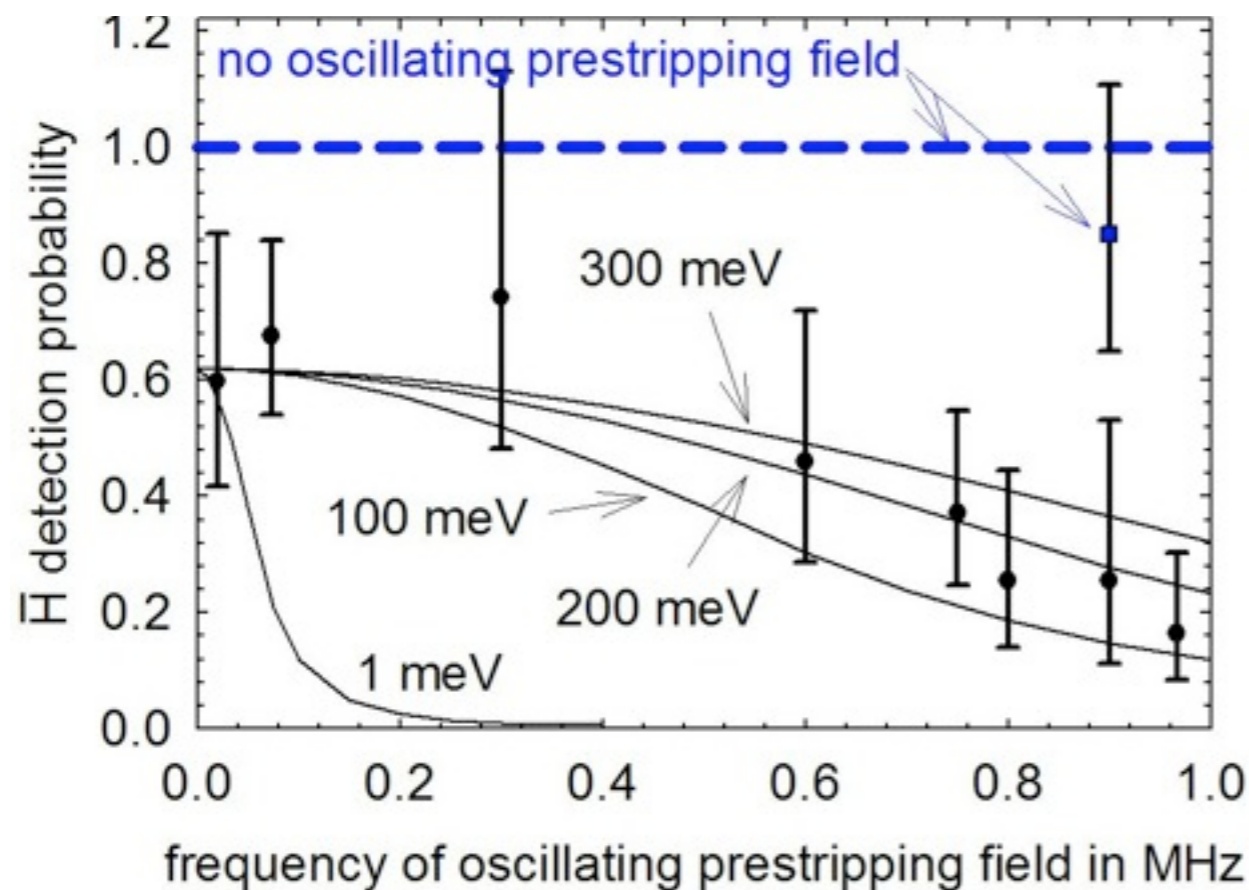
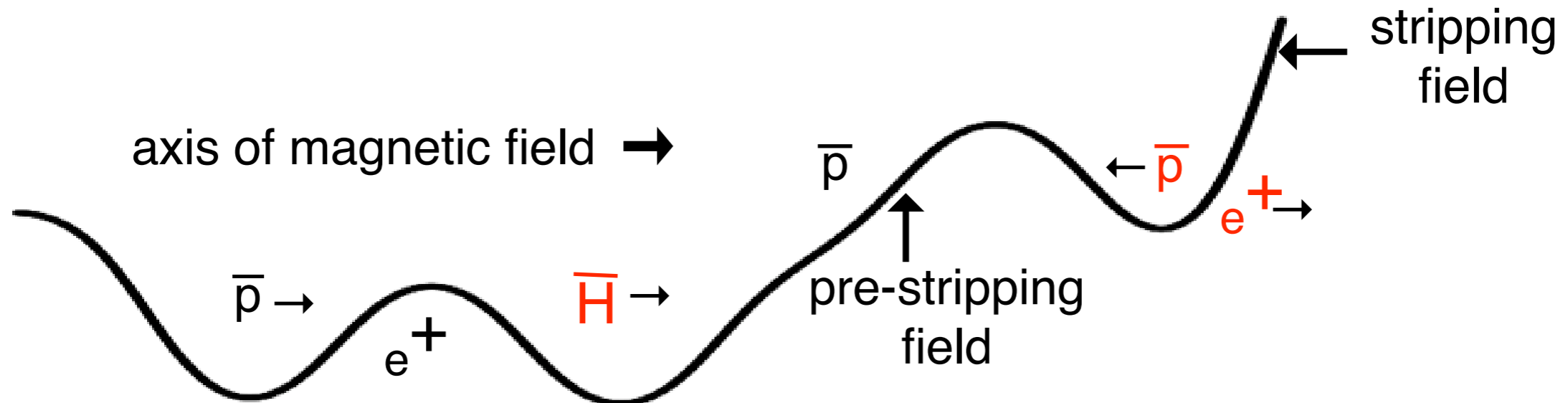
(Received 11 October 2002; published 31 October 2002)

ATRAP PRL 89 (2002) 213401

Nested Penning traps  
Capture energy: few keV



# Temperature of produced $\bar{H}$



Fraught with uncertainty: collisions, plasma temperature, selectivity to lightly bound states, lack of control on initial conditions...

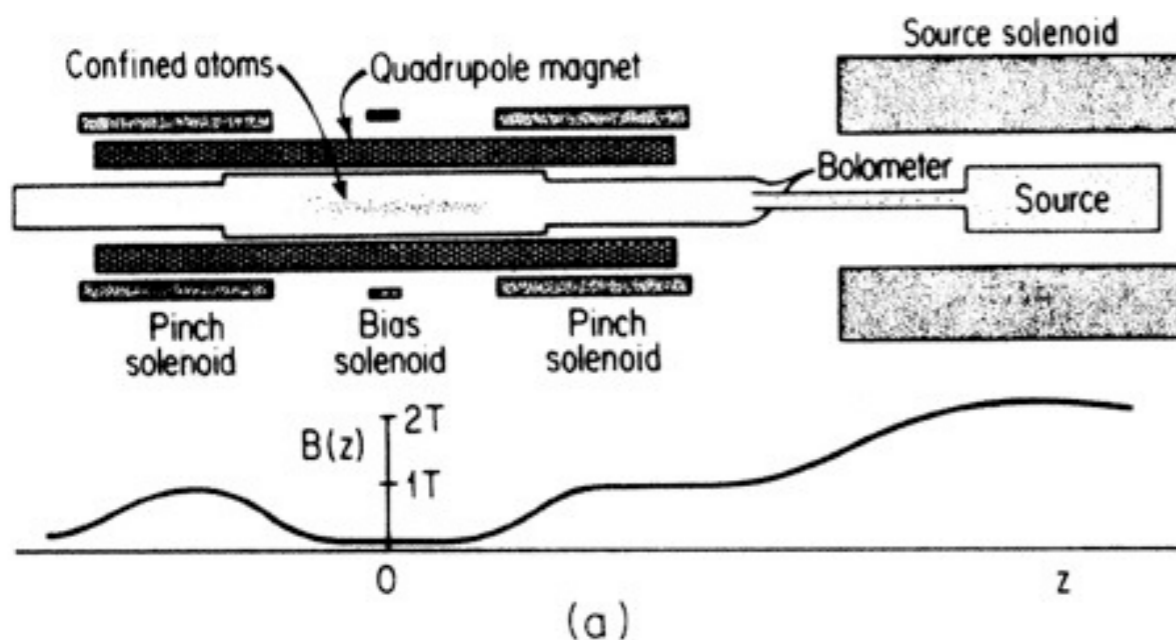
**BUT**

4.2 K  $\bar{H} \sim 0.3$  meV

# Trapping of $\bar{H}$ ?

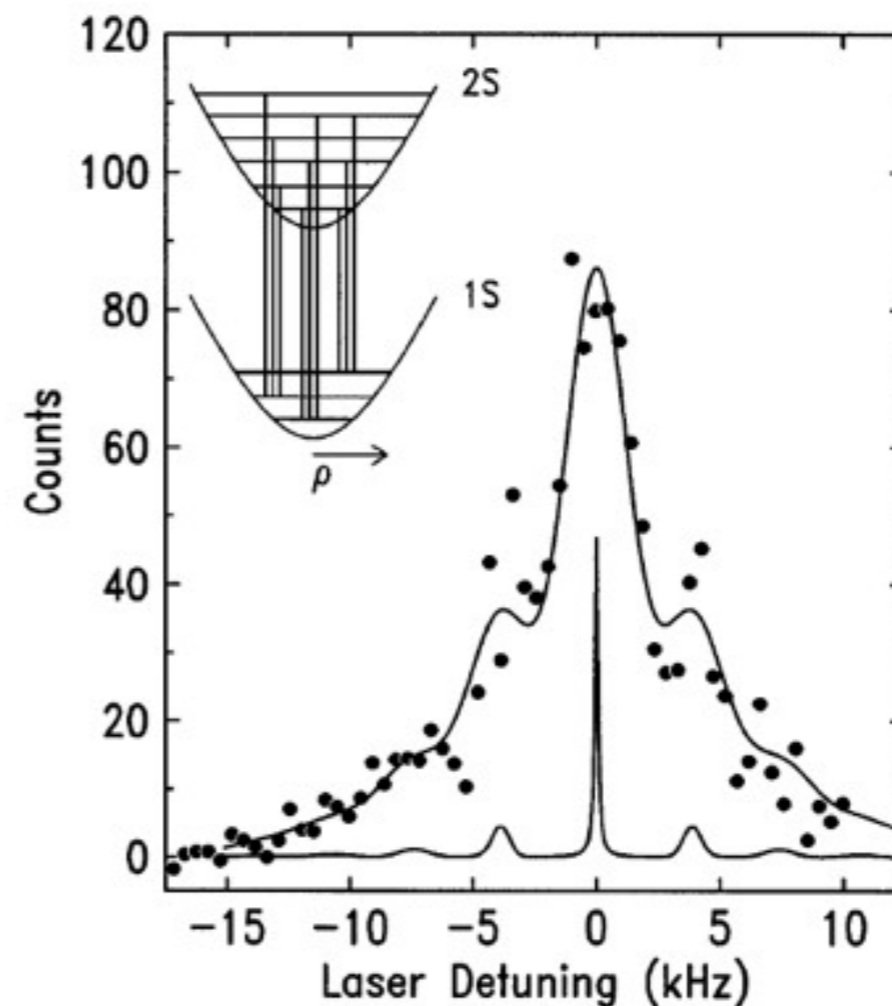
## Trapping

- Force of magnetic field gradient on magnetic moment of atom
- “depth” typically  $< 1$  K  
( $50 \mu\text{eV}$ )
- Constant holding-field  $B_{z,0}$  to avoid spin flips
- Typical configuration:



- Trapped hydrogen C. Cesar et al., Phys. Rev. Lett. 77, 255 (1996)

$10^{13} - 10^{10}$  atoms at 25 mK to 100  $\mu\text{K}$   
 $B_{z,0} = 2 \times 10^{-4} \text{ T}$



$\bar{H}$ : Confine both *charged plasmas* and *neutral atoms without heating* them

- Preserve cylindrical symmetry (plasma confinement)
- Magnetic field minimal in center (atom confinement)
- Antihydrogen **must be formed inside its trap**

# Challenges to trapping of produced $\bar{H}$

temperature considerations:

- $\bar{p}$  cooling: typically cooled via electrons, but electrons can ionize produced  $\bar{H}$ ; however,  $e^-$  kick-out heats antiprotons
  - ⇒ cooling of  $\bar{p}$  ?
- $e^+$  cooling: high density ⇒ plasma regime ⇒ high angular momentum ⇒ strong radial compression needed!
- temperature of  $\bar{H}$ : depends on formation mechanism

