

Scalar Dark Matter

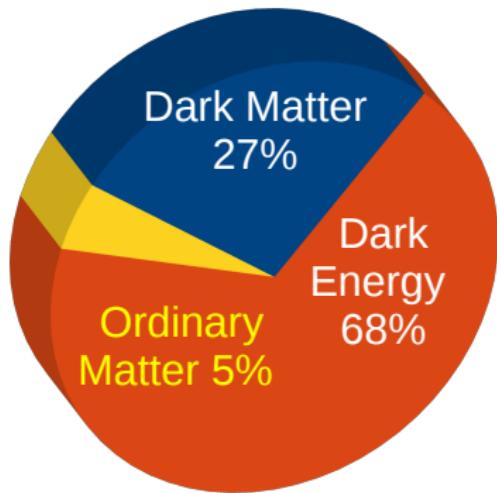
Laura Lopez Honorez

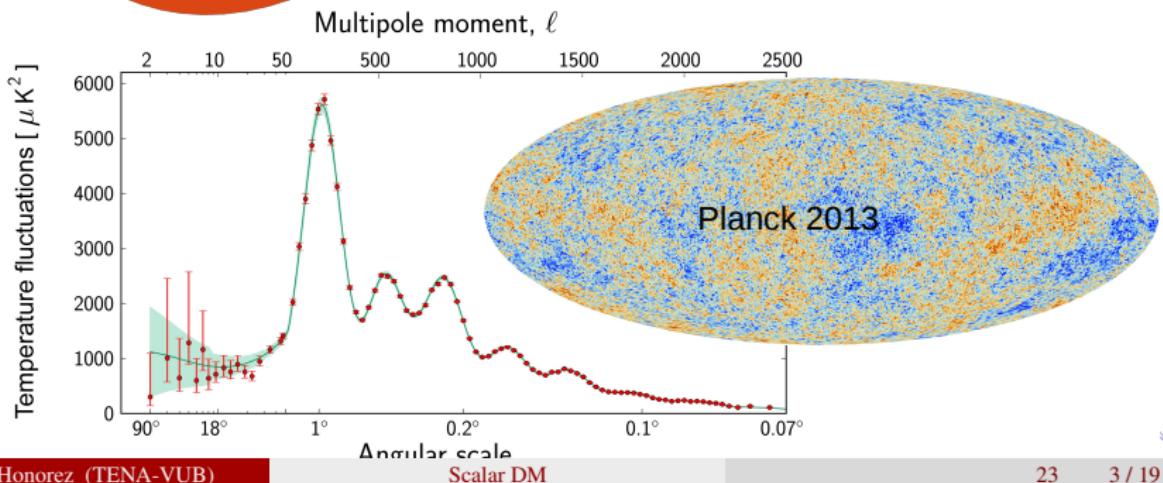
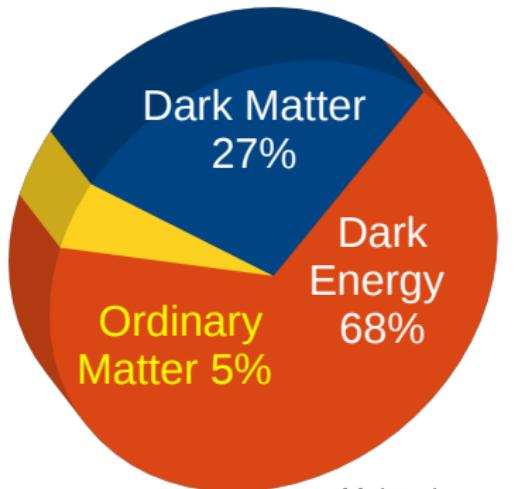


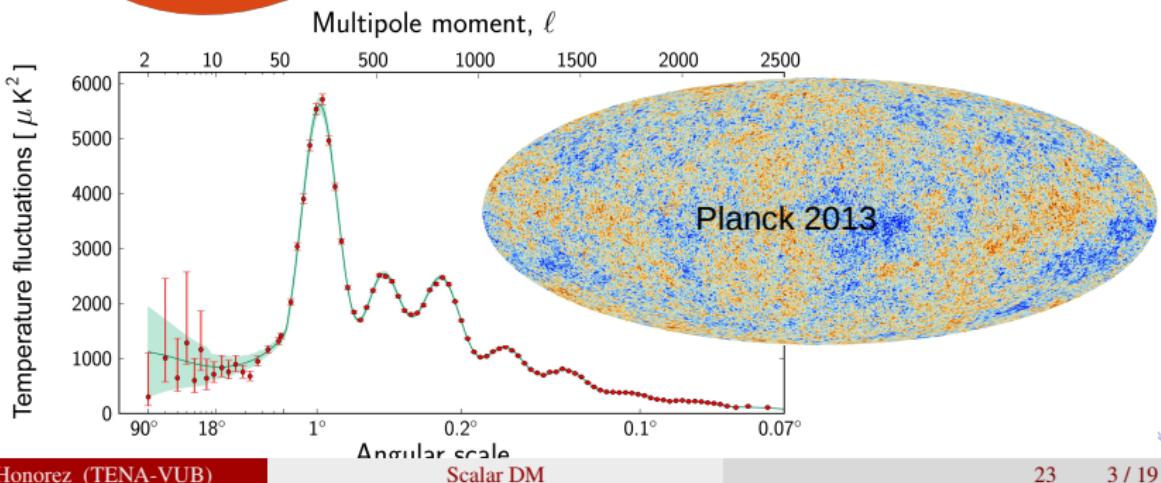
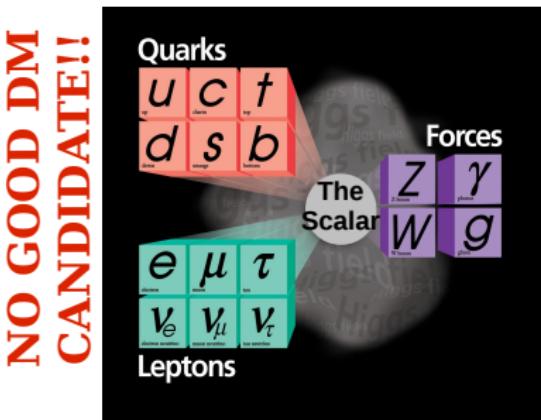
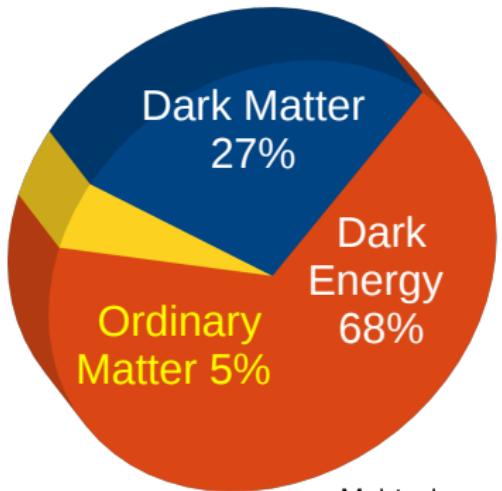
Vrije
Universiteit
Brussel

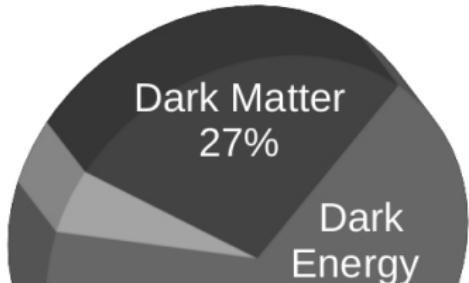
Mini-workshop on scalar sector in Belgium

What is the Universe made of?

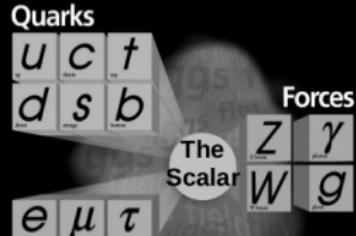








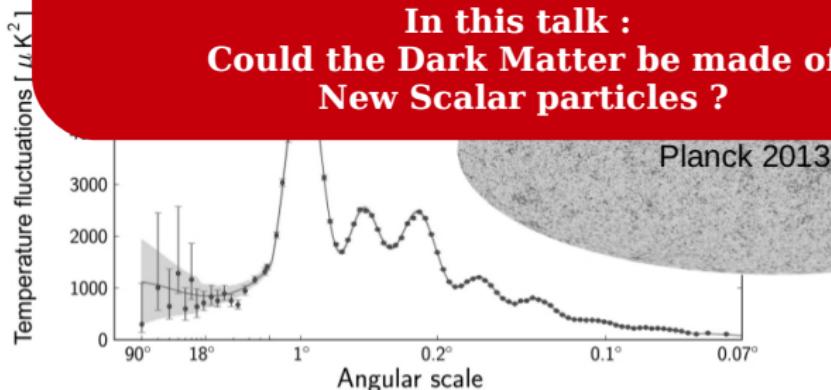
**GOOD DM
CANDIDATE!!**



**95 % of the Matter-Energy budget of the Universe
is UNKNOWN**

~84 % of the Matter Content is made of Dark Matter

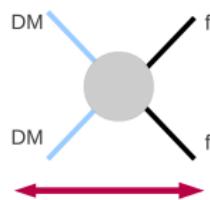
**In this talk :
Could the Dark Matter be made of
New Scalar particles ?**



Focus on WIMPs

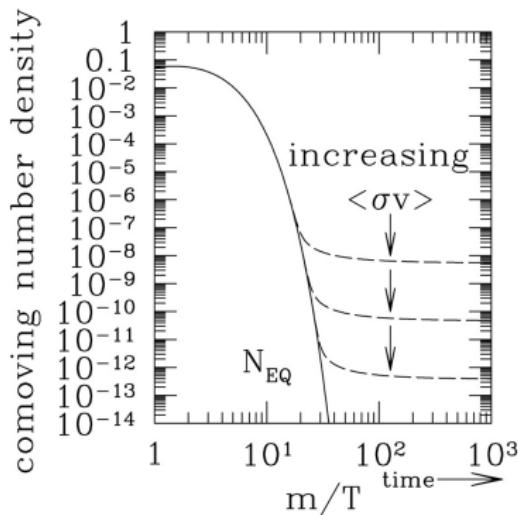
Weakly Interacting Massive Particles

- WIMP relic abundance is driven by :



