



Vrije
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Natural SUSY and the 125.5 GeV Higgs

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The MSSM

3-generations:
stops are typically the
lightest
coloured
superpartners



Names		spin 0	spin 1/2	$SU(3)_C, SU(2)_L, U(1)_Y$
squarks, quarks ($\times 3$ families)	Q	$(\bar{u}_L \ \bar{d}_L)$	$(u_L \ d_L)$	$(\mathbf{3}, \mathbf{2}, \frac{1}{6})$
	\bar{u}	\bar{u}_R^*	u_R^\dagger	$(\bar{\mathbf{3}}, \mathbf{1}, -\frac{2}{3})$
	\bar{d}	\bar{d}_R^*	d_R^\dagger	$(\bar{\mathbf{3}}, \mathbf{1}, \frac{1}{3})$
sleptons, leptons ($\times 3$ families)	L	$(\bar{\nu} \ \bar{e}_L)$	$(\nu \ e_L)$	$(\mathbf{1}, \mathbf{2}, -\frac{1}{2})$
	\bar{e}	\bar{e}_R^*	e_R^\dagger	$(\mathbf{1}, \mathbf{1}, 1)$
Higgs, higgsinos	H_u	$(H_u^+ \ H_u^0)$	$(\bar{H}_u^+ \ \bar{H}_u^0)$	$(\mathbf{1}, \mathbf{2}, +\frac{1}{2})$
	H_d	$(H_d^0 \ H_d^-)$	$(\bar{H}_d^0 \ \bar{H}_d^-)$	$(\mathbf{1}, \mathbf{2}, -\frac{1}{2})$

Table 1.1: Chiral supermultiplets in the Minimal Supersymmetric Standard Model. The spin-0 fields are complex scalars, and the spin-1/2 fields are left-handed two-component Weyl fermions.

Names	spin 1/2	spin 1	$SU(3)_C, SU(2)_L, U(1)_Y$
gluino, gluon	\bar{g}	g	$(\mathbf{8}, \mathbf{1}, 0)$
winos, W bosons	$\tilde{W}^\pm \ \tilde{W}^0$	$W^\pm \ W^0$	$(\mathbf{1}, \mathbf{3}, 0)$
bingo, B boson	\tilde{B}^0	B^0	$(\mathbf{1}, \mathbf{1}, 0)$

Table 1.2: Gauge supermultiplets in the Minimal Supersymmetric Standard Model.

1. The Higgs mass 125.5 GeV

The MSSM at one-loop

$$m_h^2 \simeq m_z^2 \cos^2(2\beta) + \frac{3}{(4\pi)^2} \frac{m_t^4}{v_{ew}^2} \left[\log \frac{m_{\tilde{t}}^2}{m_t^2} + \frac{X_t^2}{m_{\tilde{t}}^2} \left(1 - \frac{X_t^2}{12m_{\tilde{t}}^2} \right) \right]$$

Annotations:
- "top mass" points to m_t
- "average stop mass" points to $m_{\tilde{t}}$

$$126^2 = 91^2 + 81^2$$

$$X_t = A_t - \mu \cot \beta$$

stop mixing

- Radiative corrections are same order as tree level piece
- corrections run logarithmically in SUSY
- MSSM case implies either heavy stops or large $X_t = A_t + \dots$

MSSM fine tuning: little hierarchy problem

$$m_z^2 = -2(m_{H_u}^2 + |\mu|^2) + \dots$$

Light Higgsino

For a natural cancellation these should be of the same order

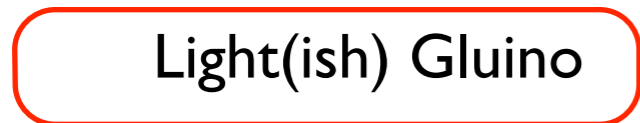
Light stops

$$\delta m_{H_u}^2 \sim -\frac{3y_t^2 m_{\tilde{t}}^2}{4\pi^2} \text{Log} \left(\frac{\Lambda}{m_{\tilde{t}}} \right) - \frac{3g^2}{8\pi^2} (m_{\tilde{W}}^2 + m_{\tilde{h}}^2) \text{Log} \left(\frac{\Lambda}{m_{\tilde{W}}} \right)$$