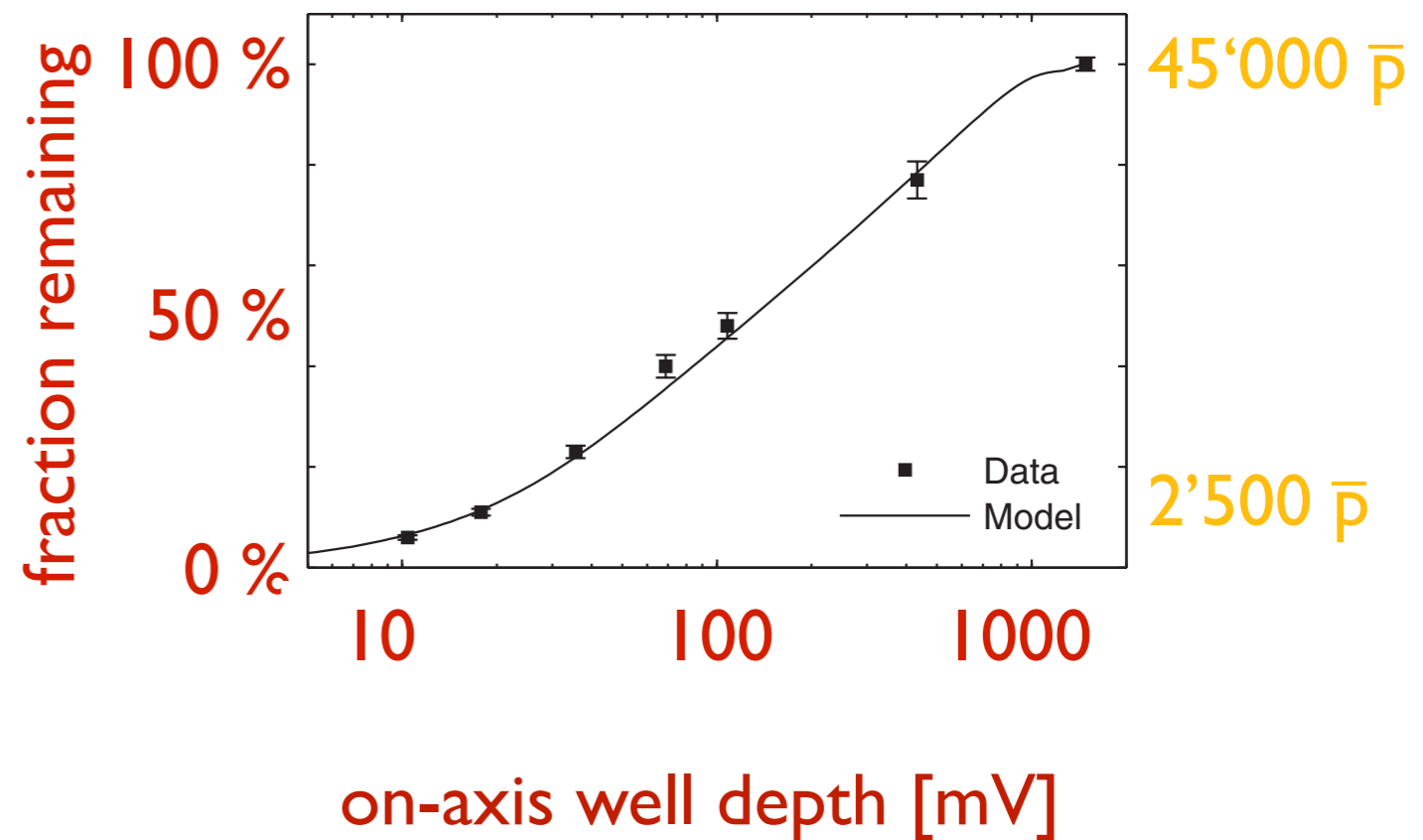
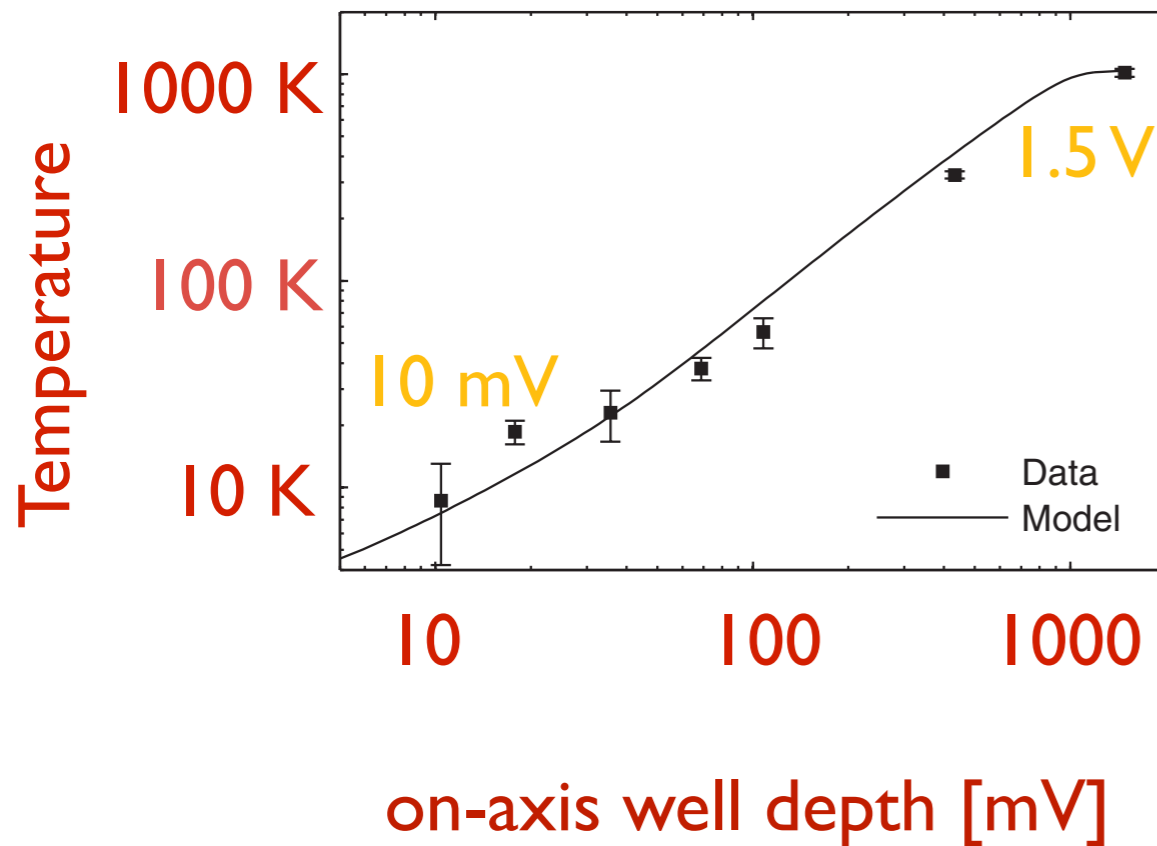
magnetic field considerations

- $e^+$  plasma stability in magnetic multipole traps: expansion due to anisotropies ⇒ possibly higher effective temperature

## Reaching the few K regime

## evaporative cooling of antiprotons (ALPHA)

PRL 105, 013003 (2010)



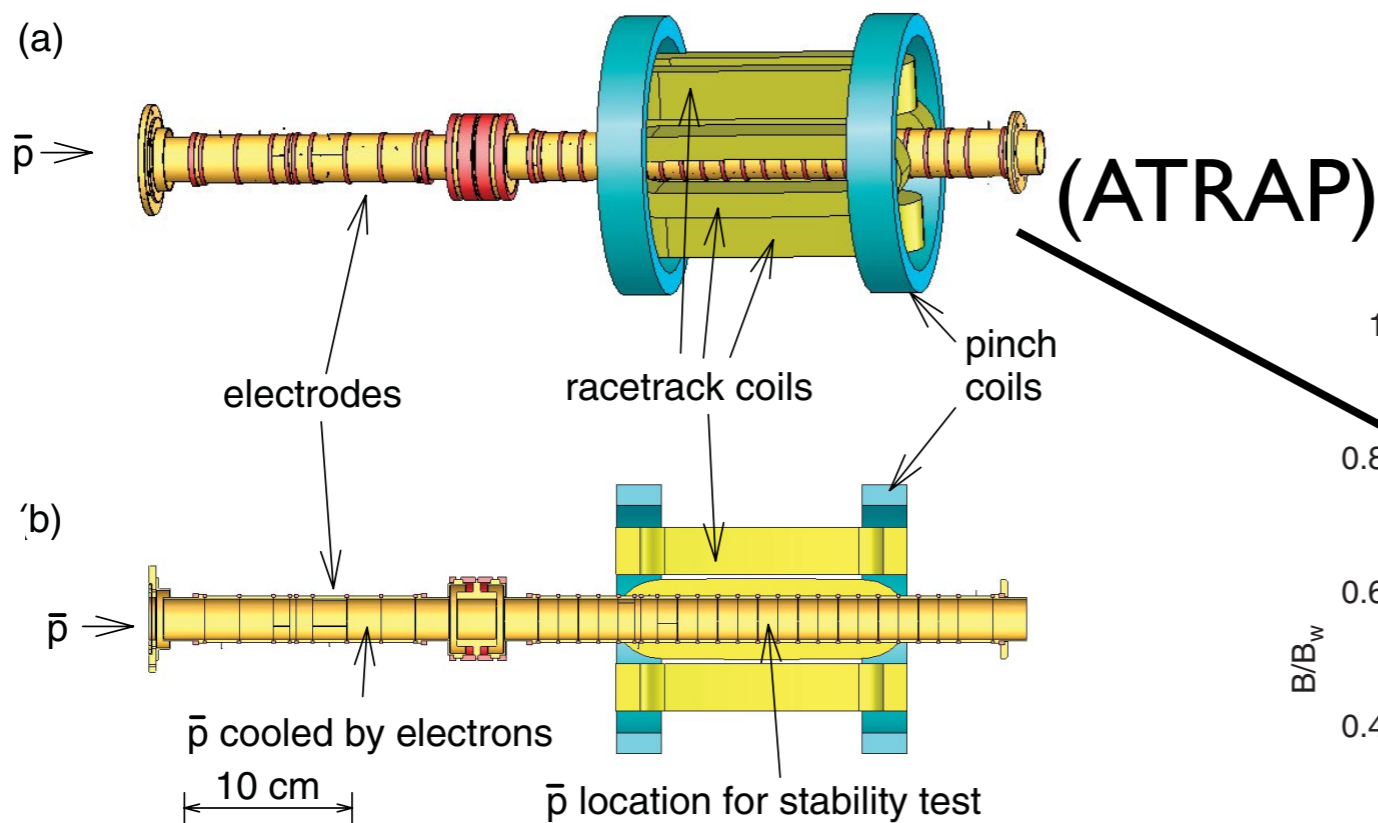
essential to avoid reheating:

- great care needed on noise reduction;
- can not use electron cooling to pre-cool
- bring  $e^+$  to cold  $\bar{p}$ , not vice-versa (?)
- (alternatively, coherently excite cold  $\bar{p}$  and interact with cold  $e^+$ )

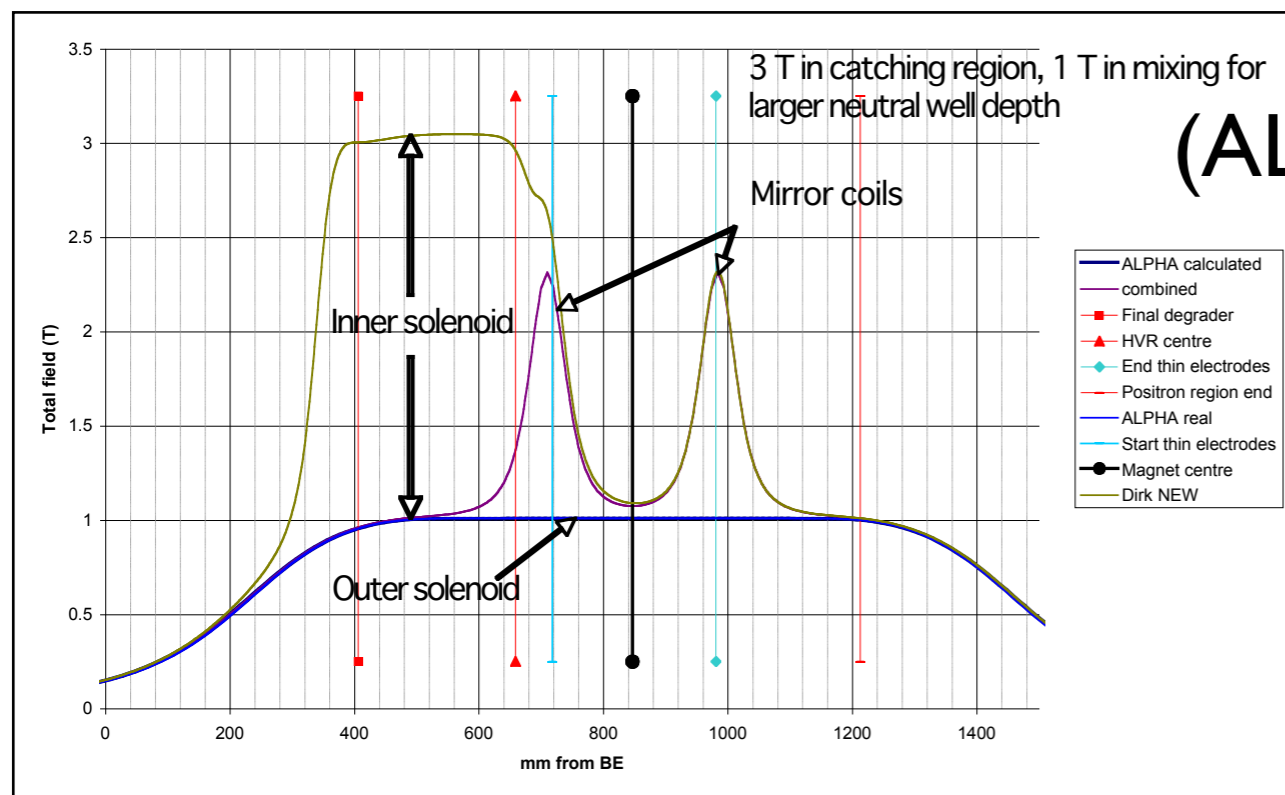
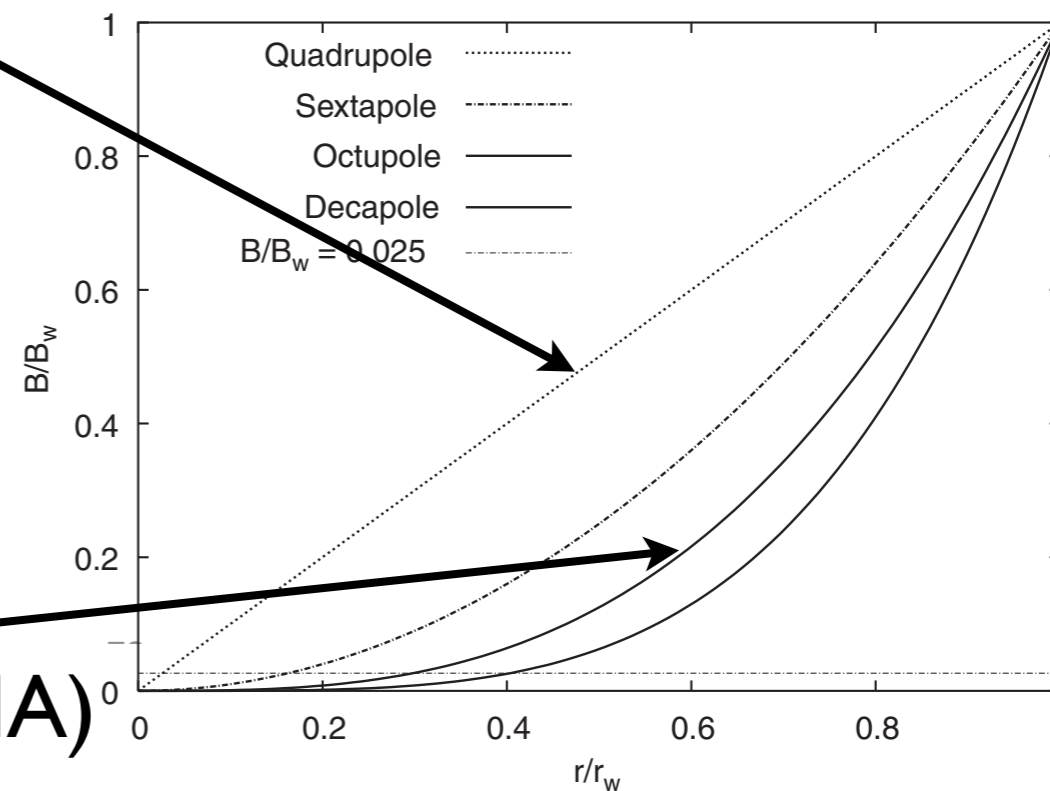