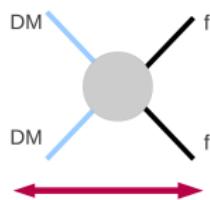
Freeze-out mechanism :

$$\rightsquigarrow \Omega h^2 \propto 1/\langle\sigma v\rangle$$



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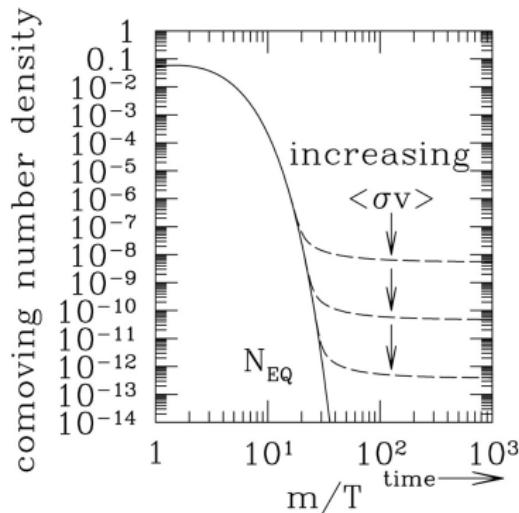


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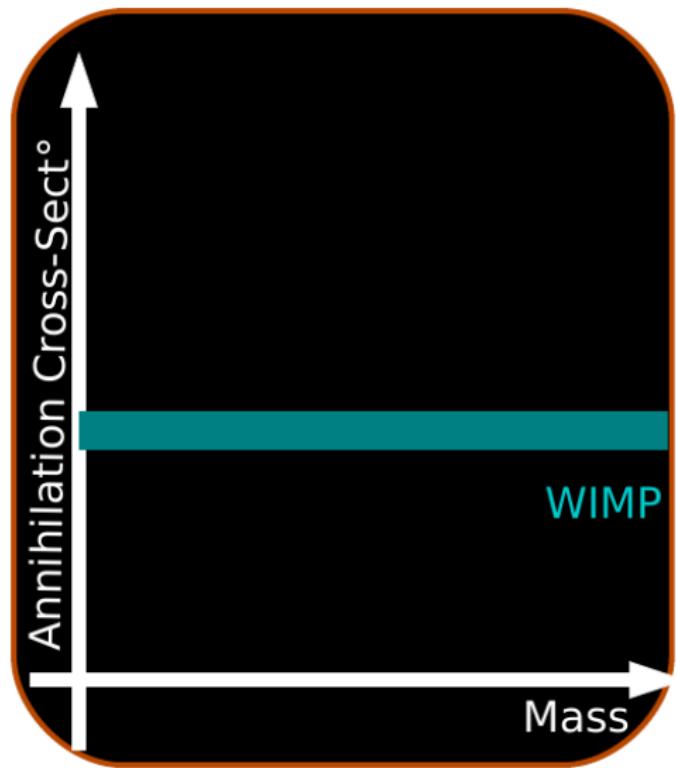
- Cosmo observations ($\Omega h^2 \sim 0.11$) can be interpreted as

$$\langle\sigma v\rangle \sim 3 \cdot 10^{-26} \text{ cm}^3/\text{s}$$

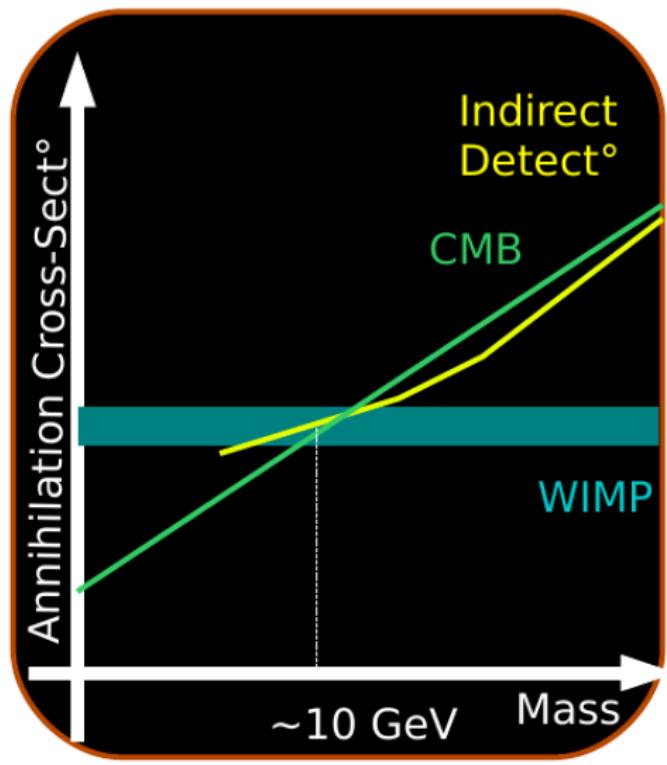
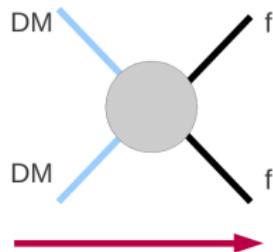
\rightsquigarrow target value for detection experiments
 looking for annihilation products of WIMPs



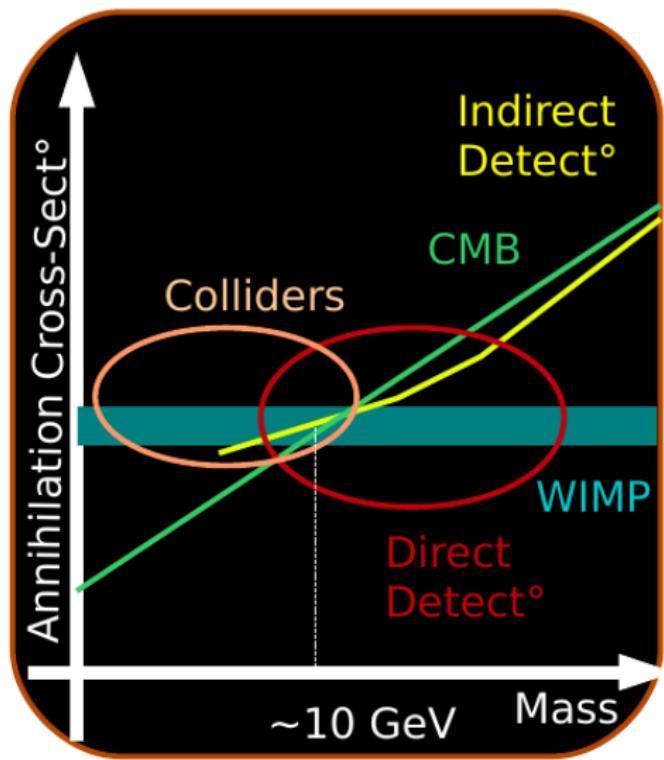
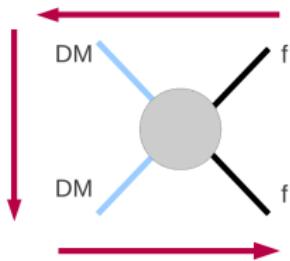
WIMP tests



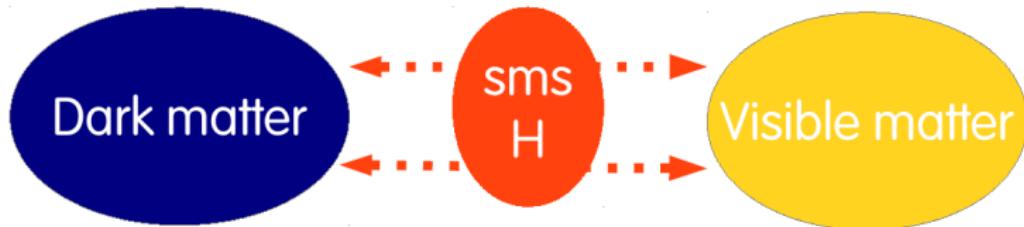
WIMP tests



WIMP tests



Worked Examples with SMS Portal



$(H^\dagger H)$ - dark sector operators drive the SM-DM interactions

[Silveira & Zee'85 ; McDonald'94 ; Burgess, Pospelov & ter Veldhuis'00 ; Patt & Wilczek'06 ; Barger et al'08 ; Andreas, Hambye, Tytgat'08,...]

Scalar Singlet of $SU(2)_L \times U(1)$

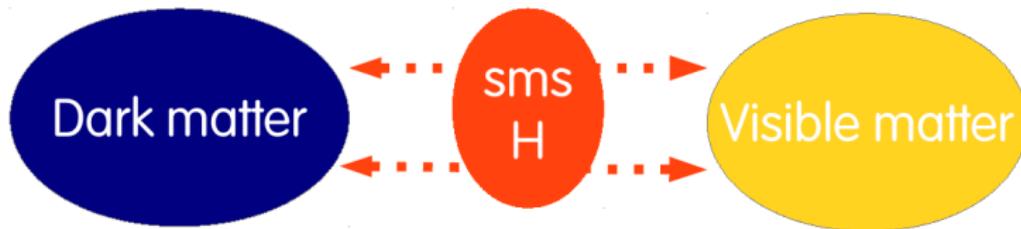
SMS portal with singlet scalar DM



DM = SM singlet scalar S :

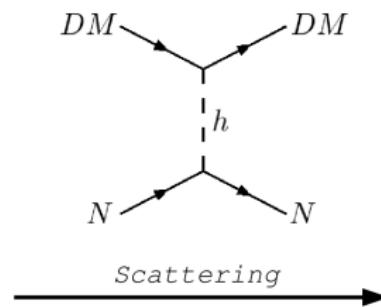
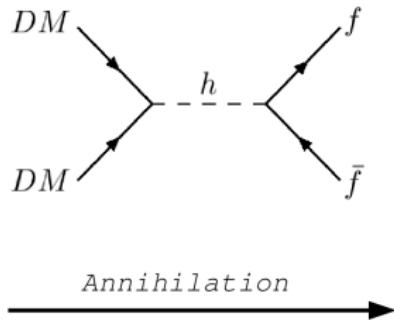
- DM stability : Z_2 symmetry
- sms-DM interactions : $\lambda_S S^2 (H^\dagger H)$