Light(ish) Gluino

$$\delta m_{\tilde{t}}^2 = \frac{8\alpha_s M_3^2}{3\pi} \text{Log} \left(\frac{\Lambda}{M_3} \right)$$

Light wino



Natural SUSY checklist

- **The 126 GeV Higgs- NMSSM**
or non decoupled D-terms
 e.g. (Aoife Bharucha, Andreas Goudelis & MM) [1310.4500](#)

$$m_{h_0}^2 = m_z^2 \cos(2\beta) + \lambda^2 v_{ew}^2 \sin(2\beta)$$

- Light stops (lighter than 1st & 2nd generation squarks)

$$\delta m_{H_u}^2 \sim -\frac{3y_t^2 m_{\tilde{t}}^2}{4\pi^2} \text{Log} \left(\frac{\Lambda}{m_{\tilde{t}}} \right)$$

- Dynamical explanation? Soft masses cannot be the same

$$m_{(Q,U,D)3}^2 \ll m_{(Q,U,D)1,2}^2$$

- Connection to Flavour? $Y_u \simeq \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & y_t \end{pmatrix}$, $Y_d \simeq \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & y_b \end{pmatrix}$, $Y_e \simeq \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & y_\tau \end{pmatrix}$

- No (excluded) FCNC's please!

- Realistic models of SUSY breaking? - ISS magnetic SQCD

A common problem!

Other approaches such as making A_t large, still need to explain why stops are lighter than 1st two generations? e.g. “[Large \$A_t\$ Without the Desert](#)”-ArXiv: [1405.1038](#)