## Antihydrogen Production within a Penning-Ioffe Trap

G.Gabrielse et al., Phys. Rev. Lett. 100, 113001 (2008)



trap depth  $\sim 500$  mK

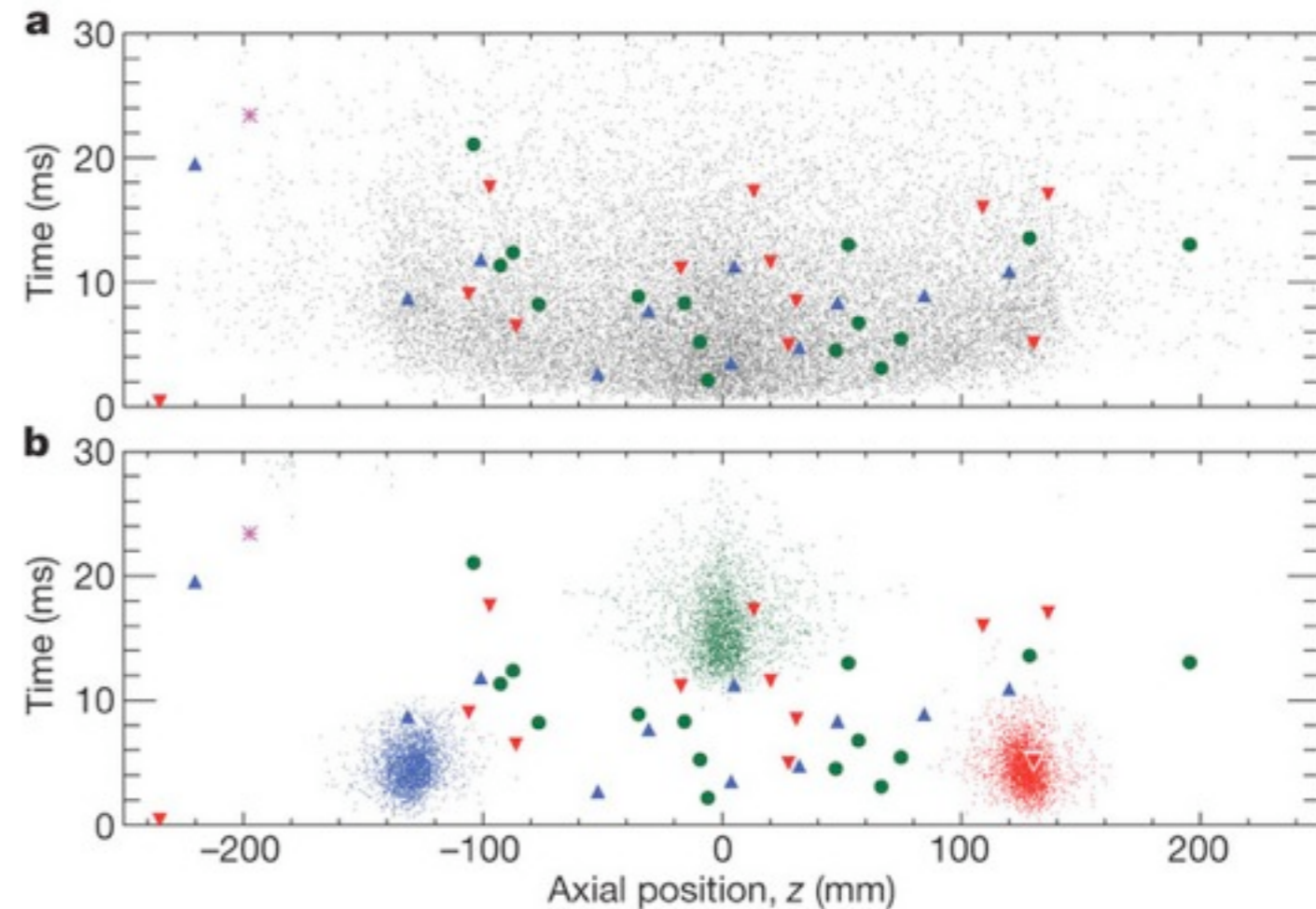
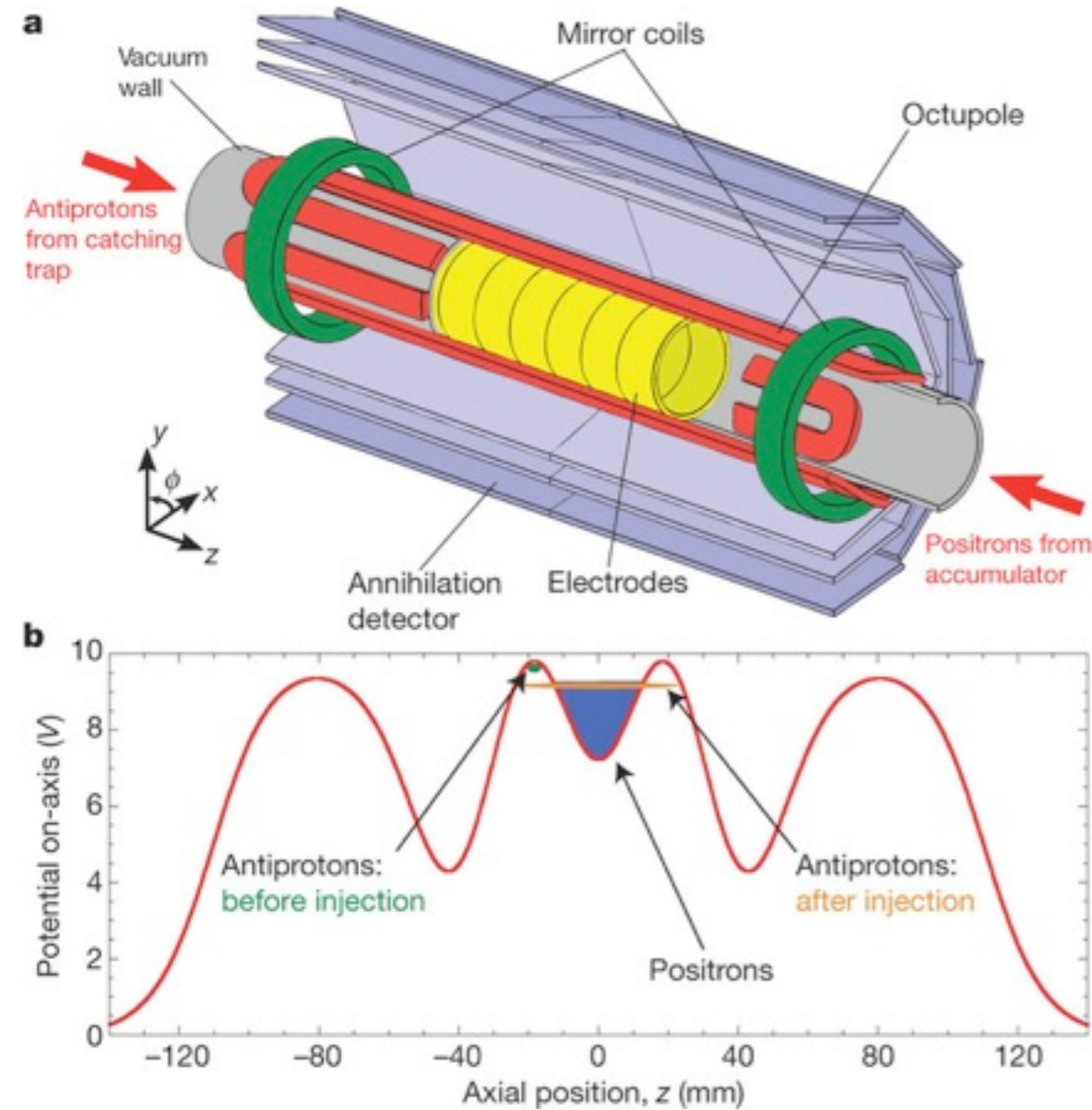


(ALPHA)

plasma stability/temperature  
 $n \gg 1$   
 spin flips during de-excitation

# Successful trapping!

(ALPHA)



quick opening of magnetic trap (20 ms)  
+ sensitive detector for antihydrogen

# Spectroscopy with trapped antihydrogen?

- Detection?
- Present schemes for H spectroscopy require large numbers of atoms:  
 $10^{10}$ – $10^{13}$  (trap),  $10^{15}$ – $10^{17}$  (beam)

- Only  $10^3$ – $10^5$   $\bar{\text{H}}$  atoms available

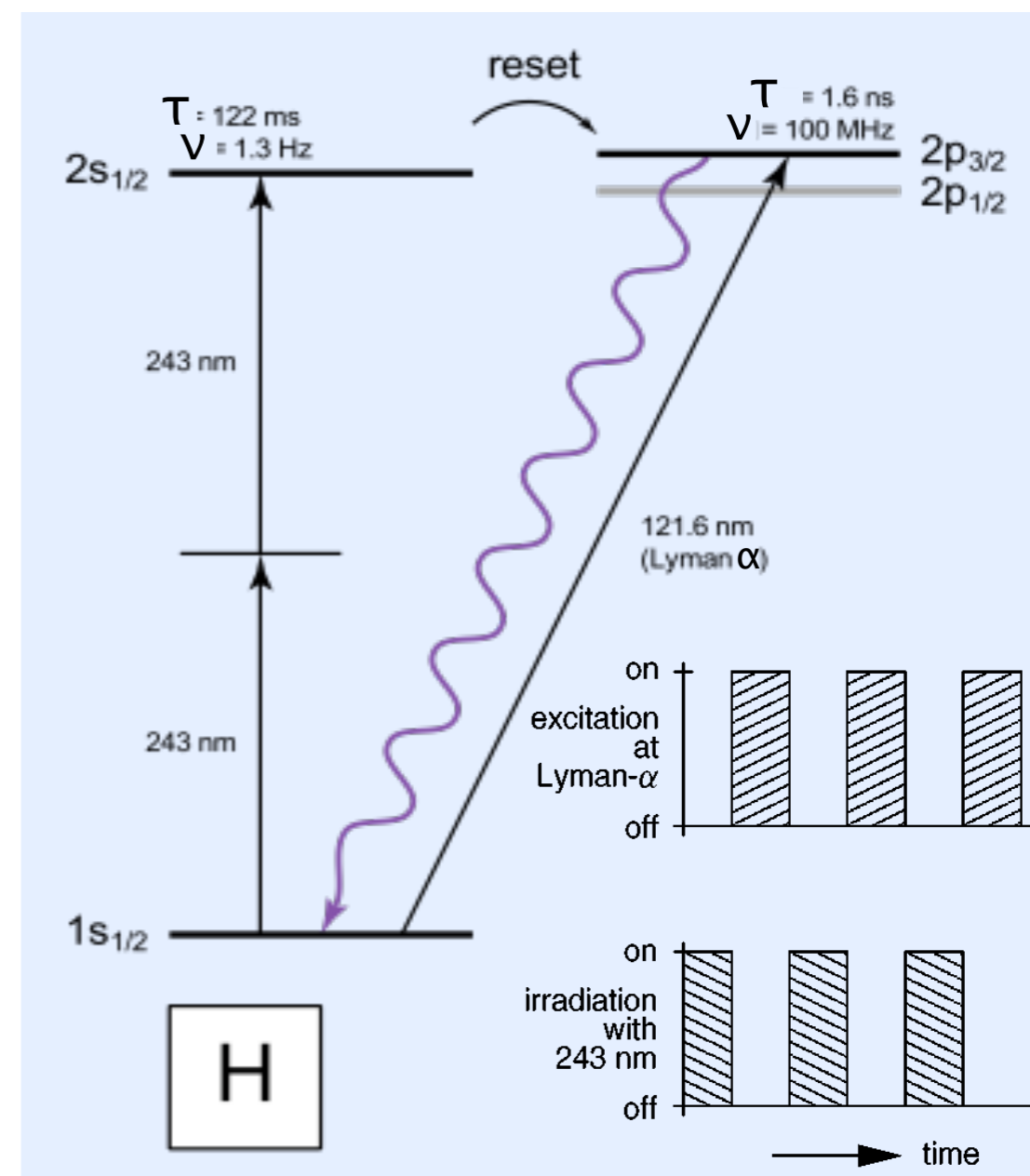
- “Shelving” scheme:

- Strong Lyman- $\alpha$  transition is excited and fluoresces
- Metastable 2s state is populated by Doppler-free 2-photon excitation
- “Shelving” suppresses fluorescence
- 2s state is “reset” with microwave field
- Resolution (nat. linewidth):  $4 \times 10^{-16}$