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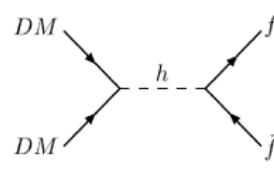
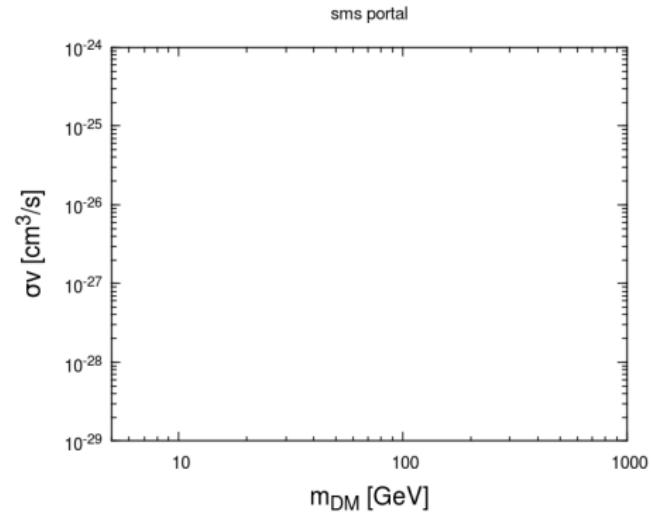
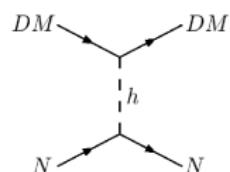
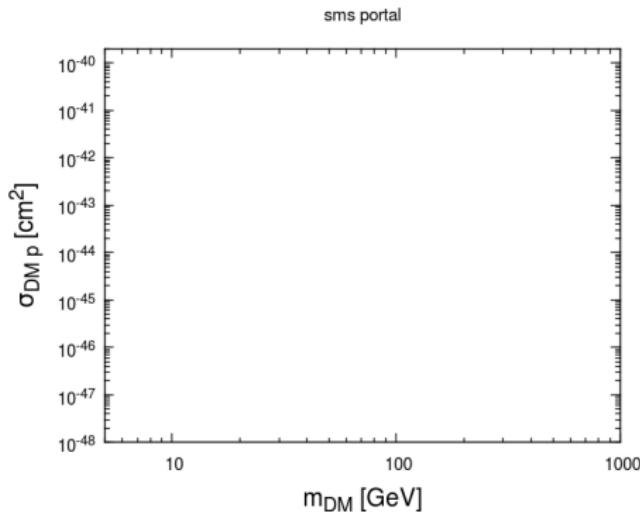


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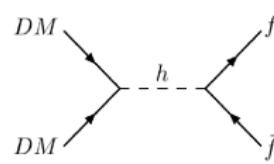
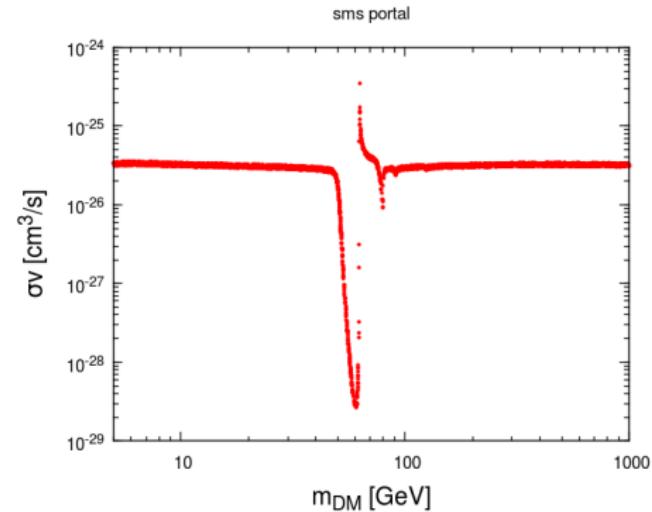
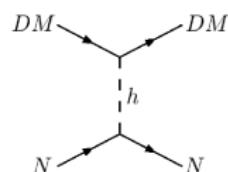
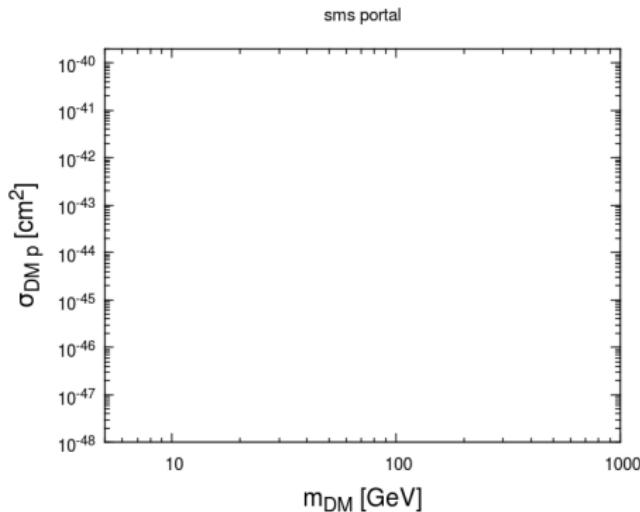
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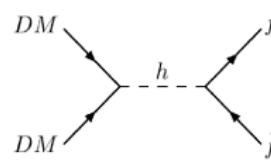
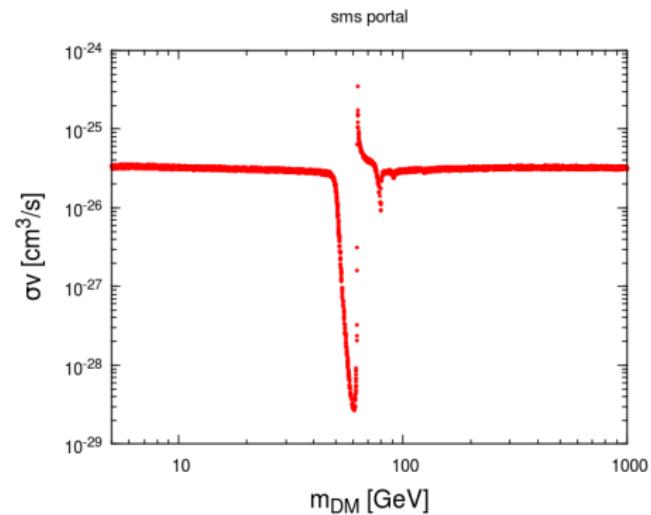
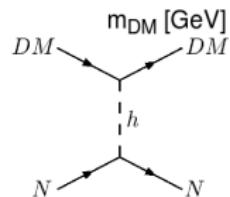
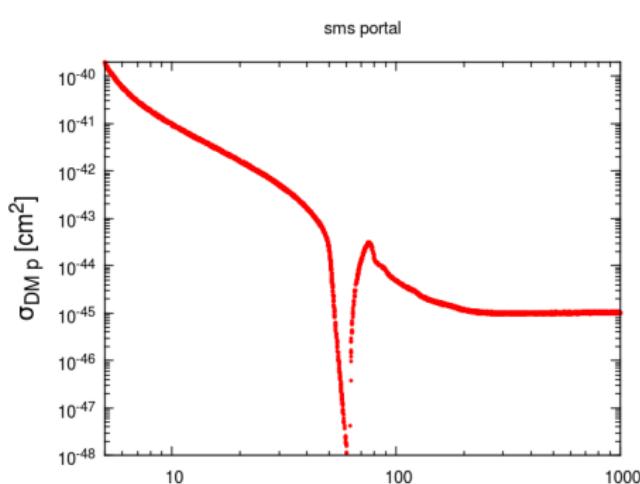
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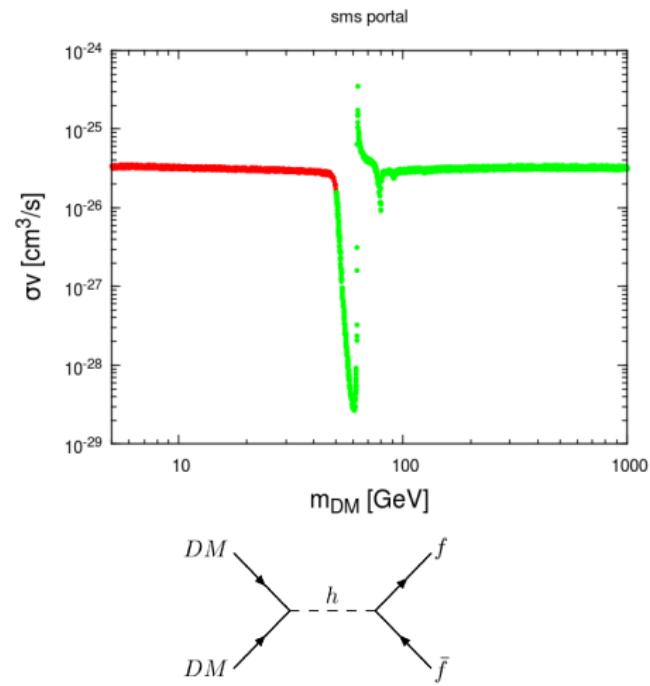
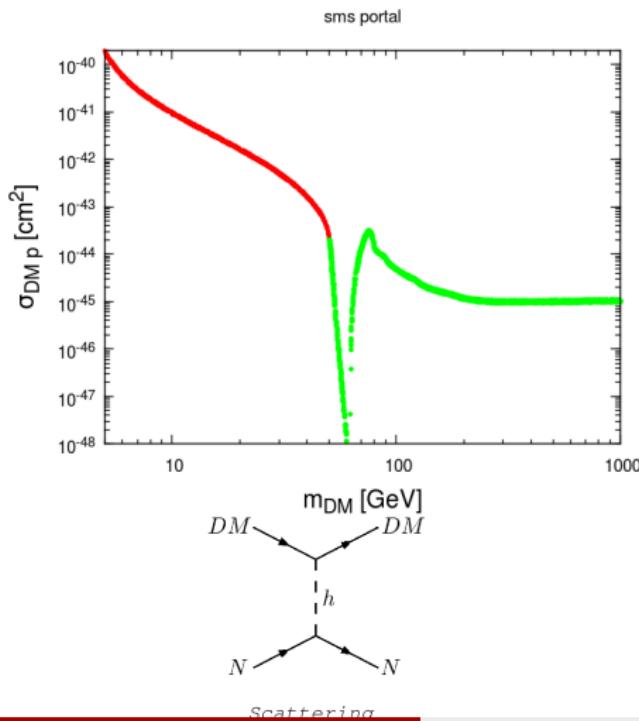