Why? $m_{(Q,U,D)3}^2 \ll m_{(Q,U,D)1,2}^2$

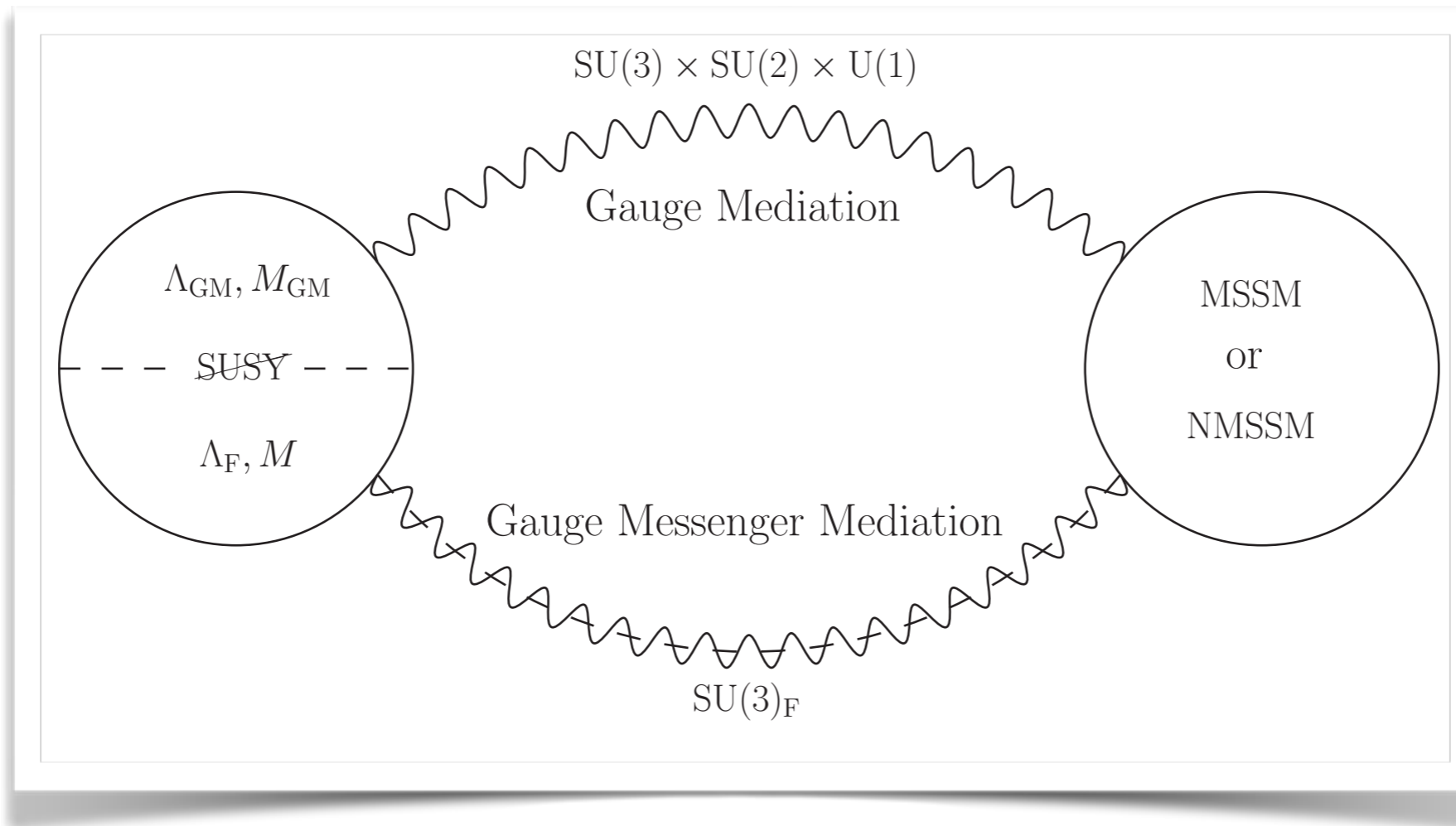
Typically for all mSUGRA, GMSB, AMSB etc

$$m_{Q,U,D}^2 \sim \Lambda^2 \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} \rightarrow \sim > 1.5 \text{ TeV exclusions}$$

$\rightarrow \sim > 400 \text{ GeV exclusions}$

first two generations degenerate to reduce FCNC's
an $SU(2)_F$?

Flavour Gauge Messengers



- Extend gauge mediation to include a gauged flavour group
- Explain Yukawas and SUSY breaking
- Fields break $SU(3)_F$ and SUSY at the same time
- Fully dynamical origin in terms of Meta-stable SUSY breaking

Gauge messengers=

Recipe:

- Gauge a group
- Higgs a group
- Fields that Higgs that group also break SUSY

Flavour?

Non Abelian Froggatt-Nielson mechanism

SUSY breaking fields are Flavons!?

From GMSB

$$m_{Q,U,D,\text{GMSB}}^2 \sim + \sum_i \frac{g_{SM,i}^4}{(16\pi^2)^2} \left(\frac{F}{M}\right)^2 \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

From flavour gauge mess.

$$\delta m_{Q,U,D}^2 = -\frac{g_F^2}{16\pi^2} \left(\frac{F}{M}\right)^2 \begin{pmatrix} \frac{7}{6} & 0 & 0 \\ 0 & \frac{7}{6} & 0 \\ 0 & 0 & \frac{8}{3} \end{pmatrix}$$