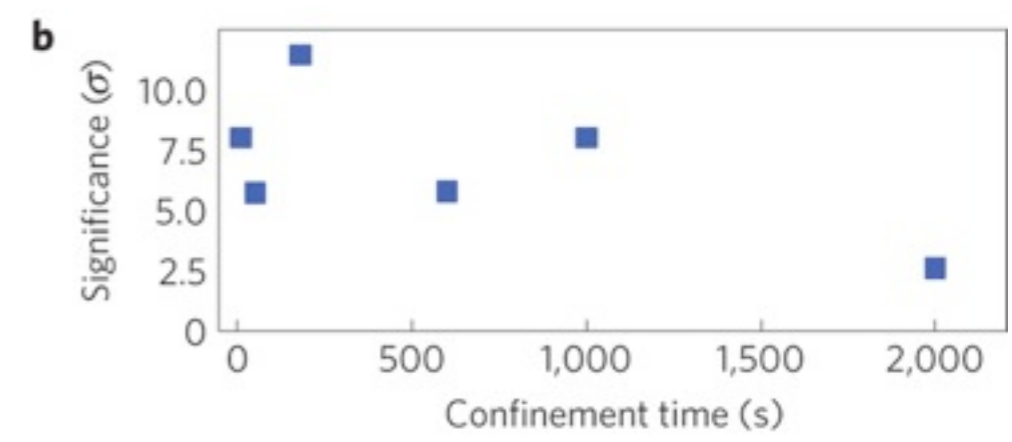
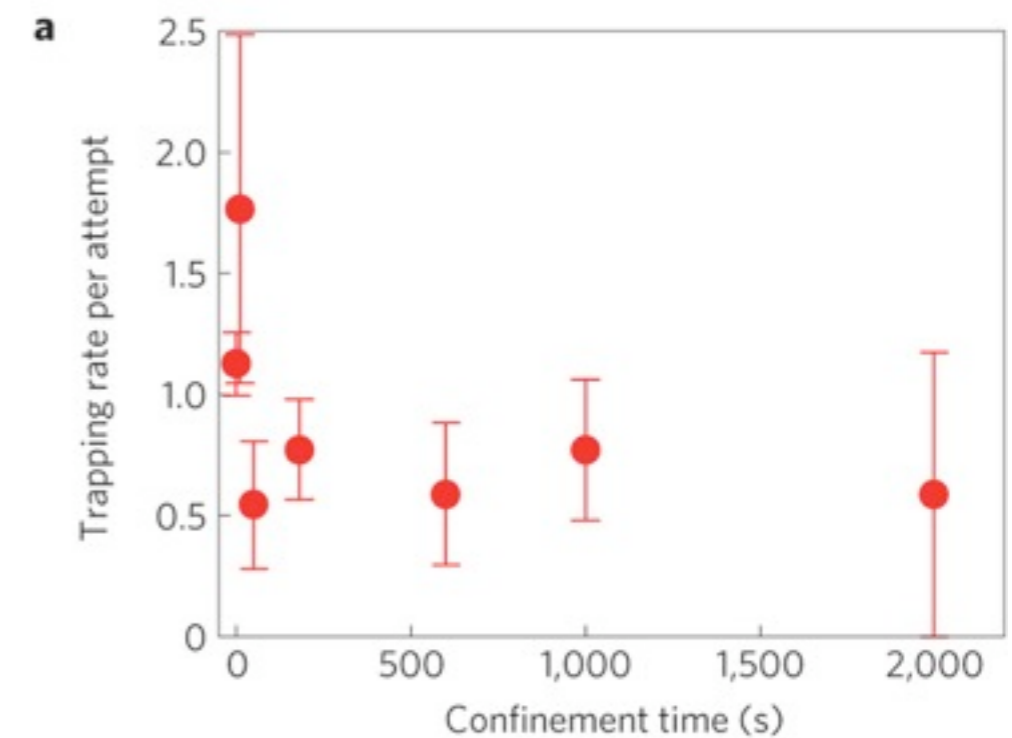
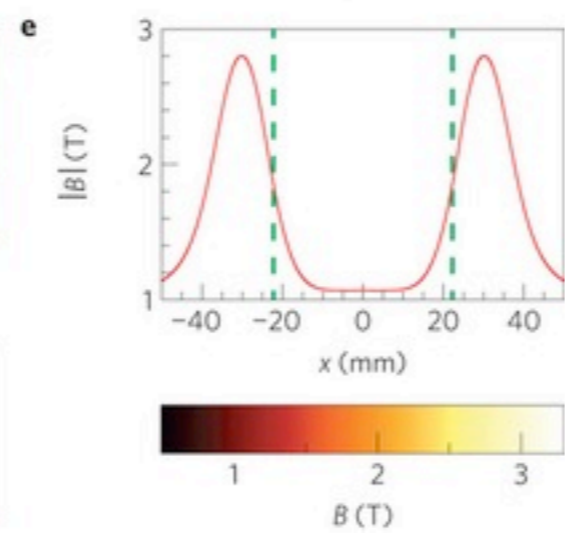
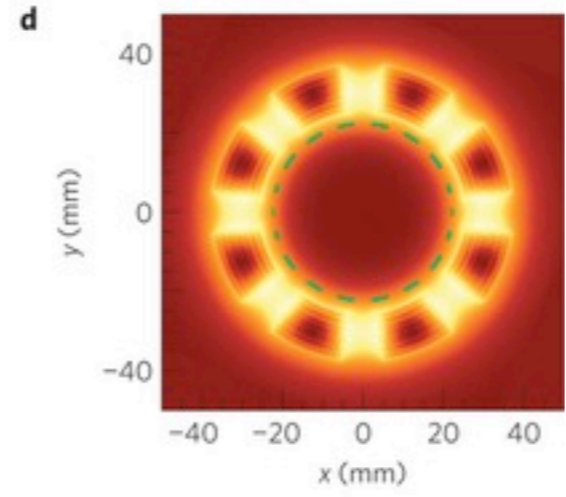
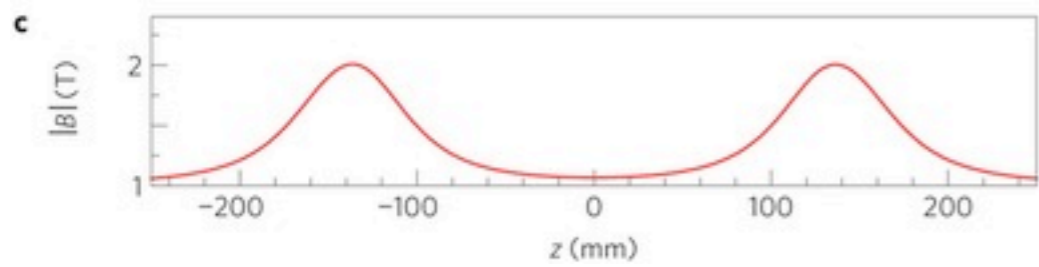
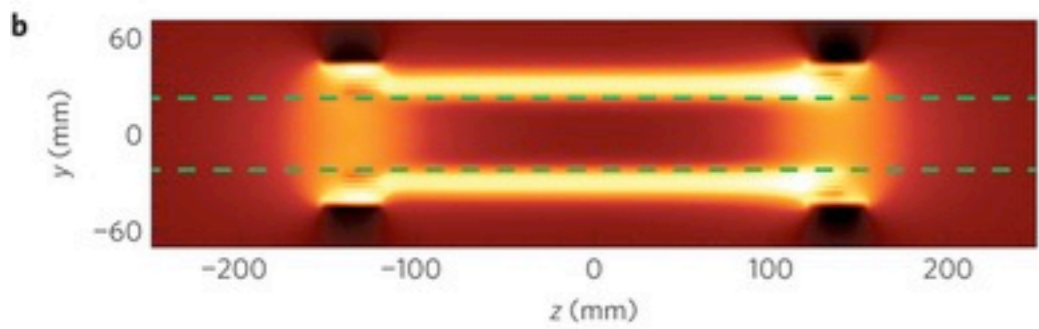
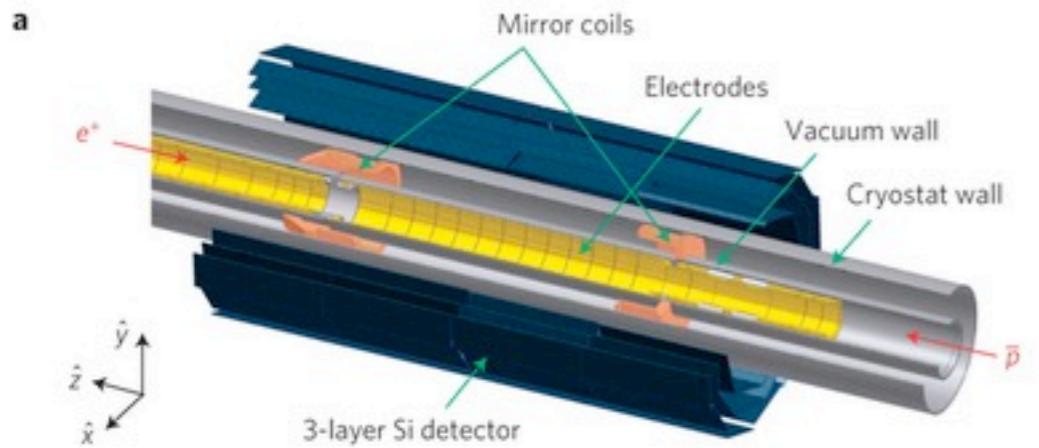
– [J. Walz et al., Hyp. Int. 127 (2000) 167]

1 nW CW can cool 1K  $\bar{\text{H}}$  in about 10s

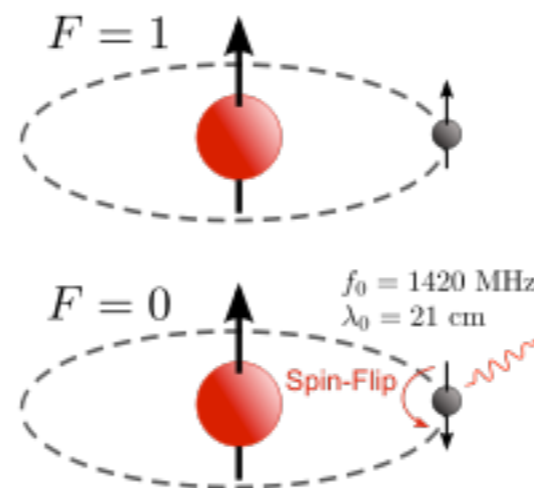
but... more power required for this scheme



# Spectroscopy with trapped antihydrogen?



Spectroscopy: plan B  
HFS via microwave

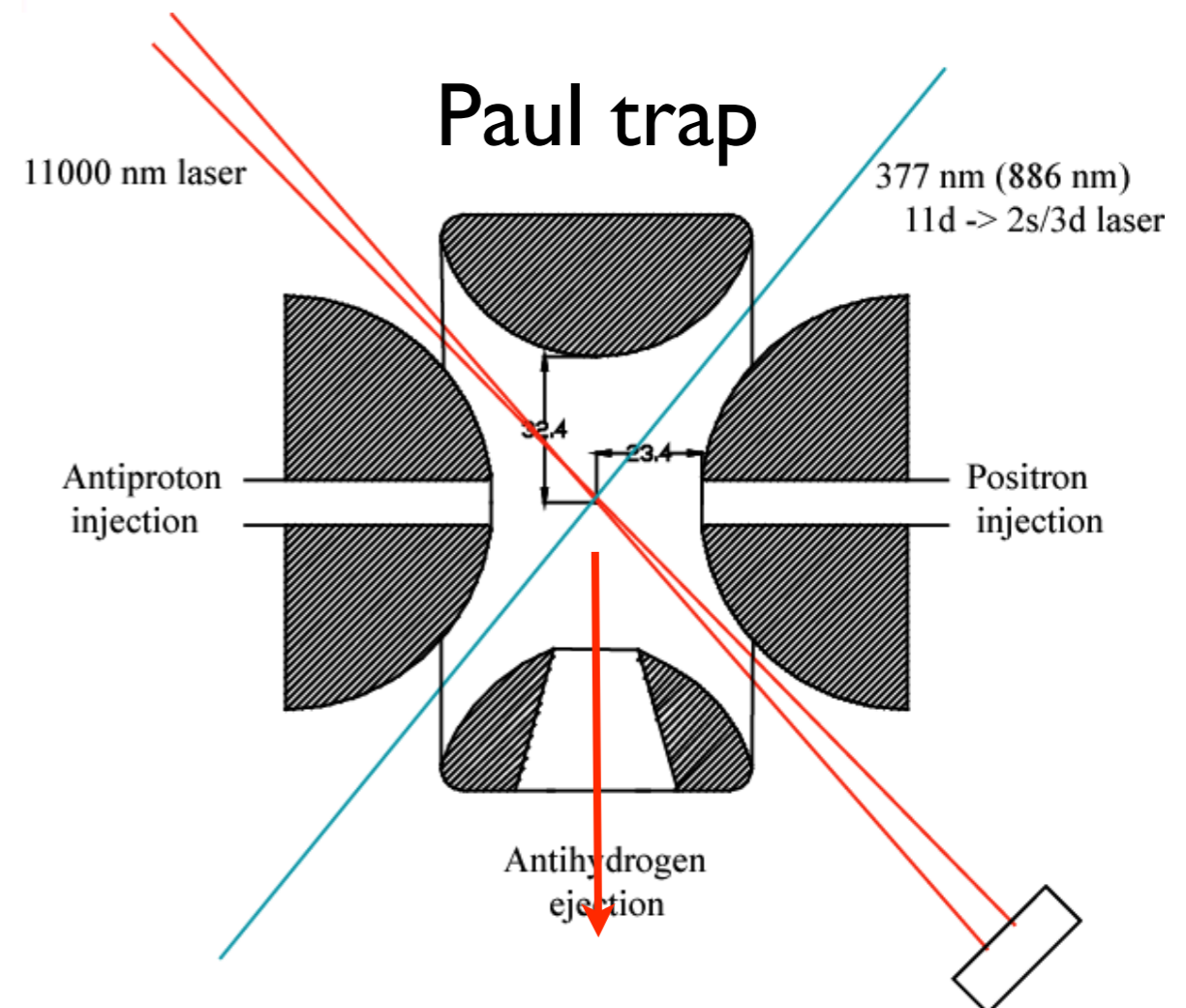
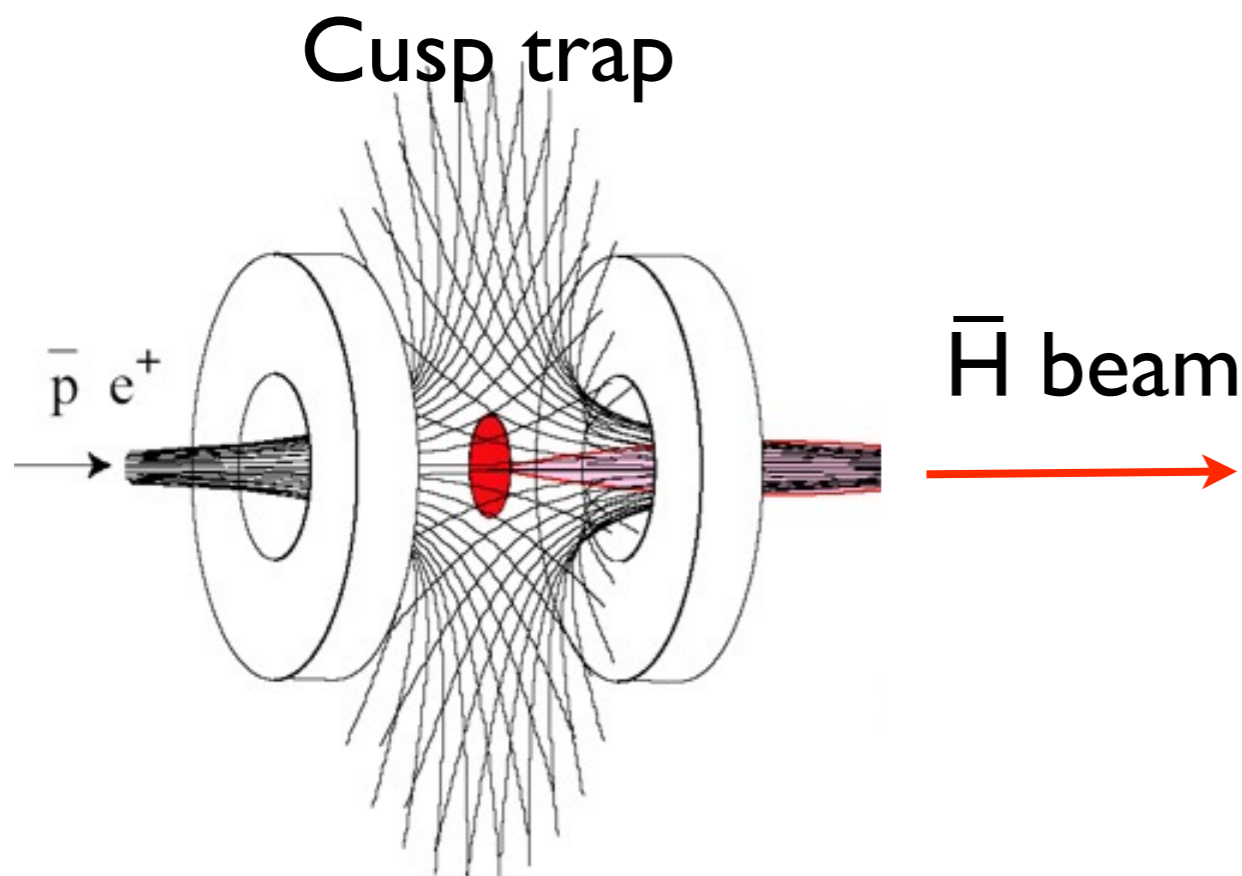