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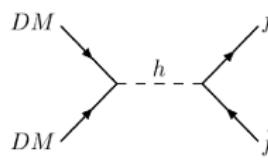
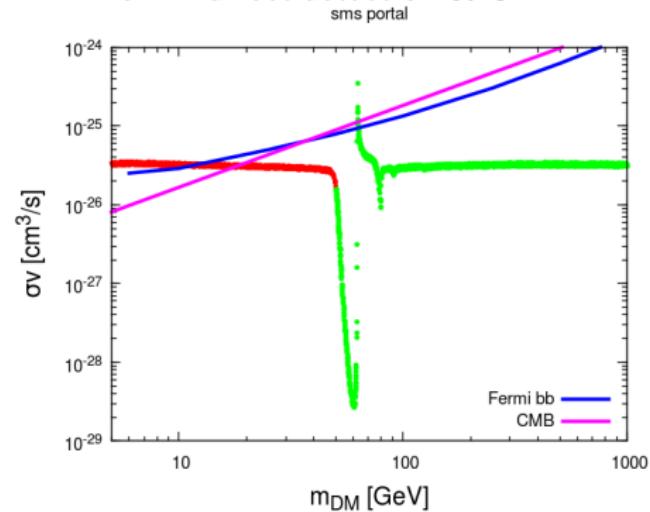
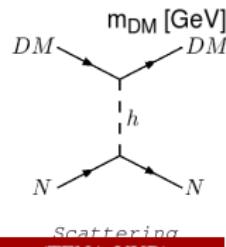
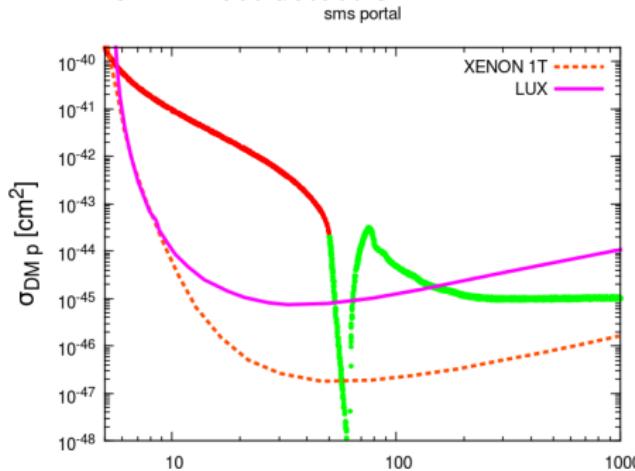
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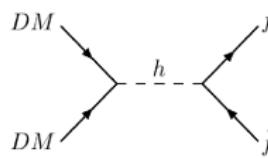
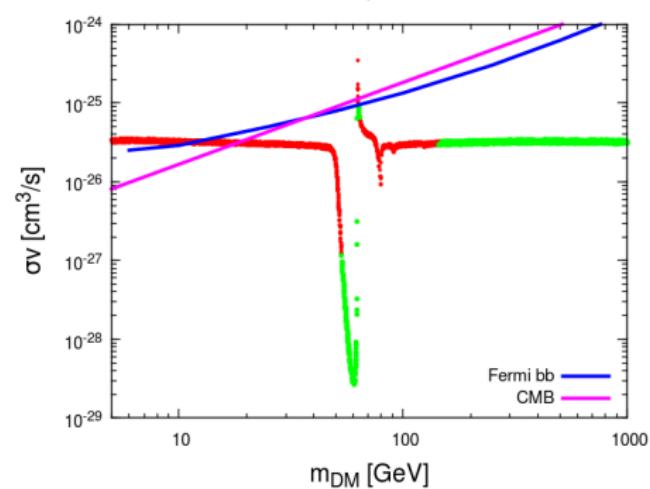
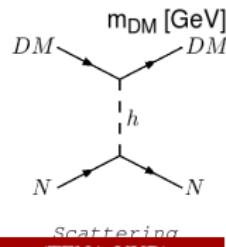
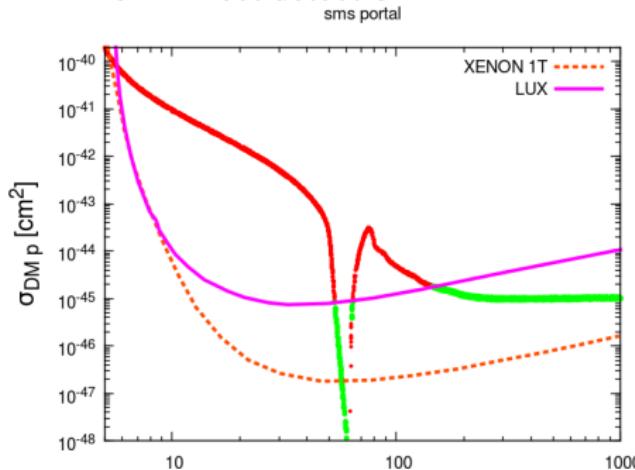
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Scalar n-plet of $SU(2)_L \times U(1)$

Scalar DM model

- Extra n -uplet case ($n > 2$) :
 - only one coupling to the Higgs $\lambda_3 |H_1|^2 |H_n|^2$
 - no mass splittings between H_n^0 and $H_n^{\pm(\dots\pm)}$

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- Particular case :  $n = 2 \equiv \text{IDM}$

- three couplings to the Higgs.

$$\lambda_3 |H_1|^2 |H_2|^2 + \lambda_4 |H_1^\dagger H_2|^2 + \frac{\lambda_5}{2} [(H_1^\dagger H_2)^2 + h.c.]$$

- non zero mass splittings :

$$H_2 = \begin{pmatrix} iH^+ \\ \frac{(H_0 - iA_0)}{\sqrt{2}} \end{pmatrix} \quad H_1 = \begin{pmatrix} 0 \\ \frac{(h+v_0)}{\sqrt{2}} \end{pmatrix}$$

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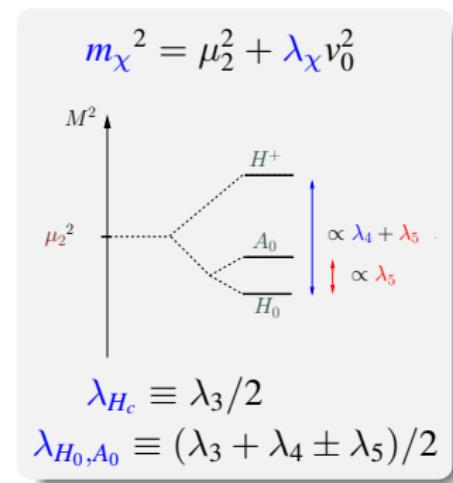
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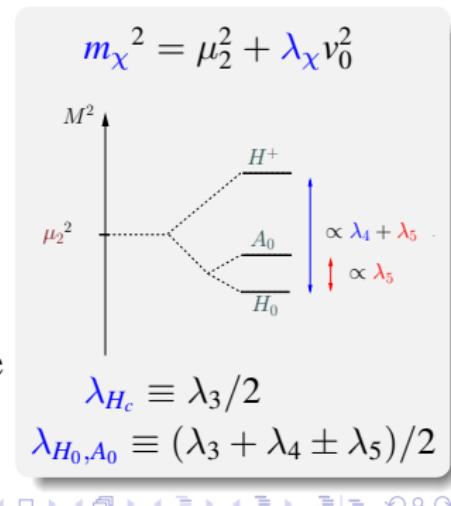
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$\rightsquigarrow$  viable mass ranges  $m_{H_0} \sim \text{GeV-TeV}$  range

We will refer to  $H_0 - h$  coupling as  $\lambda_{H_0} = \lambda_L$

Free parameters :  $m_{H_0}, \lambda_L, \Delta m_{A^0}, \Delta m_{H^+}$

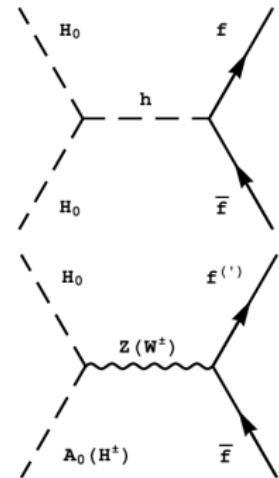


# Inert doublet model parameter space

- $m_{H_0} \lesssim m_W$  : GeV range

$$H_0 H_0 \rightarrow h^* \rightarrow \bar{f}f \text{ and } H_0 A_0 \rightarrow Z^* \rightarrow \bar{f}f$$

Barbieri PRD06, LLH JCAP06, Gustafsson PRL07, Cao PRD07, Andreas JCAP08,...

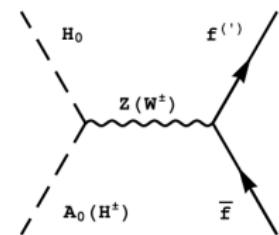
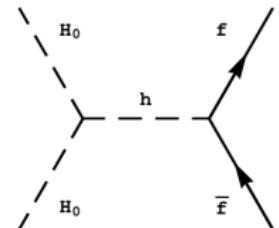


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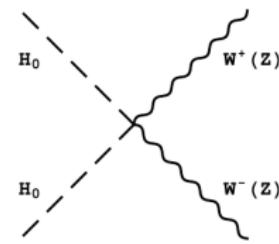
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$H_0 H_0 \rightarrow ZZ, WW, hh$  and coannihil into bosons

Cirelli NPB06, Hambye, Ling, LLH & Rocher JHEP09

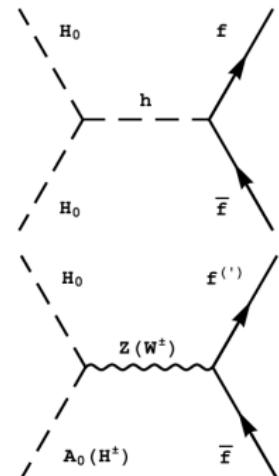


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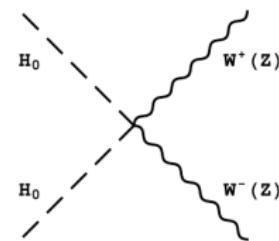


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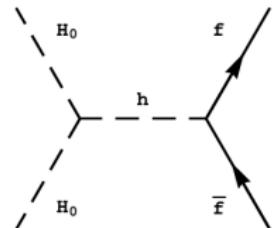