Nett

$$m_{Q,U,D}^2 \sim \Lambda^2 \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -\# \end{pmatrix}$$

a tachyonic soft term for stops

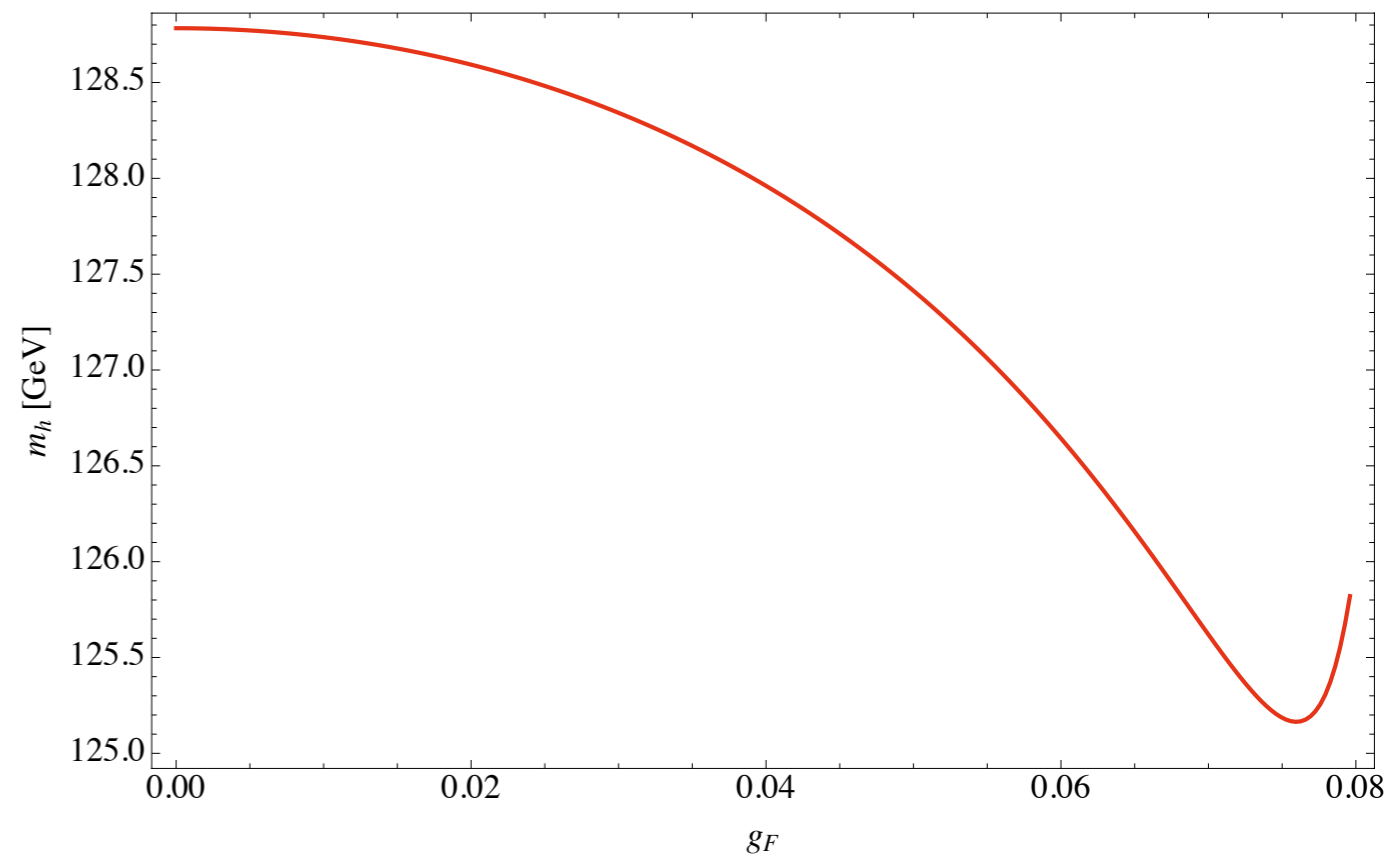
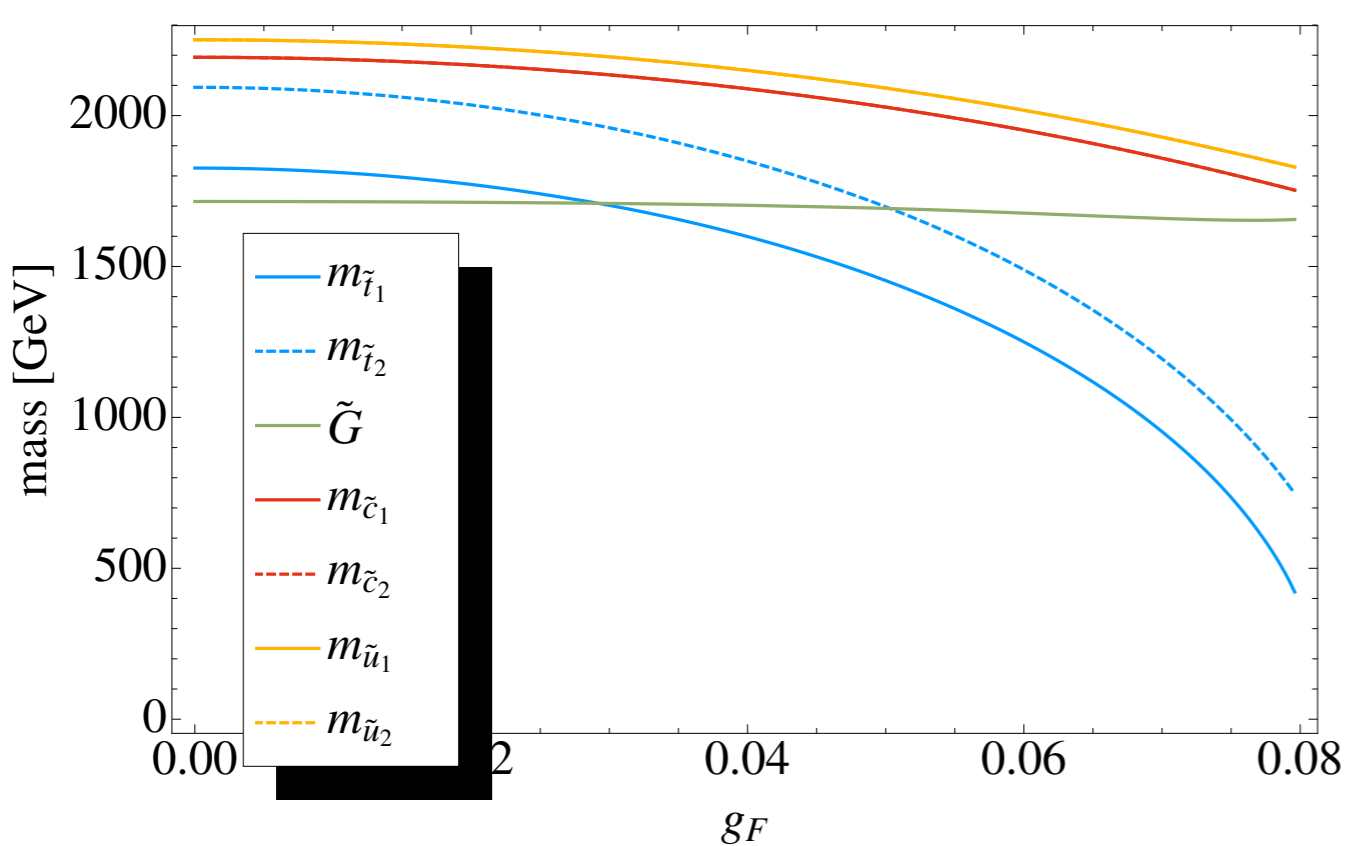
From GMSB