but: B-field at position  
of antihydrogen poorly  
defined ( $1\text{T} < B < 2\text{T}$ )

# Alternatives to Penning-Ioffe traps?

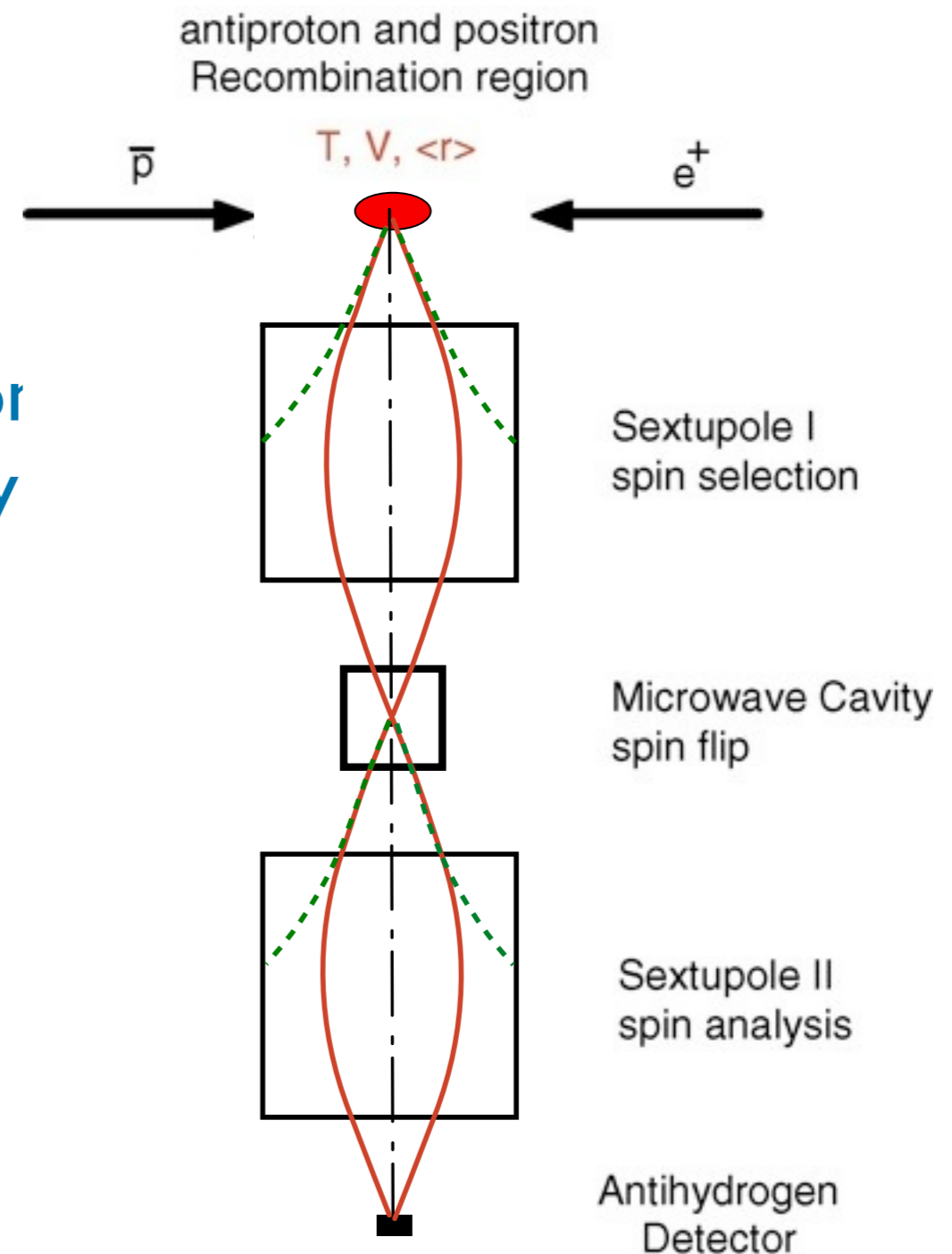
- Magnetic bottle
- $e^-$  trapping achieved
- Neutral atoms were also trapped!

Formation by 3-body recombination  
 Formed  $\bar{H}$  spin-selected  
 Polarized beam?  
 Cold atoms could be trapped?



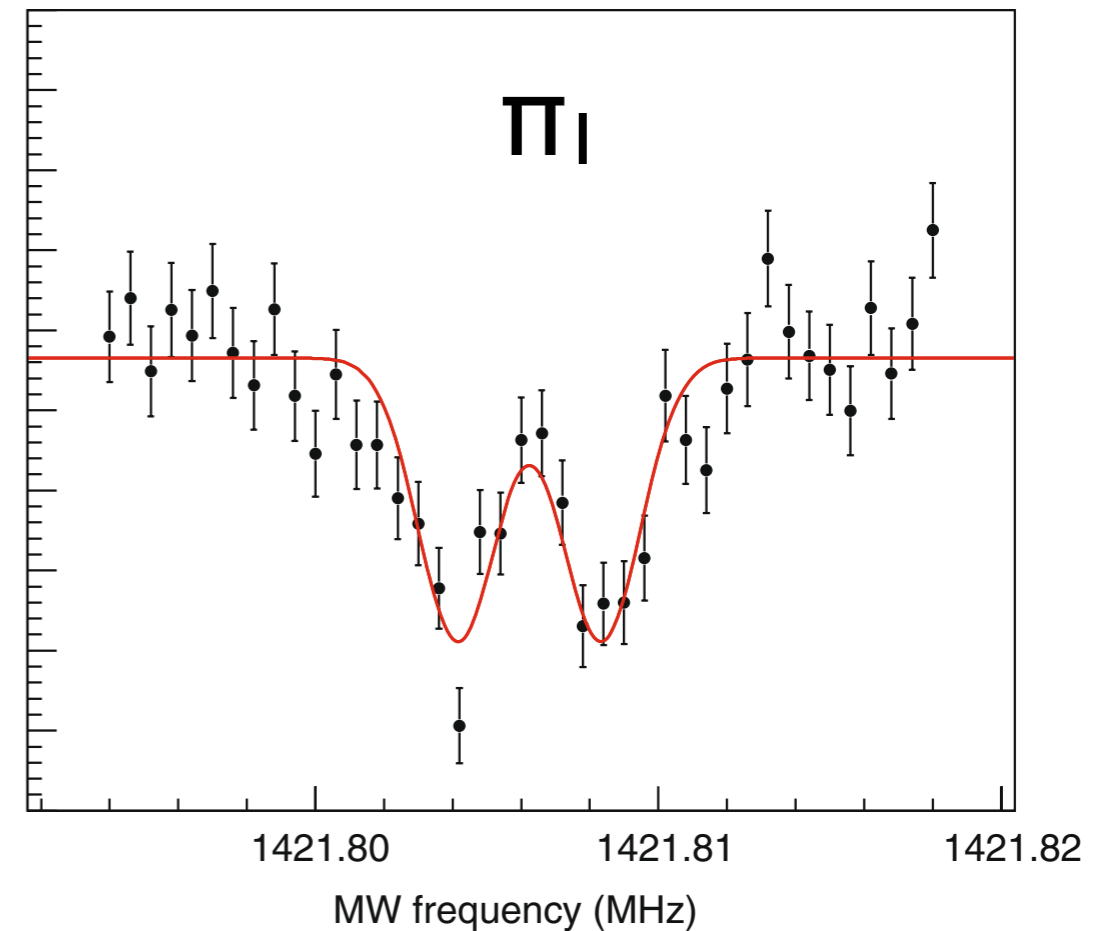
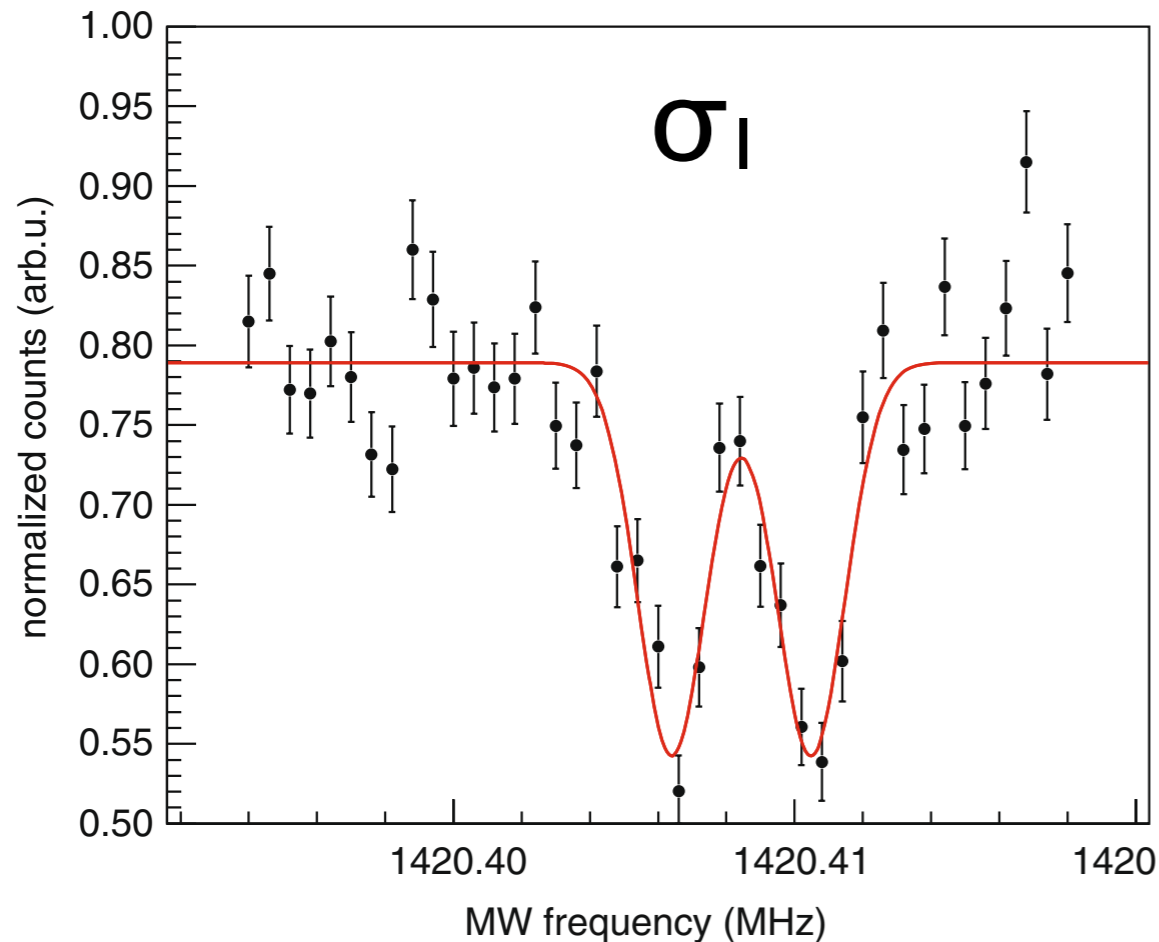
# Experiment with $\bar{\text{H}}$ beam: ground state HFS

- atoms “evaporate”
  - No trapping needed !!
- atomic beam for focussing and
- spin-flip by microwave radiation
- low-background high-efficiency through annihilation
- achievable resolution
  - better than  $10^{-6}$  for  $T < 100\text{K}$
  - $100 \bar{\text{H}}/\text{s}$  in  $1\text{S}$  state needed
- ultimate precision:
  - atomic fountain
- higher temperature is OK