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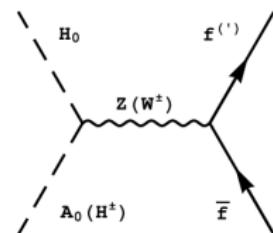
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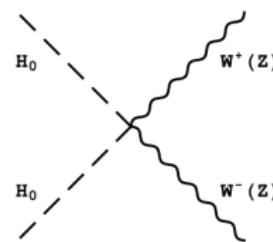
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Significantly affected by 3bdy annihilation :

$$H_0 H_0 \rightarrow WW^* \rightarrow W\bar{f}f' \text{ LLH & Yaguna JHEP10}$$

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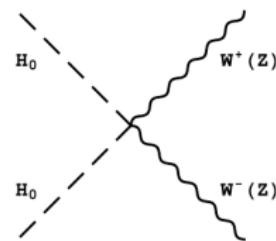
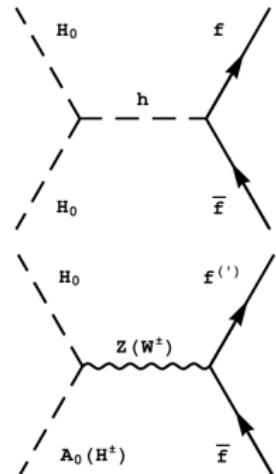
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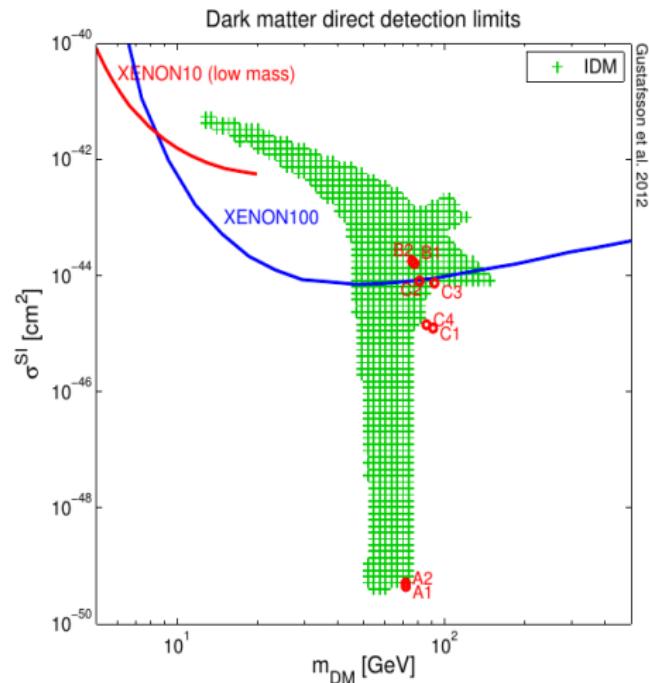
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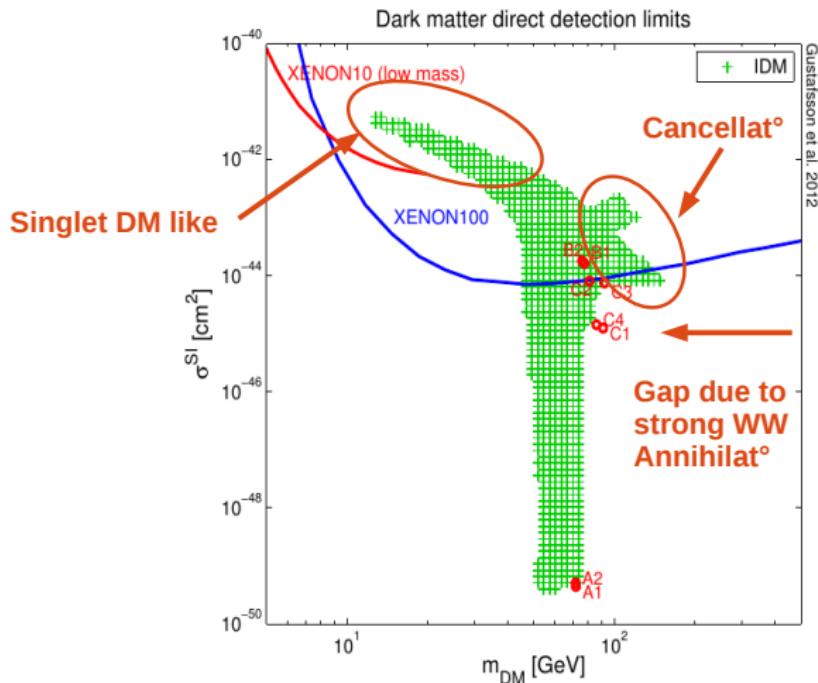


# Inert doublet model : viable parameter space



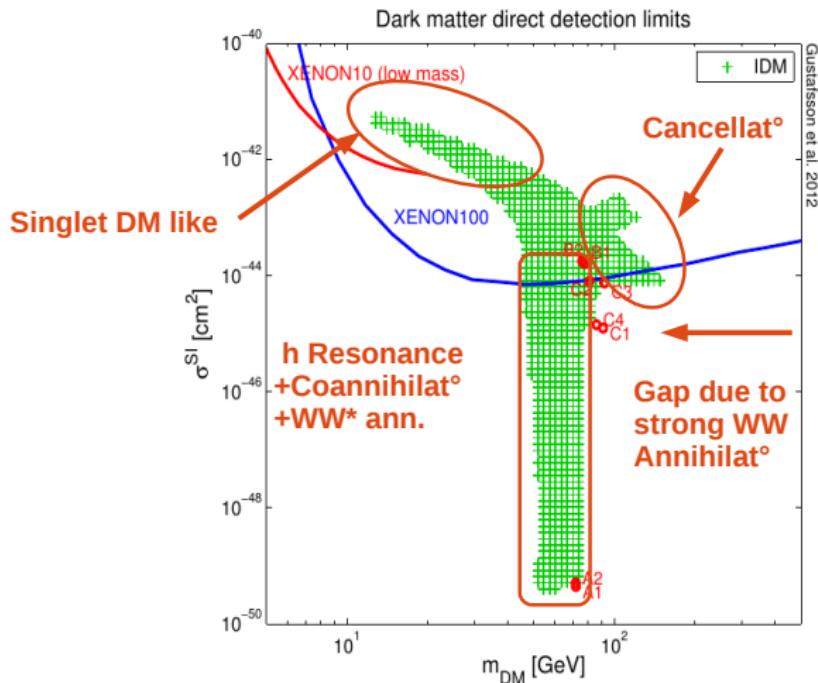
[Gustafsson, Rydbeck, LLH, Lundstrom PRD'12]

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[Gustafsson, Rydbeck, LLH, Lundstrom PRD'12]

# Inert doublet model : viable parameter space



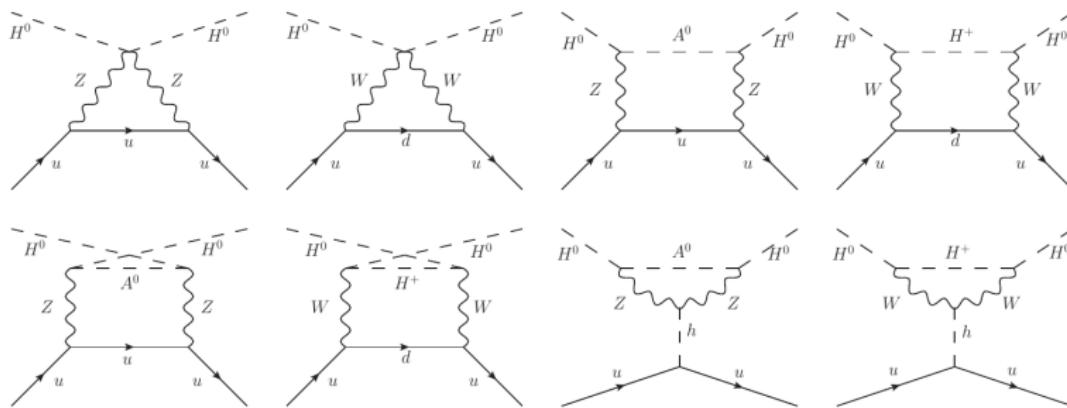
[Gustafsson, Rydbeck, LLH, Lundstrom PRD'12]

# Loop Corrections in the IDM

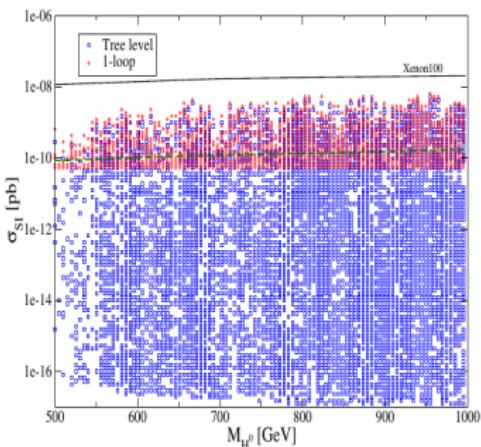
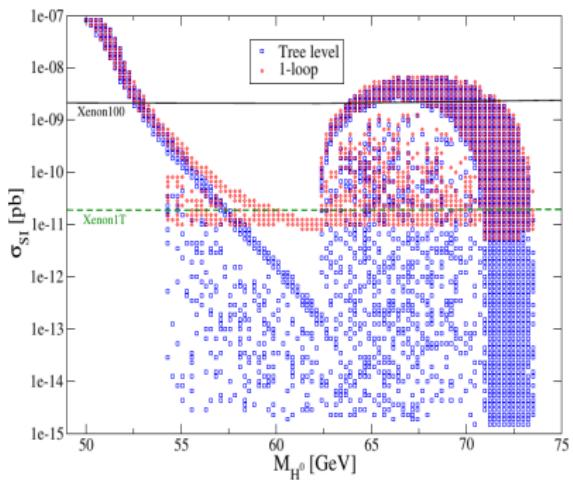
based on : arXiv :1302.1657, Yaguna et al.

# Important loop corrections due to gauge processes

$$V = \mu_1^2 |H_1|^2 + \mu_2^2 |H_2|^2 + \lambda_1 |H_1|^4 + \lambda_2 |H_2|^4 + \lambda_3 |H_1|^2 |H_2|^2 \\ + \lambda_4 |H_1^\dagger H_2|^2 + \frac{\lambda_5}{2} [(H_1^\dagger H_2)^2 + \text{h.c.}] ,$$



# Effect on Spin Independent scattering cross-section



# Conclusion

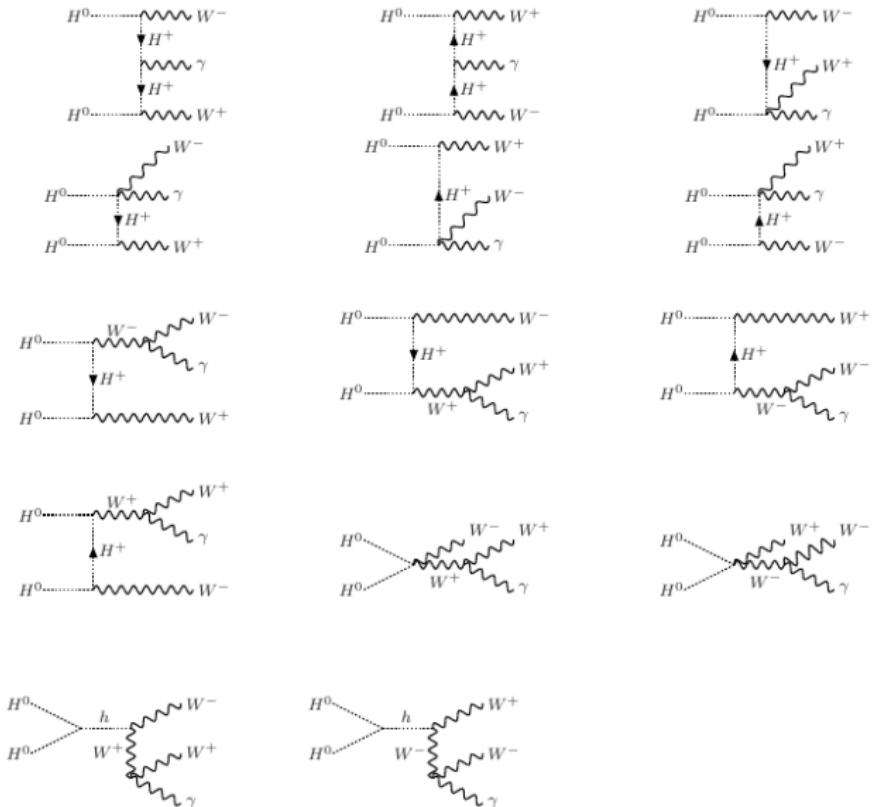
- Cosmo : Compiling cosmological probes tell us that **95% of the Universe content is unknown**. Dark matter would make **84% of the matter content** but its true nature still obscure.
- Particle : Up to now no convincing evidence for a given candidate BUT **DM searches are now seriously digging into the viable WIMP DM parameter space**.
- SMS portal a worked example :
  - **Low mass dark matter** ( $5 \lesssim m_{DM} \lesssim 40$  GeV) is now **excluded** by the combination of Direct, Indirect and Collider searches
  - **Middle mass regime** ( $40 \lesssim m_{DM} \lesssim 100$  GeV) is seriously **threatened** by direct detection searches a part for resonant annihilation or coannihilations
  - **Large mass regime** will be **tested up to  $\sim$  TeV range** by future Direct detection experiments

Thank you for your attention !!!