From flavour gauge mess.

$$m_{Q,U,D,GMSB}^2 \sim + \sum_i \frac{g_{SM,i}^4}{(16\pi^2)^2} \left(\frac{F}{M}\right)^2 \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

$$\delta m_{Q,U,D}^2 = -\frac{g_F^2}{16\pi^2} \left(\frac{F}{M}\right)^2 \begin{pmatrix} \frac{7}{6} & 0 & 0 \\ 0 & \frac{7}{6} & 0 \\ 0 & 0 & \frac{8}{3} \end{pmatrix}$$

Stick the model into an NMSSM spectrum generator (SPheno)



Squarks and Gluino

Higgs

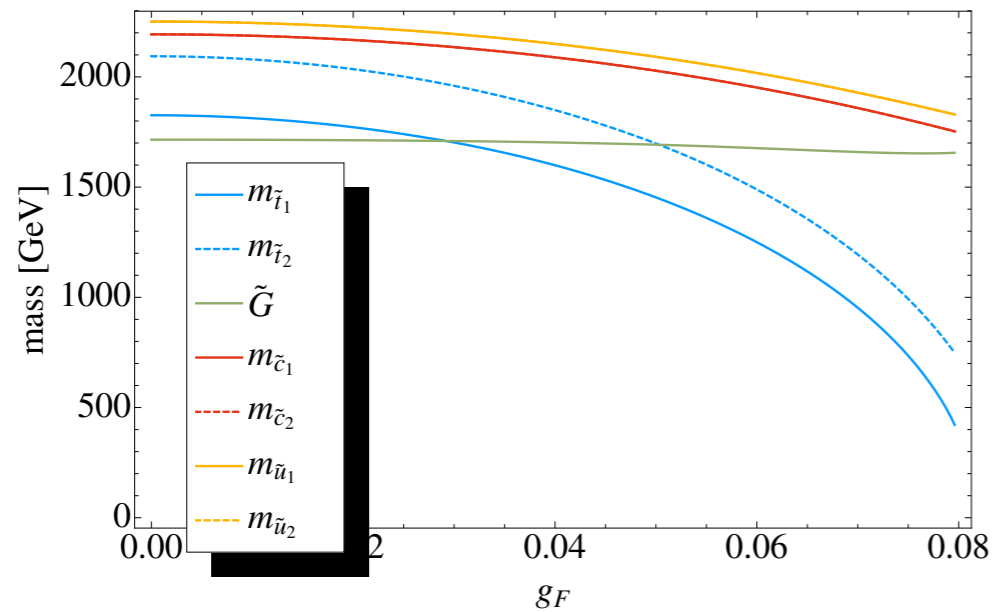
Figure 2. A plot [Left] of the squark and gluino masses for model 1 with the NMSSM. [Right] a plot of Higgs mass versus g_F for the same range. $\lambda = 0.8$, $\kappa = 0.8$, $v_s = 1000$, $m_{H_d}^2 = m_{H_u}^2 = 10^5$, $\Lambda = \Lambda_F = 2.3 \times 10^5$, $M = 10^7$, $\tan \beta = 1.5$.