# Simulation of expected signal

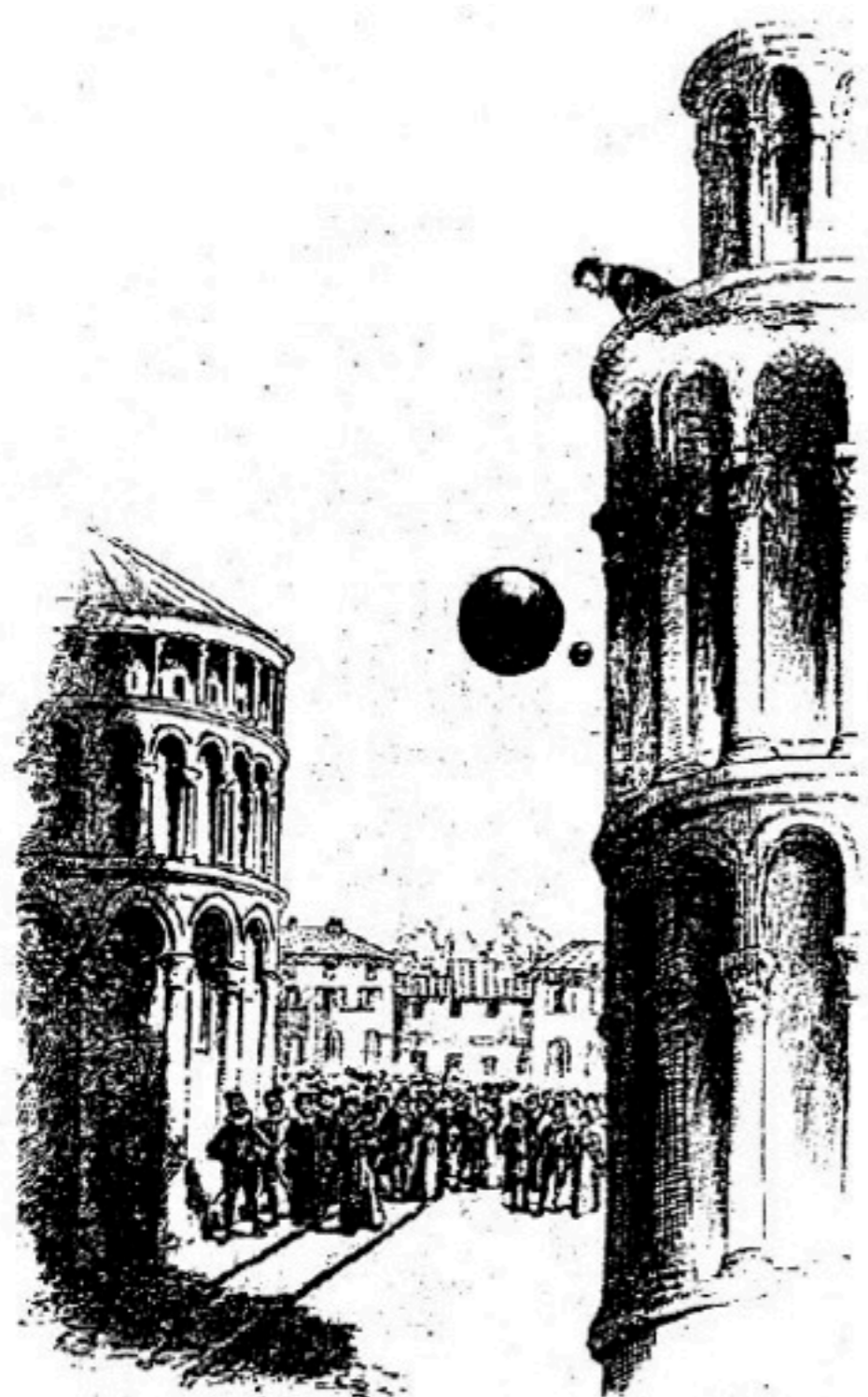
B.Juhasz, E. Widmann, *Hyperfine Interact* (2009) 193:305



(double dip due to structure - and thus modes - of the microwave cavity between the sextupoles)

Under reasonable assumptions & measuring both resonances to extrapolate to zero field  $\Rightarrow$  measurement to  $1 \times 10^{-7}$  appears possible

# One step further: a beam of $\bar{H}$ to test gravity



Tests of gravity require very cold trapped  $\bar{H}$  or a pulsed cold beam of  $\bar{H}$

$$G \sim 100 \text{ nV/m on } \bar{p}$$

Experimental goal:  $g$  measurement with 1% accuracy\* on antihydrogen

(first direct measurement on antimatter)

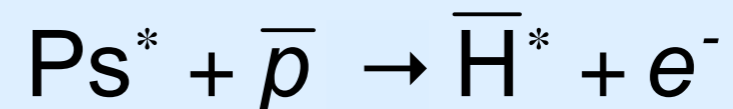
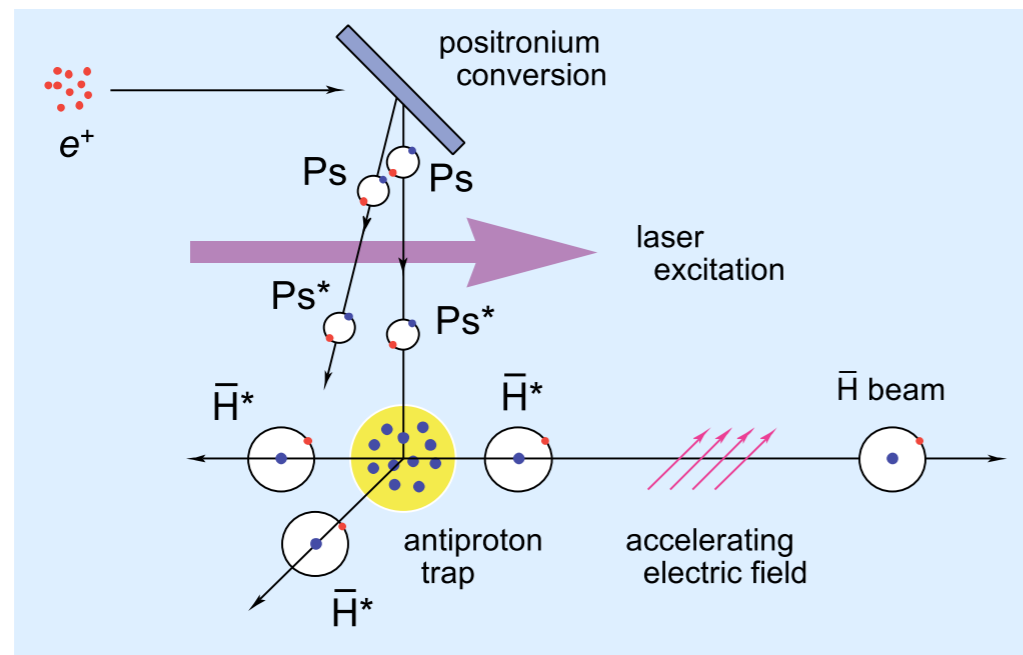
a) production of a pulsed cold beam of antihydrogen ( $T \sim 0.1 \text{ K}$ )

b) measurement of the beam deflection with a Moiré deflectometer



# Step i) antihydrogen formation

- Charge exchange reaction:



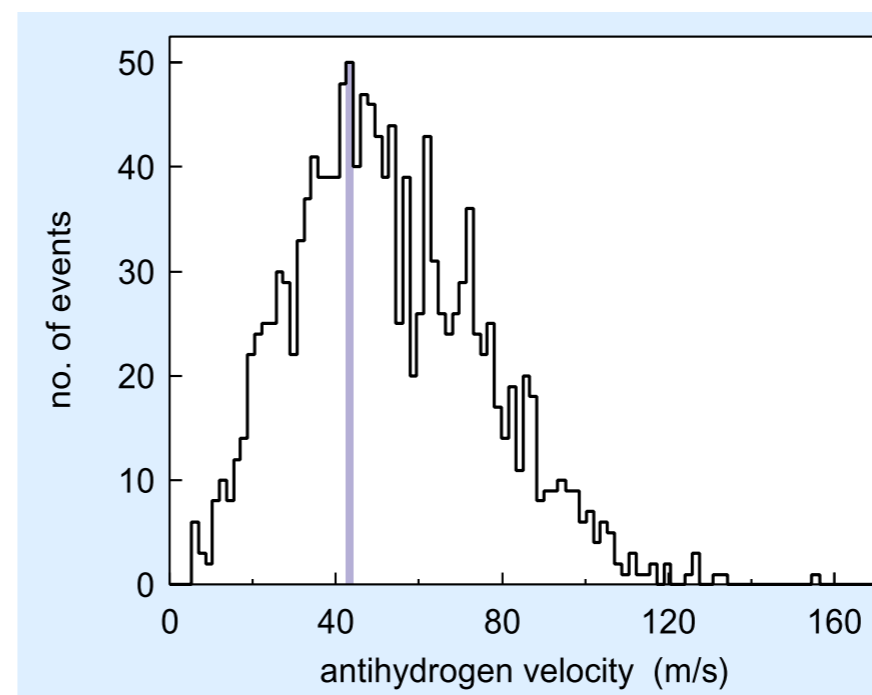
- cold antiprotons ( $T \sim 0.1\text{K}$ )
- production of Rydberg positronium
- production of antihydrogen atoms

- Principle demonstrated by ATRAP ( $Cs^* \rightarrow Ps^* \rightarrow \bar{H}^*$ )

[C. H. Storry *et al.*, Phys. Rev. Lett. **93** (2004) 263401]

- Advantages:

- Large cross-section:  $\sigma \approx a_0 n^4$
- Narrow and well-defined  $\bar{H}$   $n$ -state distribution
- $\bar{H}$  production from  $\bar{p}$  at rest  $\rightarrow$  ultracold  $\bar{H}$
- **pulsed** production of  $\bar{H}$



At  $T(p) = 100\text{mK}$ ,  
 $n(Ps) = 35$   
 $\Rightarrow v(H) \approx 45\text{ m/s}$   
 $T(H) \approx 120\text{mK}$

## Step ii) beam formation

- Neutral atoms are not sensitive to static electric and magnetic fields
- Electric field gradients exert force on electric dipoles:

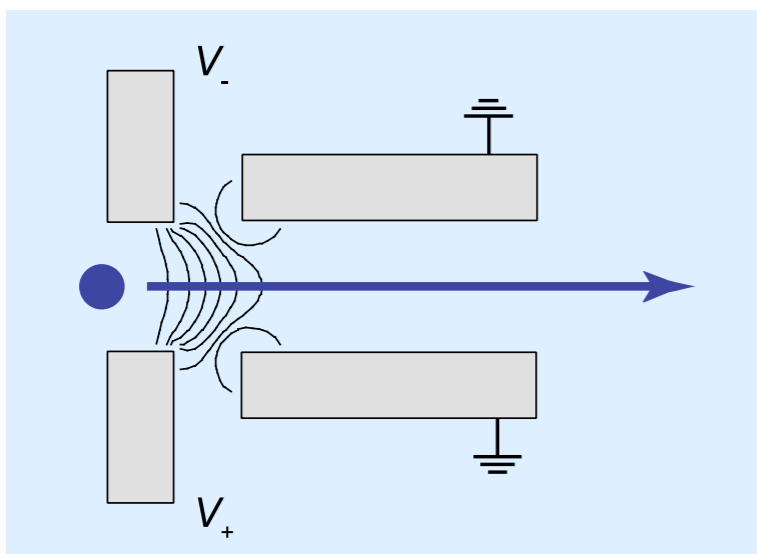
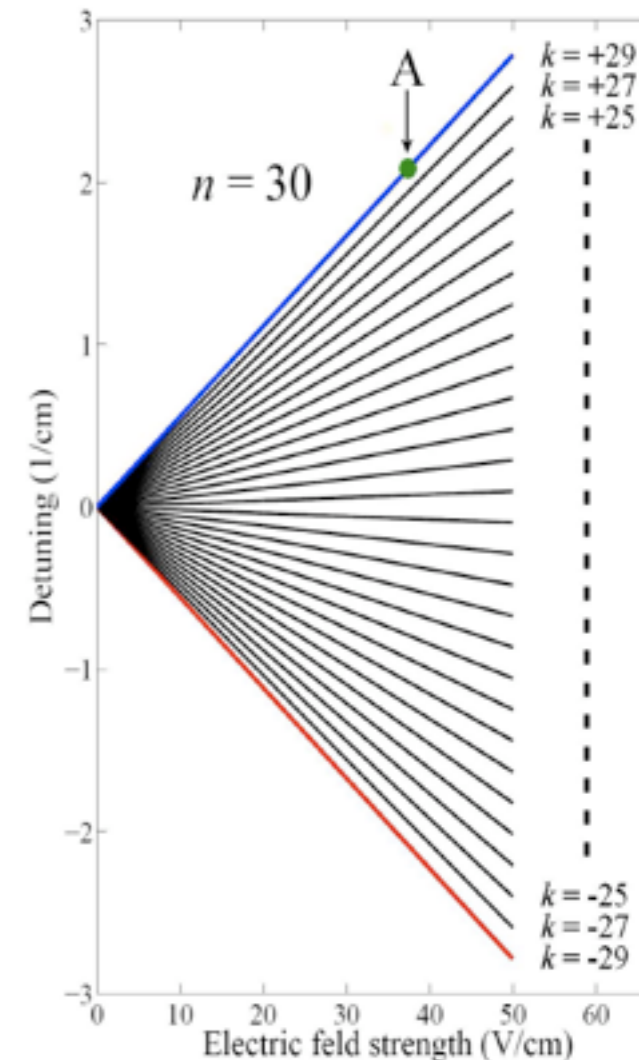
$$E = -\frac{1}{2n^2} + \frac{3}{2}nkF$$

$$Force = -\frac{3}{2}nk\vec{\nabla}F$$

⇒ Rydberg atoms are very sensitive to inhomogeneous electric fields

- Stark deceleration of hydrogen demonstrated

[E. Vliegen & F. Merkt, J. Phys. B **39** (2006) L241 - ETH Physical Chemistry]