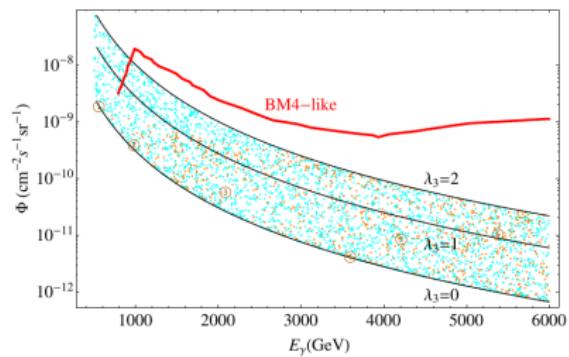
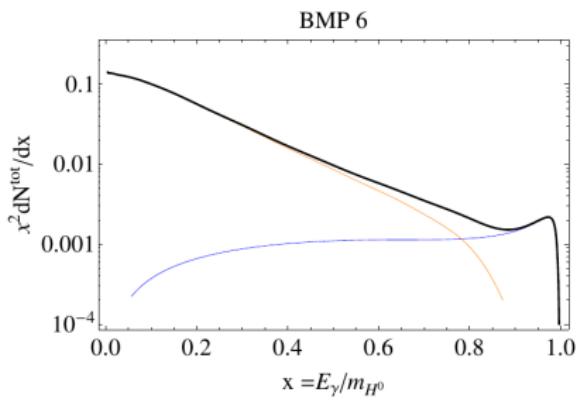
# Backup

## Detection & Constraints

# spectral features with Bremsstrahlung (Garcia-Cely '13)

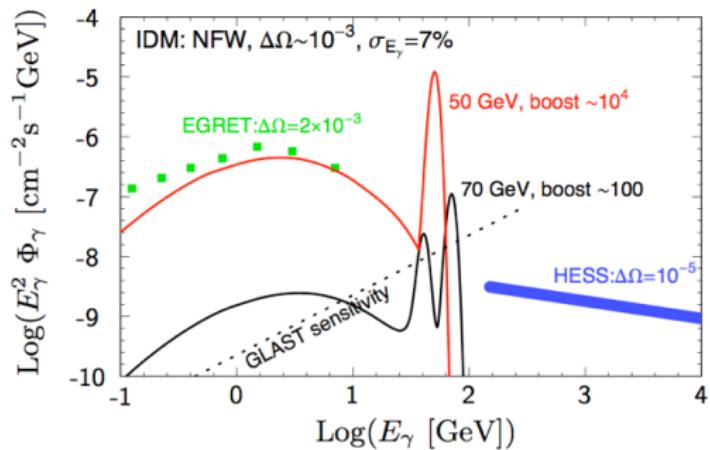


# spectral features with Bremsstrahlung (Garcia-Cely '13)



# Gamma ray lines in the IDM

## «Significant gamma-ray line from Inert Doublet»



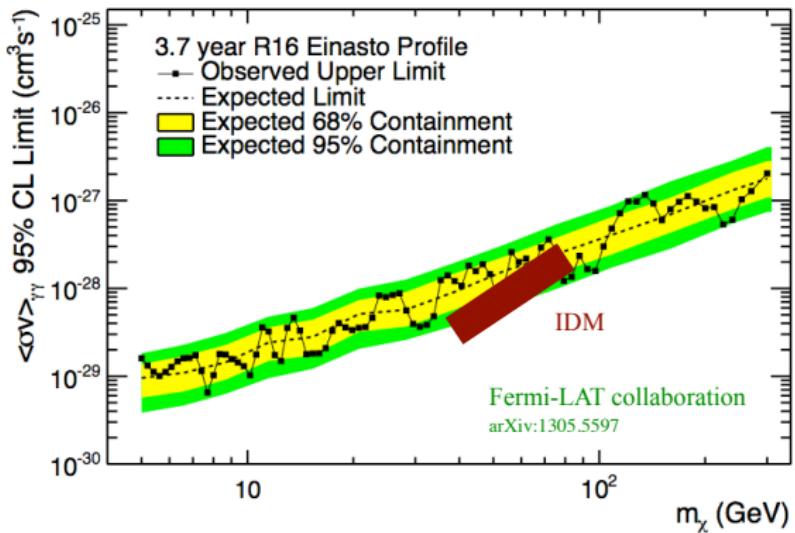
Gustafsson, Bergstrom,  
Lundstrom & Edsjo  
Phys.Rev.Lett. 99 (2007) 041301

$M_{\text{higgs}} \sim 500 \text{ GeV}$

TABLE II: IDM benchmark model results.

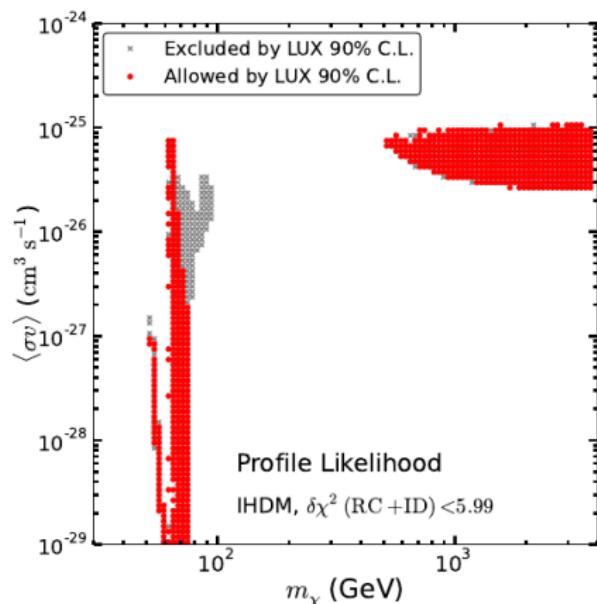
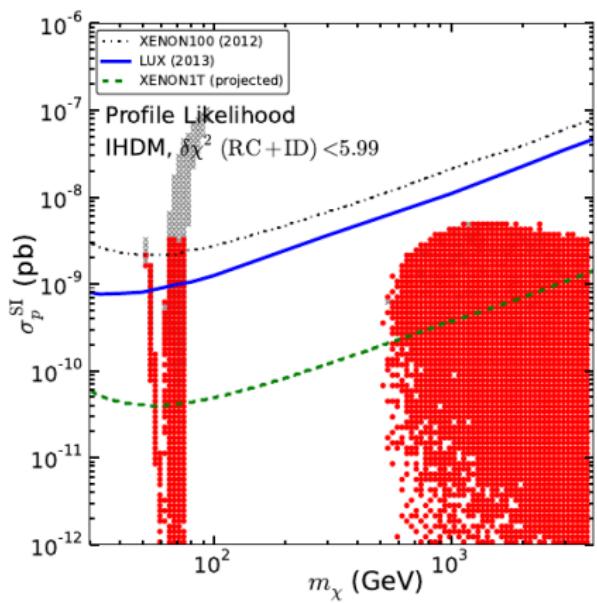
| Model | $v\sigma_{tot}^{v \rightarrow 0}$<br>[cm <sup>3</sup> s <sup>-1</sup> ] | Branching ratios [%]: |           |            |            |                | $\Omega_{\text{CDM}} h^2$ |
|-------|-------------------------------------------------------------------------|-----------------------|-----------|------------|------------|----------------|---------------------------|
|       |                                                                         | $\gamma\gamma$        | $Z\gamma$ | $b\bar{b}$ | $c\bar{c}$ | $\tau^+\tau^-$ |                           |
| I     | $1.6 \times 10^{-28}$                                                   | 36                    | 33        | 26         | 2          | 3              | 0.10                      |
| II    | $8.2 \times 10^{-29}$                                                   | 29                    | 0.6       | 60         | 4          | 7              | 0.10                      |
| III   | $8.7 \times 10^{-27}$                                                   | 2                     | 2         | 81         | 5          | 9              | 0.12                      |
| IV    | $1.9 \times 10^{-26}$                                                   | 0.04                  | 0.1       | 85         | 5          | 10             | 0.11                      |

## CURRENT EXPERIMENTAL LIMITS



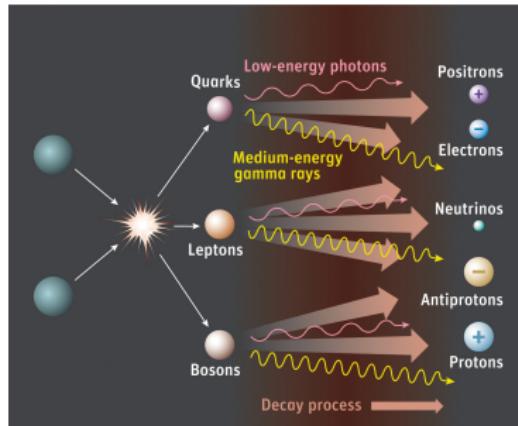
Fermi-LAT limits on gamma ray lines

# Latest analysis of the IDM- Tsai '13



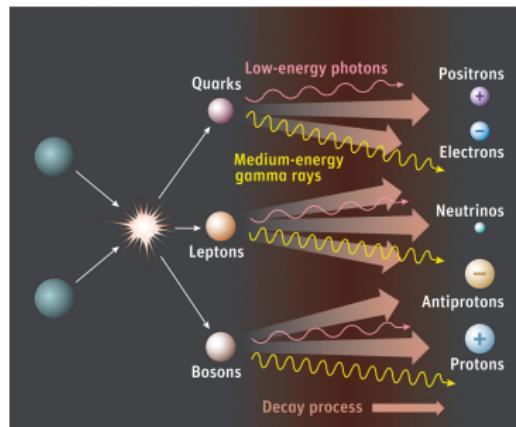
# Making use of dark matter annihilation