Flavour changing neutral currents

(S.Abel & MM) 1404.1318

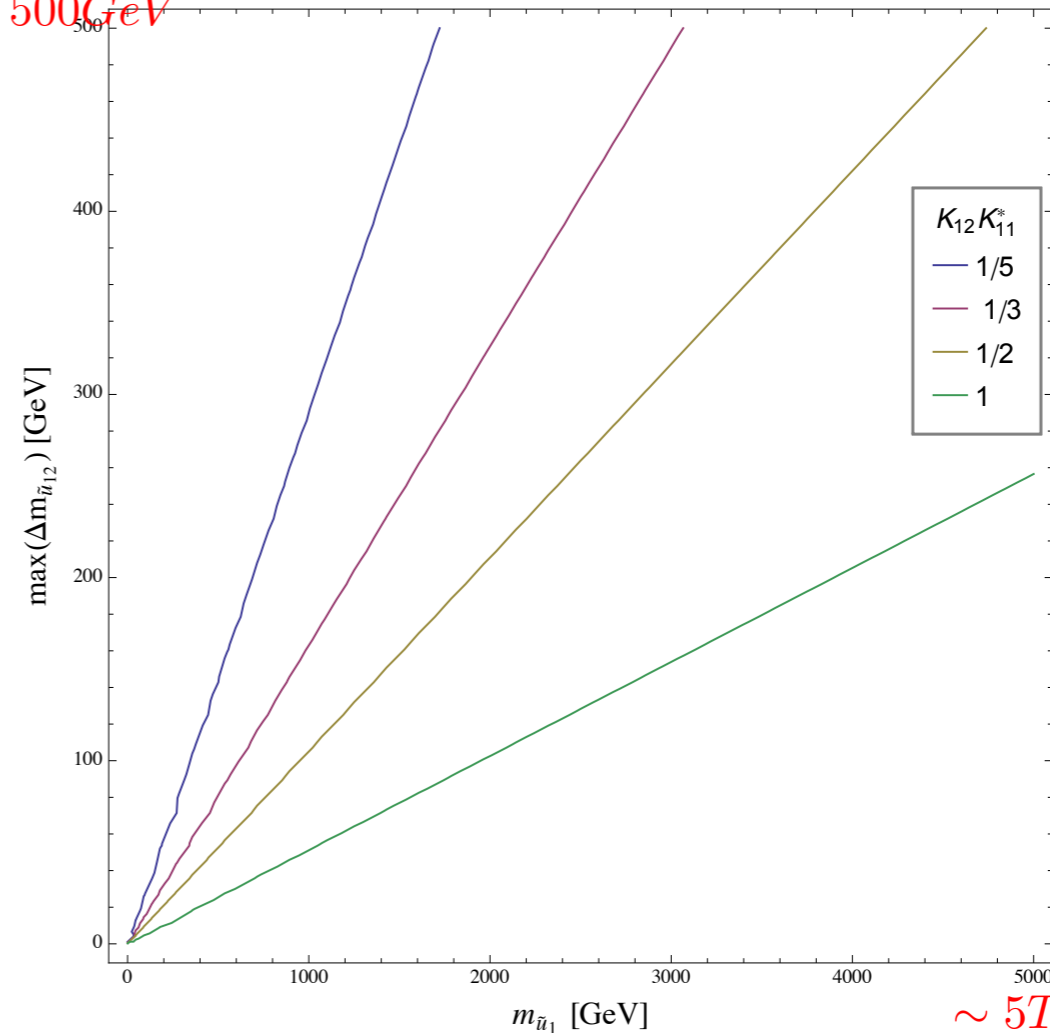
$$\delta_{u,12} < 0.1$$

Model 1: degenerate 1st & 2nd

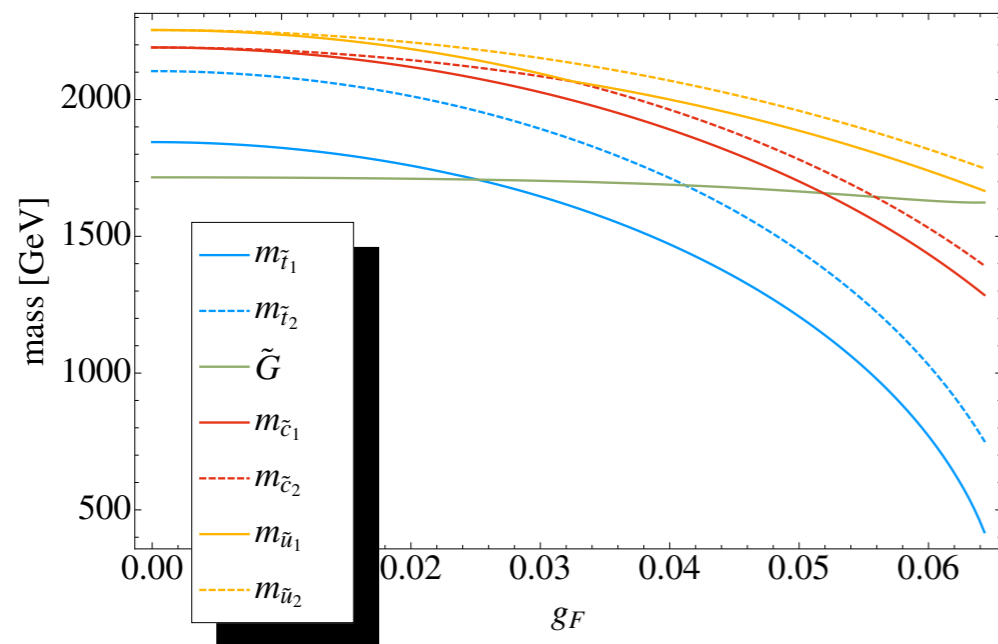


$$\delta_{ij} = \frac{m_{q_2}^2 - m_{q_1}^2}{\frac{1}{2}(m_{q_2}^2 + m_{q_1}^2)} K_{ij} K_{ii}^*$$

$\sim 500 \text{ GeV}$



Model 2: split 1st & 2nd



Sizeable splittings allowed for multi-TeV 1st and 2nd Gen.

If extended to leptons, we expect Stau NLSP (Gravitino LSP)

Tachyons are natural?!

For a natural cancellation these should be of the same order

$$m_z^2 = -2(m_{H_u}^2 + |\mu|^2) + \dots$$

Massless stops at M_{planck} , turn tachyonic at messenger scale, are turned positive by gluino

stops run positive

$$\longrightarrow \delta m_{\tilde{t}}^2 = -\frac{8\alpha_s M_3^2}{3\pi} \text{Log} \left(\frac{\Lambda}{M_3} \right)$$

$$\delta m_{H_u}^2 \sim -\frac{3y_t^2 m_{\tilde{t}}^2}{4\pi^2} \text{Log} \left(\frac{\Lambda}{m_{\tilde{t}}} \right)$$

$$(+) + (-) \sim 0$$

Reduces fine tuning on the Higgs.

How to Gauge flavour?

Field	G_{SM}	$SU(3)_L \times SU(3)_R \rightarrow SU(3)_F$