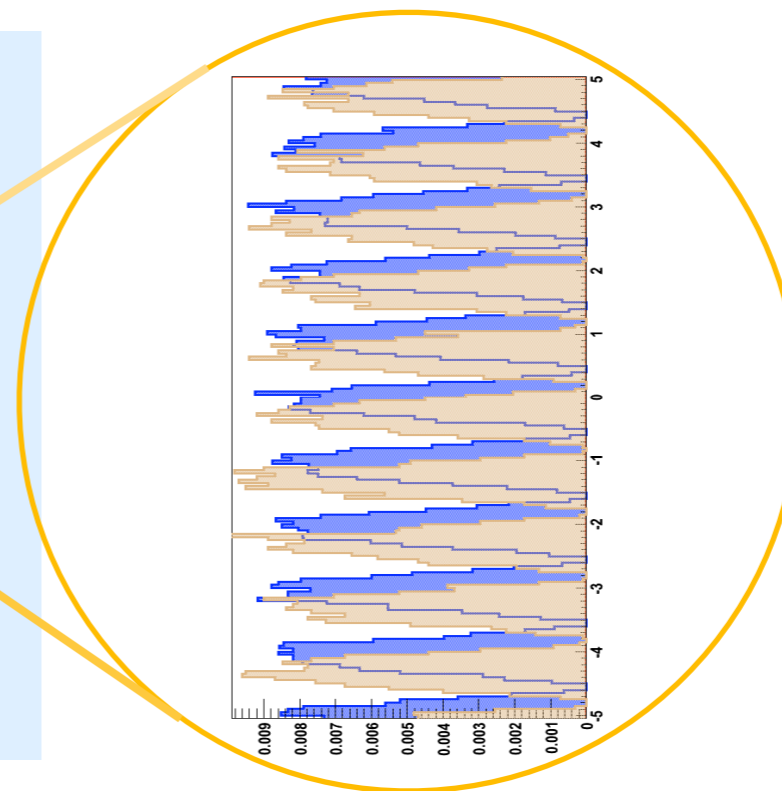
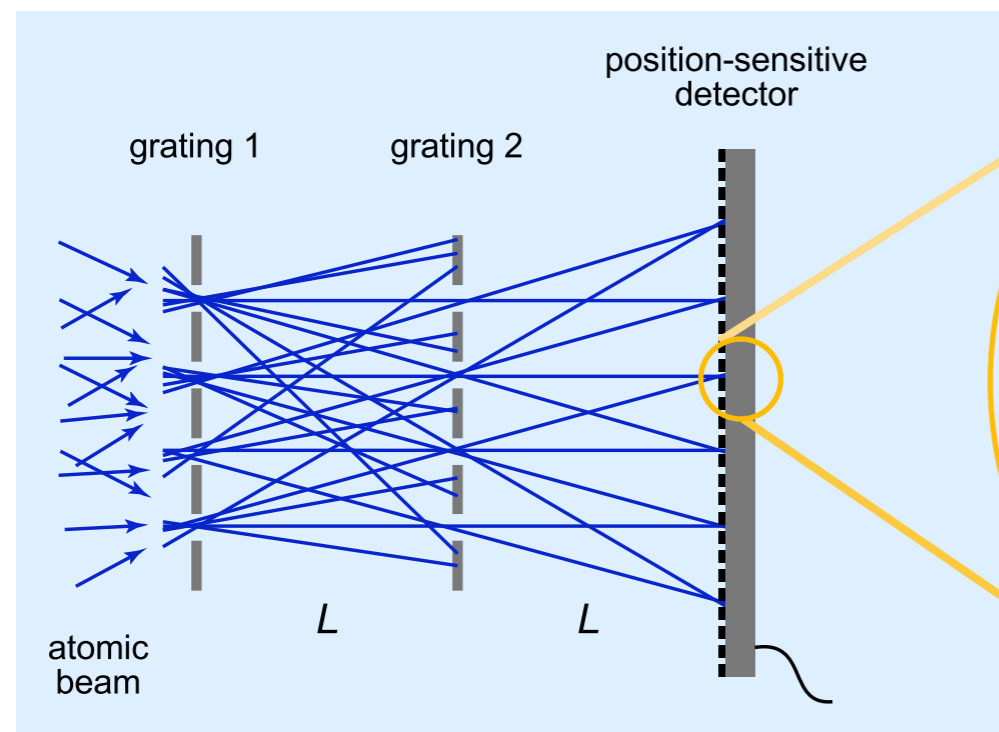


- $n = 22, 23, 24$
- Accelerations of up to  $2 \times 10^8 \text{ m/s}^2$  achieved
- Hydrogen beam at 700 m/s can be stopped in 5  $\mu\text{s}$  over only 1.8 mm
- ongoing work on Zeeman deceleration, Stark deceleration and trapping of H

# Step iii) trajectory measurement

- Classical counterpart of the Mach-Zehnder interferometer
  - Decoherence effects reduced
  - “Self-focusing” effect – beam collimation uncritical

Fringe phase and phase shift identical to Mach-Zehnder interferometer!



$v = 250$  m/s

$v = 600$  m/s

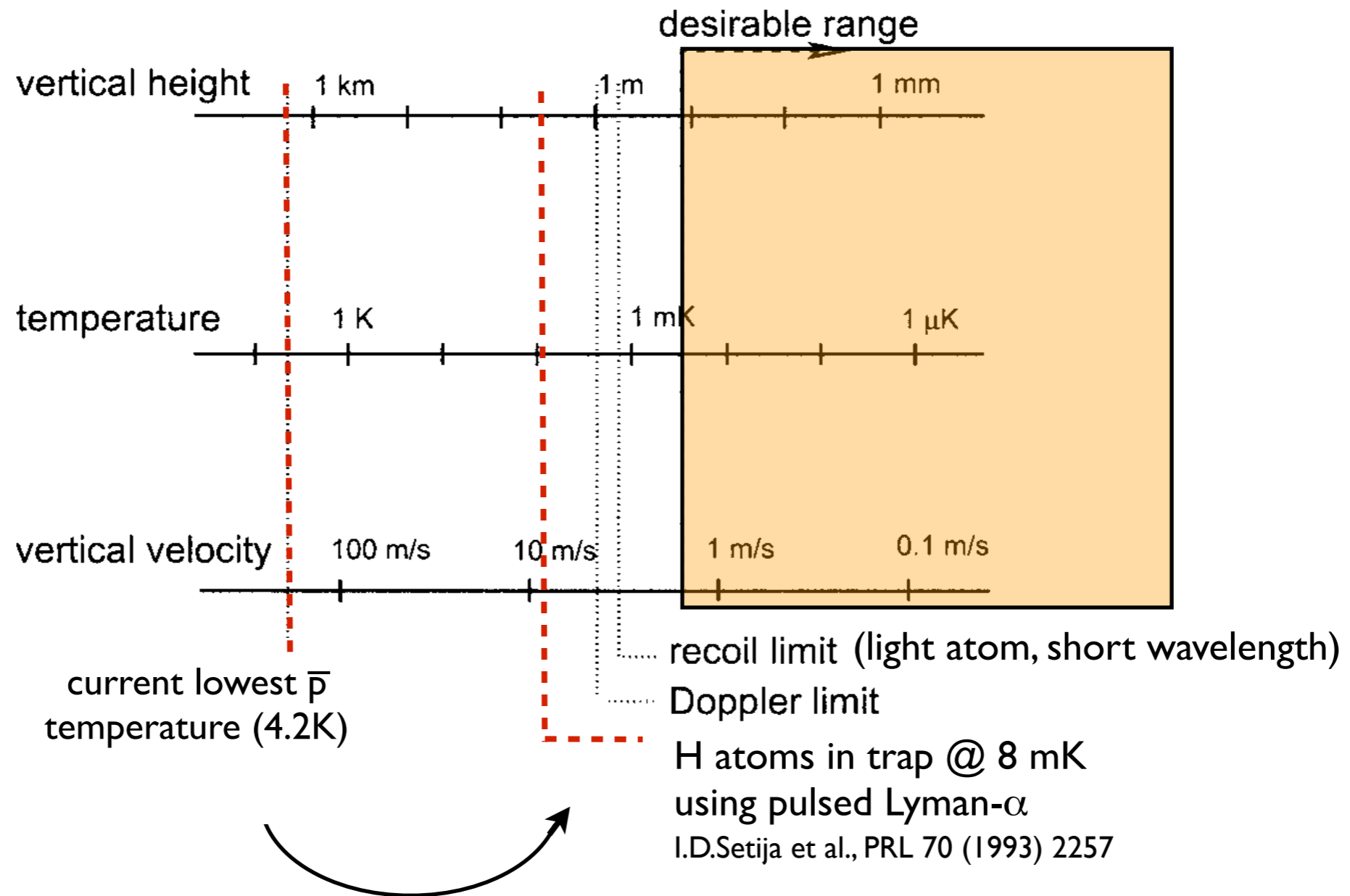
$$\delta = \frac{gt^2}{a}$$

- Replace the third grating and detector by position-sensitive detector
  - $\Rightarrow$  Transmission increases by  $\sim$  factor 3
- Has been successfully used for a gravity measurement with ordinary matter,  $\sigma(g)/g = 2 \times 10^{-4}$
- with  $10^5$   $\bar{H}$  at 100mK,  $\sigma(g)/g = 1\%$  (expected)

[M. K. Oberthaler *et al.*, Phys. Rev. A **54** (1996) 3165]

[A. Kellerbauer *et al.*, Phys. Rev. A **54** (1996) 3165]

# “Ultra-cold” ( $\sim 1 \mu\text{K}$ ) Antihydrogen



IS $\rightarrow$ 2P laser cooling: cw Lyman- $\alpha$  source  
Eikema, Walz, Hänsch, PRL 86 (2001) 5679

# sympathetic cooling to the rescue

## cooling of $\bar{H}^+$

J. Walz and T. Hänsch, Gen. Rel. and Grav. 36 (2004) 561

formation of  $\bar{H}^+$  (binding energy = 0.754 eV)

how? perhaps through  $Ps(2p) + \bar{H}(1s) \rightarrow \bar{H}^+ + e^-$

Roy & Sinha, EPJD 47 (2008) 327

sympathetic cooling of  $\bar{H}^+$

e.g.  $In^+$   $\rightarrow$  20  $\mu$ K

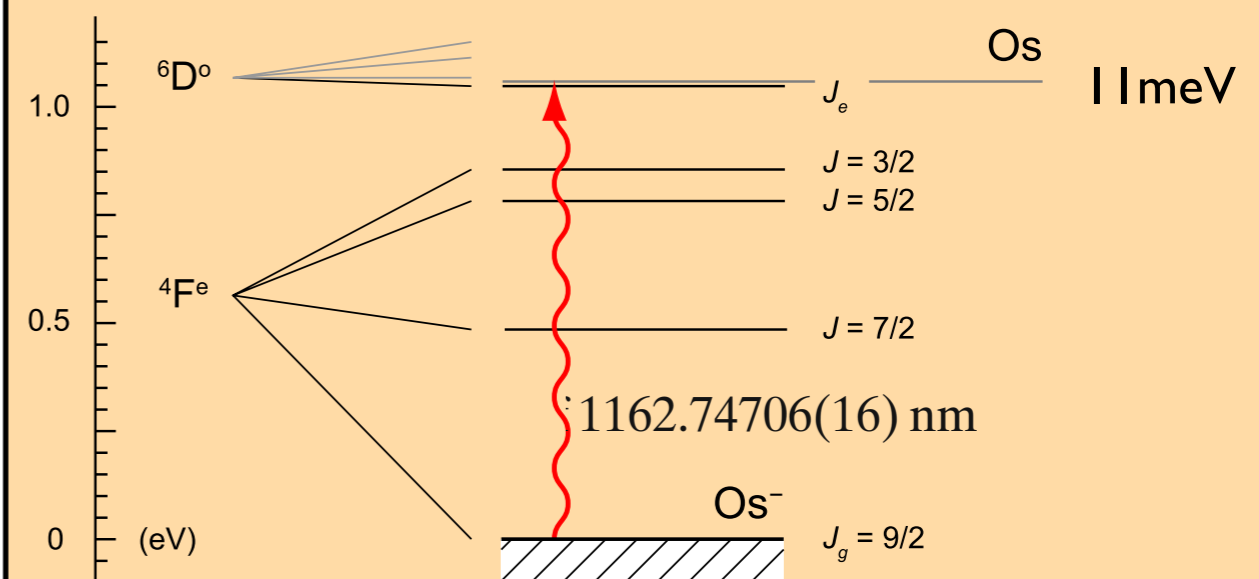
photodetachment at  $\sim 6083 \text{ cm}^{-1}$

gravity measurement via TOF

## cooling of $\bar{p}$

Warring et al, PRL 102 (2009) 043001

Fischer et al, PRL 104 (2010) 073004



very weak cooling

$\rightarrow$  best to start at  $\sim 4\text{K}$  and cool to Doppler limit ( $T_D \approx 0.24 \mu\text{K}$ )

should allow reaching same precision on  $g$  as with atoms ( $10^{-6}$  or better)

the other bottleneck:  $\bar{p}$ 's

The Antiproton decelerator produces  $10^7 \bar{p}/\text{cycle}$  (100s)

Trapping efficiency  $\sim 0.1\% = 10^7 \bar{p}/\text{cycle}$  (100s)