DM annihilation driving the relic abundance also give rise to  $\gamma, \nu, p^\pm, e^\pm$  production that is constrained :



# Making use of dark matter annihilation

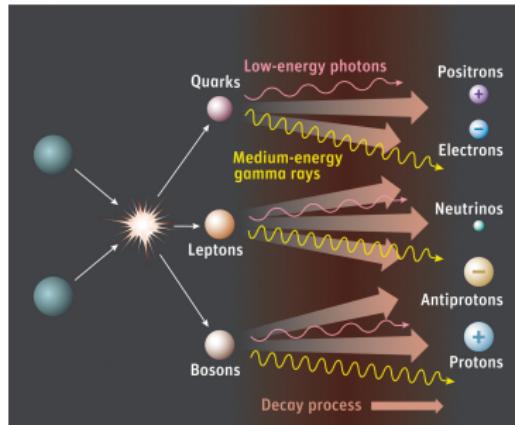
DM annihilation driving the relic abundance also give rise to  $\gamma, \nu, p^\pm, e^\pm$  production that is constrained :



- *today* by Indirect detection searches :
  - ~~ Among the latter **Fermi-Lat** limits for gamma rays from **dwarf spheroidal galaxies** are the most constraining

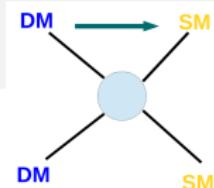
# Making use of dark matter annihilation

DM annihilation driving the relic abundance also give rise to  $\gamma, \nu, p^\pm, e^\pm$  production that is constrained :

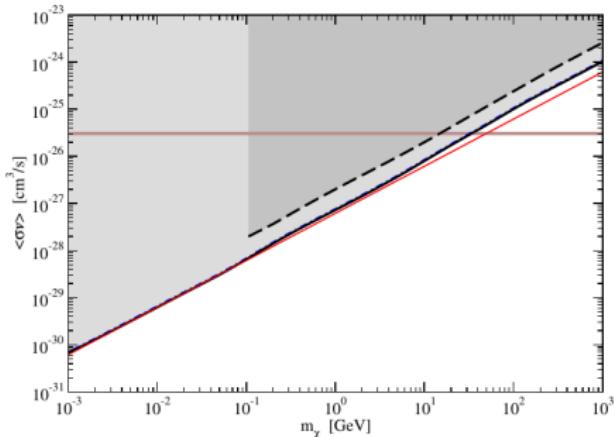


- *today* by Indirect detection searches :
  - ~~ Among the latter Fermi-Lat limits for gamma rays from dwarf spheroidal galaxies are the most constraining
- *at early times (z=1000)* by CMB :
  - ~~ Energy losses in the IGM at epoch of recombination
  - ~~ affects recombination history
  - ~~ impact on CMB anisotropy spectrum at high multipoles.

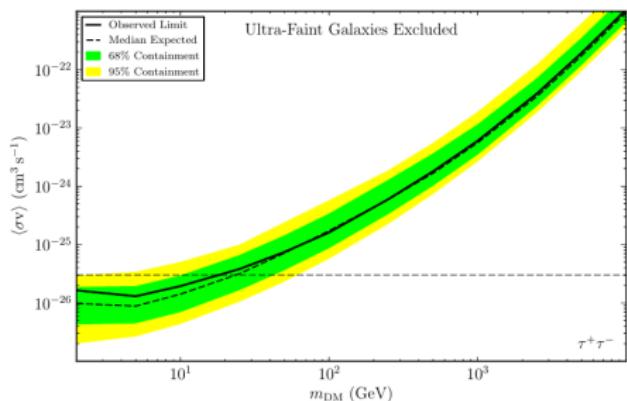
# Making use of dark matter annihilation



## Constraints from CMB



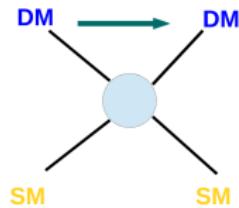
## Constraints from Fermi-Lat



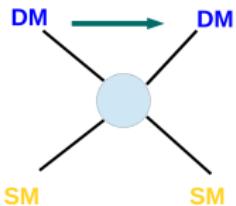
upper bounds using  
WMAP9+SPT/ACT 12+HST+BAO  
[LLH, Mena, Palomares-Ruiz, Vincent '13]

upper bound using 20 dwarfs and 200  
MeV-100 GeV gamma rays  
[ Fermi-LAT Collaboration PRL '13]

# Direct Detection

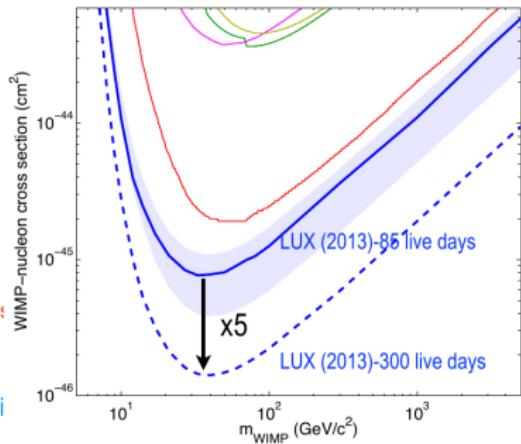
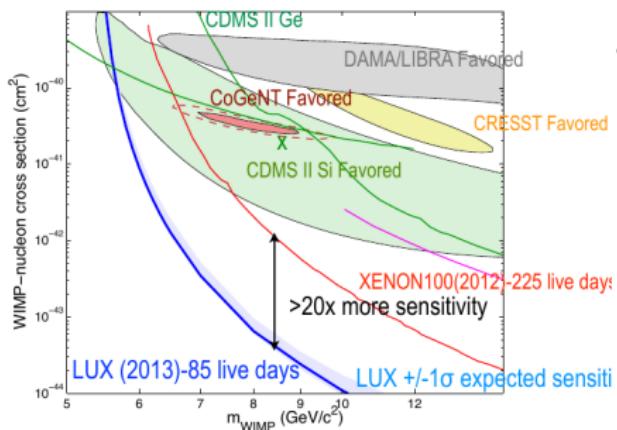


# Direct Detection



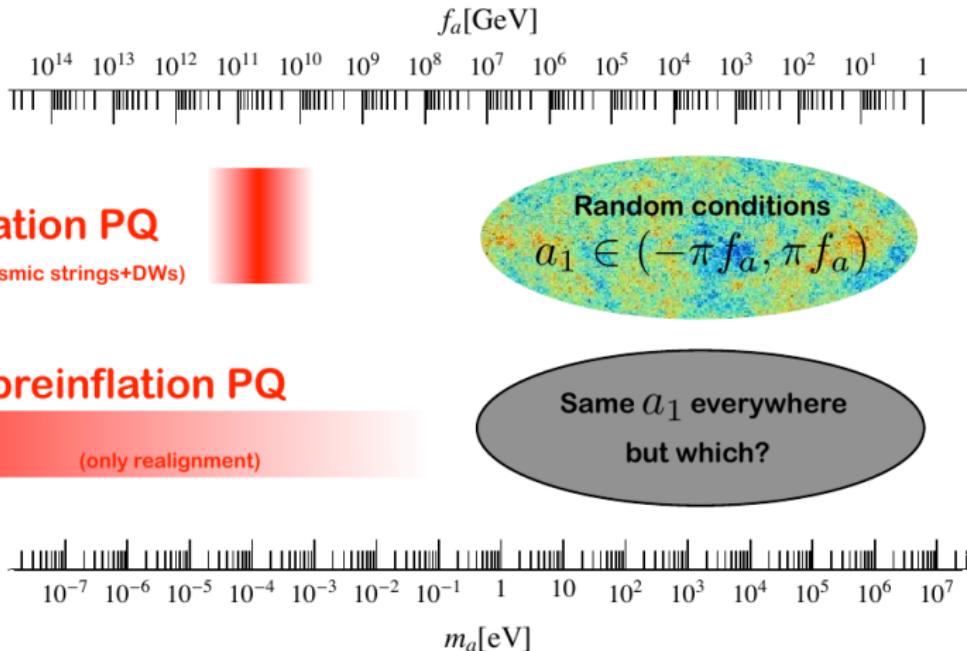
Upper bound on the DM scattering cross-section on  
Nucleons in Underground detectors

[Akerib et al '13]



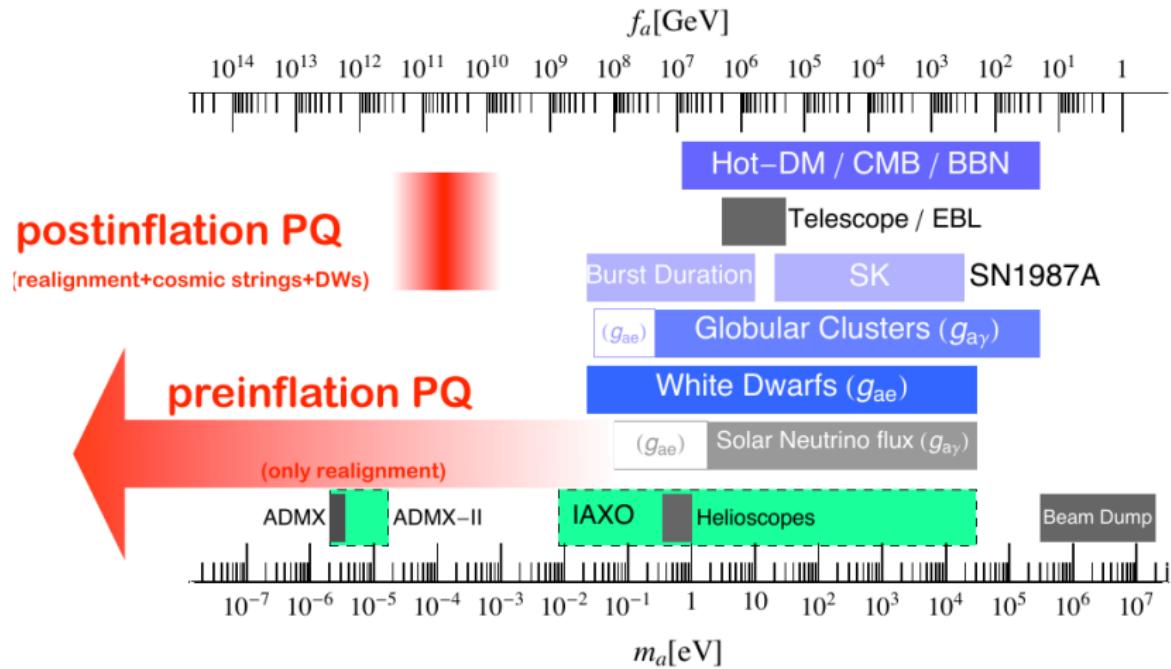
# Axion DM (courtesy J. Redondo)

## QCD axion cold dark matter (two scenarios)



# Axion DM (courtesy J. Redondo)

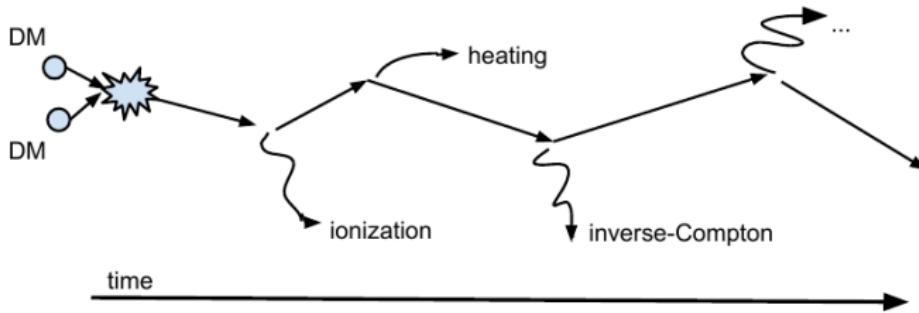
+ Bounds on axions (and prospects)



# DM impact on CMB

## Proper calculation of the deposition efficiency

- ➊ At a given redshift  $z$ , calculate the final-state spectrum  $dN_i/dE_i$  for  $i = \{e^+, e^-, \gamma\}$
- ➋ Calculate the energy loss to (inverse) Compton scattering, Coulomb scattering, (photo) ionization or pair-production for each species.
- ➌ Step forward to the next value of  $z$ , given the new  $E_i = E_{i,0} - E(z)'dz$ , including loss to IGM and to redshift.
- ➍ Repeat.



# DM impact on CMB

- Dark matter annihilation rate is proportional to  $(1 + z)^6$ , which leads to a dependence of

$$\sqrt{1 + z} \quad (2)$$

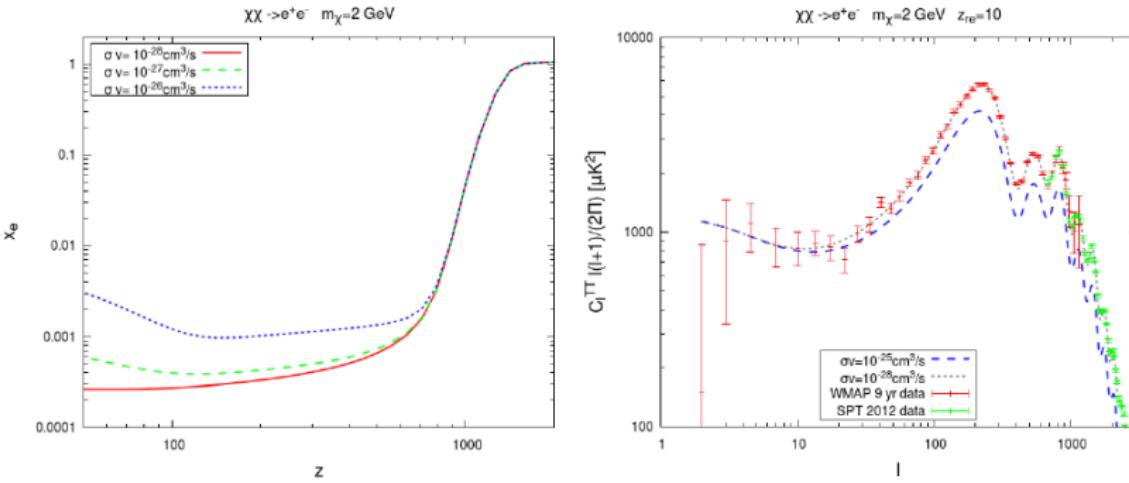
for the heating and ionization rates. Therefore dominates in the early Universe. Around  $z = 1100$ , the extra energy injection has the effect of **delaying recombination**.

- This **broadens the last scattering surface**. This can be seen as a broadening of the CMB's "focal plane": you can still resolve large structures, but smaller details become blurred:  $\Rightarrow$  **suppression of the correlations at high multipoles**.
- This is **degenerate** with a change in the scalar spectral index  $n_s$ .
- This can be disentangled by late-time effects.

courtesy

of A. Vincent

# DM impact on CMB



courtesy

of A. Vincent

| Parameter                   | <i>Planck</i> |                       | <i>Planck+lensing</i> |                        | <i>Planck+WP</i> |                           |
|-----------------------------|---------------|-----------------------|-----------------------|------------------------|------------------|---------------------------|
|                             | Best fit      | 68% limits            | Best fit              | 68% limits             | Best fit         | 68% limits                |
| $\Omega_b h^2$              | 0.022068      | $0.02207 \pm 0.00033$ | 0.022242              | $0.02217 \pm 0.00033$  | 0.022032         | $0.02205 \pm 0.00028$     |
| $\Omega_c h^2$              | 0.12029       | $0.1196 \pm 0.0031$   | 0.11805               | $0.1186 \pm 0.0031$    | 0.12038          | $0.1199 \pm 0.0027$       |
| $100\theta_{\text{MC}}$     | 1.04122       | $1.04132 \pm 0.00068$ | 1.04150               | $1.04141 \pm 0.00067$  | 1.04119          | $1.04131 \pm 0.00063$     |
| $\tau$                      | 0.0925        | $0.097 \pm 0.038$     | 0.0949                | $0.089 \pm 0.032$      | 0.0925           | $0.089^{+0.012}_{-0.014}$ |
| $n_s$                       | 0.9624        | $0.9616 \pm 0.0094$   | 0.9675                | $0.9635 \pm 0.0094$    | 0.9619           | $0.9603 \pm 0.0073$       |
| $\ln(10^{10} A_s)$          | 3.098         | $3.103 \pm 0.072$     | 3.098                 | $3.085 \pm 0.057$      | 3.0980           | $3.089^{+0.024}_{-0.027}$ |
| $\Omega_\Lambda$            | 0.6825        | $0.686 \pm 0.020$     | 0.6964                | $0.693 \pm 0.019$      | 0.6817           | $0.685^{+0.018}_{-0.016}$ |
| $\Omega_m$                  | 0.3175        | $0.314 \pm 0.020$     | 0.3036                | $0.307 \pm 0.019$      | 0.3183           | $0.315^{+0.016}_{-0.018}$ |
| $\sigma_8$                  | 0.8344        | $0.834 \pm 0.027$     | 0.8285                | $0.823 \pm 0.018$      | 0.8347           | $0.829 \pm 0.012$         |
| $z_{\text{re}}$             | 11.35         | $11.4^{+4.0}_{-2.8}$  | 11.45                 | $10.8^{+3.1}_{-2.5}$   | 11.37            | $11.1 \pm 1.1$            |
| $H_0$                       | 67.11         | $67.4 \pm 1.4$        | 68.14                 | $67.9 \pm 1.5$         | 67.04            | $67.3 \pm 1.2$            |
| $10^9 A_s$                  | 2.215         | $2.23 \pm 0.16$       | 2.215                 | $2.19^{+0.12}_{-0.14}$ | 2.215            | $2.196^{+0.051}_{-0.066}$ |
| $\Omega_m h^2$              | 0.14300       | $0.1423 \pm 0.0029$   | 0.14094               | $0.1414 \pm 0.0029$    | 0.14305          | $0.1426 \pm 0.0025$       |
| $\Omega_m h^3$              | 0.09597       | $0.09590 \pm 0.00059$ | 0.09603               | $0.09593 \pm 0.00058$  | 0.09591          | $0.09589 \pm 0.00057$     |
| $Y_P$                       | 0.247710      | $0.24771 \pm 0.00014$ | 0.247785              | $0.24775 \pm 0.00014$  | 0.247695         | $0.24770 \pm 0.00012$     |
| Age/Gyr                     | 13.819        | $13.813 \pm 0.058$    | 13.784                | $13.796 \pm 0.058$     | 13.8242          | $13.817 \pm 0.048$        |
| $z_*$                       | 1090.43       | $1090.37 \pm 0.65$    | 1090.01               | $1090.16 \pm 0.65$     | 1090.48          | $1090.43 \pm 0.54$        |
| $r_*$                       | 144.58        | $144.75 \pm 0.66$     | 145.02                | $144.96 \pm 0.66$      | 144.58           | $144.71 \pm 0.60$         |
| $100\theta_*$               | 1.04139       | $1.04148 \pm 0.00066$ | 1.04164               | $1.04156 \pm 0.00066$  | 1.04136          | $1.04147 \pm 0.00062$     |
| $z_{\text{drag}}$           | 1059.32       | $1059.29 \pm 0.65$    | 1059.59               | $1059.43 \pm 0.64$     | 1059.25          | $1059.25 \pm 0.58$        |
| $r_{\text{drag}}$           | 147.34        | $147.53 \pm 0.64$     | 147.74                | $147.70 \pm 0.63$      | 147.36           | $147.49 \pm 0.59$         |
| $k_D$                       | 0.14026       | $0.14007 \pm 0.00064$ | 0.13998               | $0.13996 \pm 0.00062$  | 0.14022          | $0.14009 \pm 0.00063$     |
| $100\theta_D$               | 0.161332      | $0.16137 \pm 0.00037$ | 0.161196              | $0.16129 \pm 0.00036$  | 0.161375         | $0.16140 \pm 0.00034$     |
| $z_{\text{eq}}$             | 3402          | $3386 \pm 69$         | 3352                  | $3362 \pm 69$          | 3403             | $3391 \pm 60$             |
| $100\theta_{\text{eq}}$     | 0.8128        | $0.816 \pm 0.013$     | 0.8224                | $0.821 \pm 0.013$      | 0.8125           | $0.815 \pm 0.011$         |
| $r_{\text{drag}}/D_V(0.57)$ | 0.07130       | $0.0716 \pm 0.0011$   | 0.07207               | $0.0719 \pm 0.0011$    | 0.07126          | $0.07147 \pm 0.00091$     |

**Table 2.** Cosmological parameter values for the six-parameter base  $\Lambda$ CDM model. Columns 2 and 3 give results for the *Planck* temperature power spectrum data alone. Columns 4 and 5 combine the *Planck* temperature data with *Planck* lensing, and columns 6 and 7 include WMAP polarization at low multipoles. We give best fit parameters as well as 68% confidence limits for constrained parameters. The first six parameters have flat priors. The remainder are derived parameters as discussed in Sect. 2. Beam, calibration



This is really the end