Build new deceleration stage  $100 \text{ MeV}/c \Rightarrow 100 \text{ keV}/c$

Trapping efficiency  $\sim O(100\%)$

ELENA = Extra Low ENergy Antiproton ring

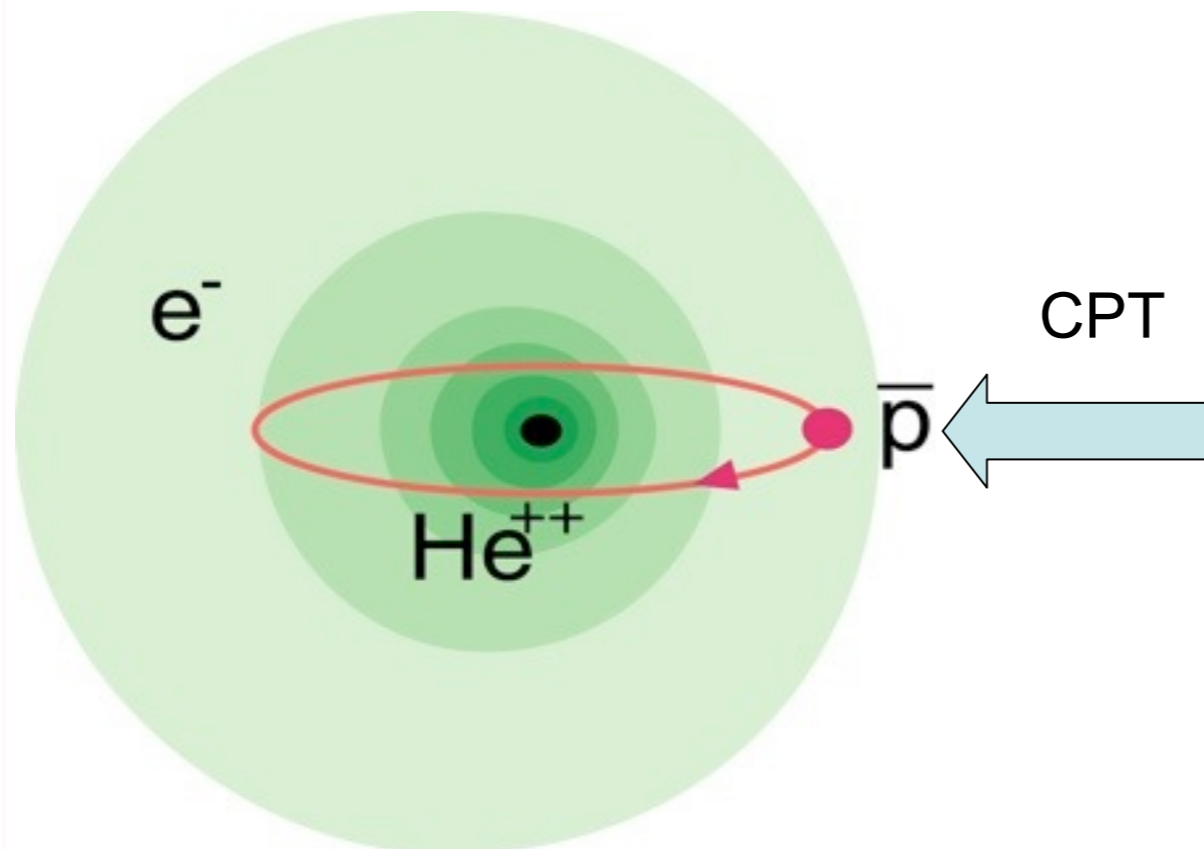
# A final detour: other antimatter spectroscopy

## Antiprotonic helium and CPT



ASACUSA

- Three-body system  $\text{He}^{++} e^- \bar{p}$ 
  - $\bar{p}$  in highly excited, near circular states  $(n,l) \sim (38,37)$
- Easy (automatic) formation
- Comparison to 3-body QED calculations that use proton mass



$$E_{nr} = \left\langle -\frac{1}{2m_{13}} \nabla_{r_1}^2 - \frac{1}{2m_{23}} \nabla_{r_2}^2 - \frac{1}{m_3} \nabla_{r_1} \nabla_{r_2} + \frac{Z_1 Z_3}{r_1} + \frac{Z_2 Z_3}{r_2} + \frac{Z_1 Z_2}{r_{12}} \right\rangle.$$

$$E_{rc} = \alpha^2 \left\langle -\frac{\nabla_i^4}{8m_e^3} + \frac{1}{8m_e^2} [Z_{\text{He}} 4\pi \delta(\mathbf{r}_{\text{He}}) + Z_{\bar{p}} 4\pi \delta(\mathbf{r}_{\bar{p}})] \right\rangle.$$

$$E_{rc-qed} = \alpha^2 \left\langle \frac{2a_e}{8m_e^2} [Z_{\text{He}} 4\pi \delta(\mathbf{r}_{\text{He}}) + Z_{\bar{p}} 4\pi \delta(\mathbf{r}_{\bar{p}})] \right\rangle,$$

$$E_{se} = \alpha^3 \left\langle \frac{4Z_i}{3} \delta(\mathbf{r}_i) \left\{ \left[ \ln \frac{1}{\alpha^2} - \ln \frac{k_0(n)}{\text{Ry}} + \frac{5}{6} - \frac{3}{8} \right] + (Z_i \alpha) 3\pi \left( \frac{139}{128} - \frac{1}{2} \ln 2 \right) - \frac{3}{4} (Z_i \alpha)^2 \ln^2 \frac{1}{(Z_i \alpha)^2} \right\} \right\rangle.$$

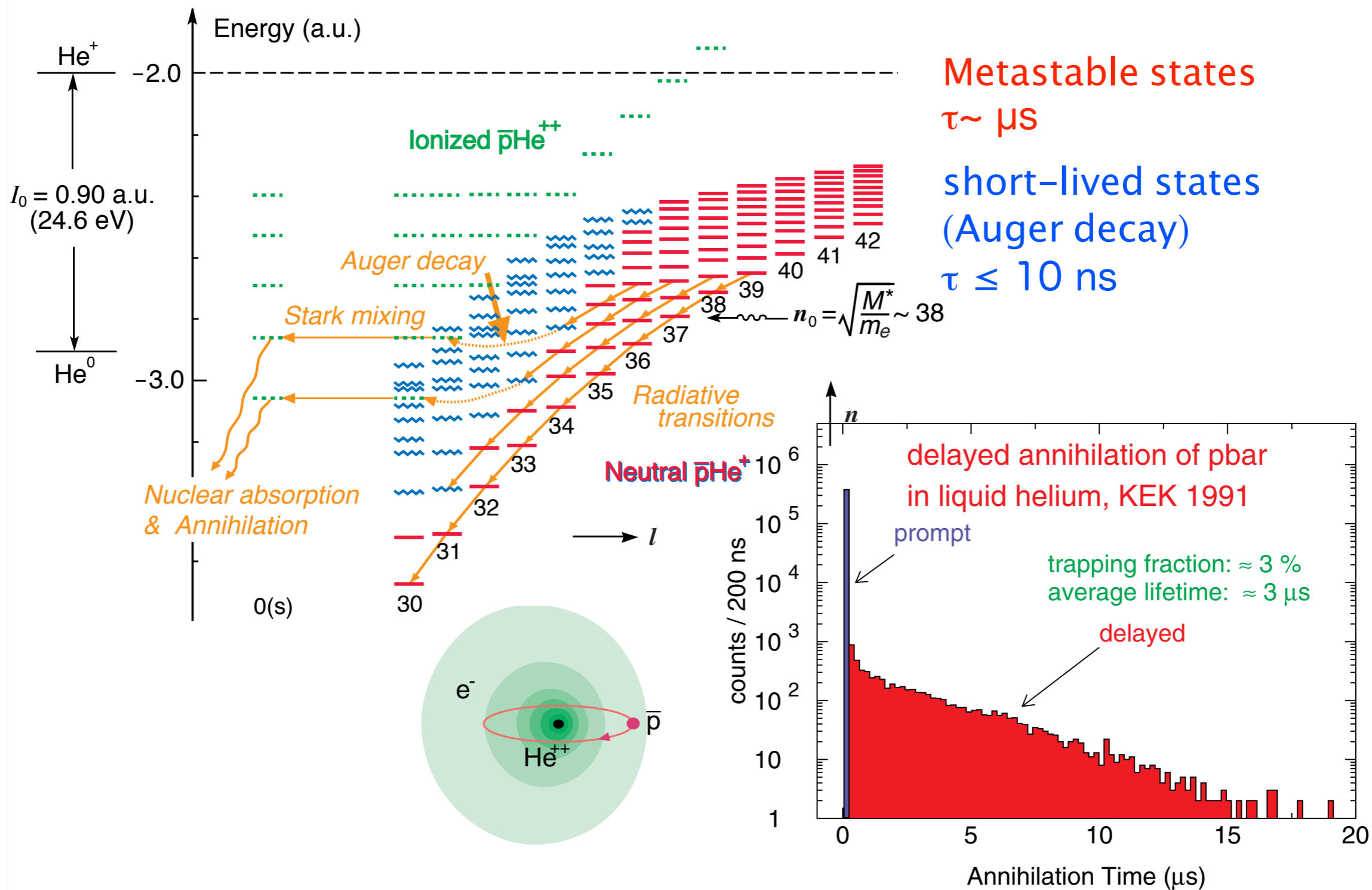
$$E_{vp} = \alpha^3 \left\langle \frac{4Z_i}{3} \left[ -\frac{1}{5} + (Z_i \alpha) \pi \frac{5}{64} \right] \right\rangle.$$

$$E_{RMC} = -\alpha^2 \left\langle \frac{\nabla_{\text{He}}^4}{8m_{\text{He}}^3} + \frac{\nabla_{\bar{p}}^4}{8m_{\bar{p}}^3} \right\rangle,$$

$$E_{ret} = \alpha^2 \sum_{i>j} \frac{Z_i Z_j}{2m_i m_j} \left\langle \frac{\nabla_i \nabla_j}{r_{ij}} + \frac{\mathbf{r}_{ij} (\mathbf{r}_{ij} \cdot \nabla_i) \nabla_j}{r_{ij}^3} \right\rangle.$$

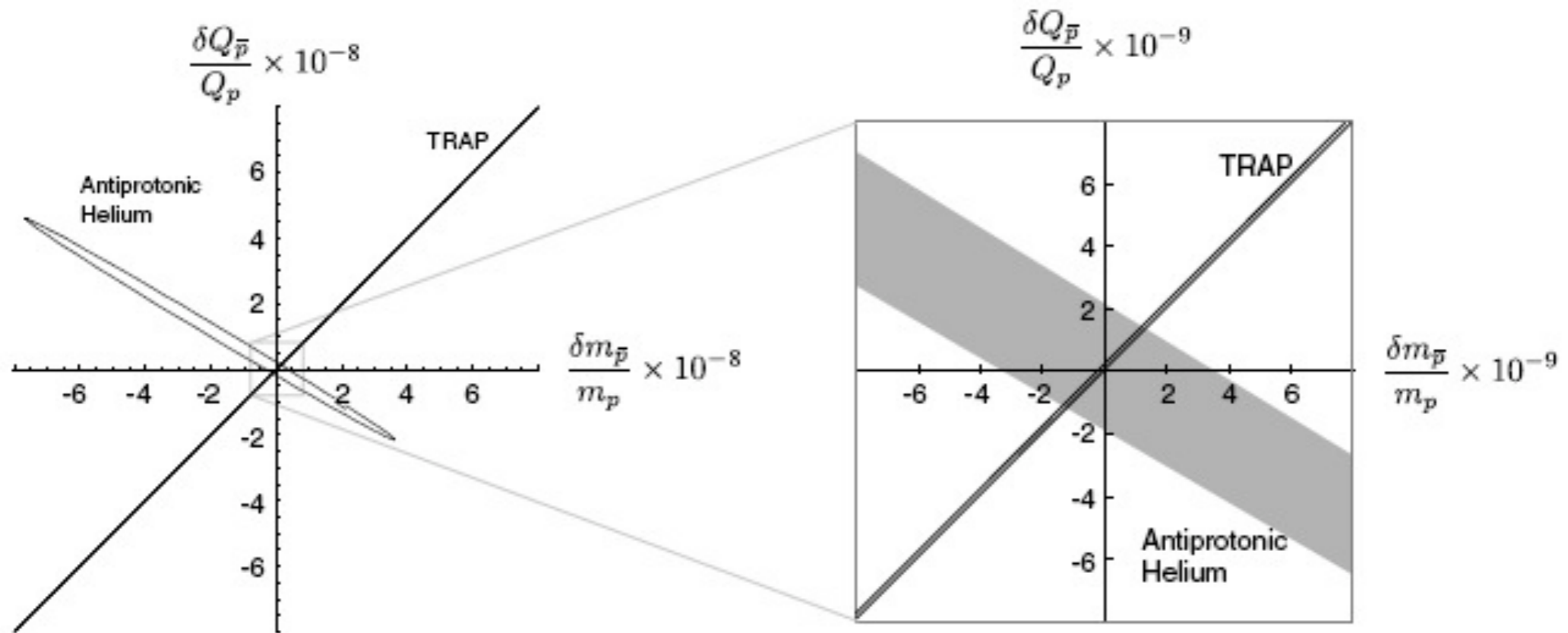
$$E_{two-loop} = \alpha^4 \left\langle \frac{Z_i}{\pi} \left[ -\frac{6131}{1296} - \frac{49\pi^2}{108} + 2\pi^2 \ln 2 - 3\zeta(3) \right] \delta(\mathbf{r}_i) \right\rangle$$

# Antiprotonic helium (“atomcules”)





# $\bar{p}/p$ charge and mass: $\bar{p}\text{He} + \text{TRAP}$



- Q/M of proton/antiproton

$$\frac{|Q/M(\bar{p}) - Q/M(p)|}{\text{average}} < 9 \times 10^{-11}$$

$$\left| \frac{M_{\bar{p}} - M_p}{M_p} \right| \approx \left| \frac{Q_{\bar{p}} - Q_p}{Q_p} \right| < \begin{cases} 6 \times 10^{-8} & (2000) \\ 1 \times 10^{-8} & (2003) \\ 3 \times 10^{-9} & (2006) \end{cases}$$

- Gabrielse et al  
Phys. Rev. Lett. 82 (1999) 3198

RS Hayano, M Hori, D Horvath and E  
Widmann Rep. Prog. Phys. 70 (2007) 1995-2065

## Summary:

### Trapping of antihydrogen:

ATRAP and ALPHA: progress in making colder ingredients

**main challenge now:** enough cold enough constituents

individual antihydrogen atoms trapped in the ground state (2010)

assuming 1 mK: 1s-2s spectroscopy to  $\sim 10^{-12}$  (perhaps in a few years)

first (rough) HFS measurements perhaps in 2011 or 2012

### Beam of antihydrogen:

ASACUSA: continuous beam (2011?)

AEGIS: pulsed sub-K beam (2012/2013) @ 1 Hz

**main challenge now:** formation mechanisms and rates

these may allow in-flight spectroscopy of

HFS to 200 Hz ( $10^{-6}$ )

1s-2s spectroscopy to ??? (will depend on temperature of  $\bar{\text{H}}$ )

and may also lead to an alternative  $\bar{\text{H}}$  trapping scheme

**Soon: New infrastructure (ELENA) and experiments**