\hat{Q}^f	$(\mathbf{2}, \frac{1}{6}, \mathbf{3})$	$(\bar{\mathbf{3}}, \mathbf{1})$
\hat{L}^f	$(\mathbf{2}, -\frac{1}{2}, \mathbf{1})$	$(\bar{\mathbf{3}}, \mathbf{1})$
\hat{H}_d	$(\mathbf{2}, -\frac{1}{2}, \mathbf{1})$	$(\mathbf{1}, \mathbf{1})$
\hat{H}_u	$(\mathbf{2}, \frac{1}{2}, \mathbf{1})$	$(\mathbf{1}, \mathbf{1})$
\hat{D}^f	$(\mathbf{1}, \frac{1}{3}, \bar{\mathbf{3}})$	$(\mathbf{1}, \mathbf{3})$
\hat{U}^f	$(\mathbf{1}, -\frac{2}{3}, \bar{\mathbf{3}})$	$(\mathbf{1}, \mathbf{3})$
\hat{E}^f	$(\mathbf{1}, \mathbf{1}, \mathbf{1})$	$(\mathbf{1}, \mathbf{3})$
$\hat{\nu}^f$	$(\mathbf{0}, \mathbf{1}, \mathbf{1})$	$(\mathbf{1}, \mathbf{3})$

Gauge this flavour group

Include right handed neutrinos

$SU(3)_F$ is anomaly free and $G_{SM} \times SU(3)_F$ mixed anomalies vanish!

We can gauge it...

.... but we still need to Higgs $SU(3)_F$

It turns out that this model can embed into magnetic SQCD too!

Field	$SU(\tilde{N})_{\text{mag}}$	$SU(3)_L \times SU(3)_R \rightarrow SU(3)_F$
Φ	1	$(\mathbf{3}, \bar{\mathbf{3}})$
φ	\square	$(\bar{\mathbf{3}}, \mathbf{1})$
$\tilde{\varphi}$	$\bar{\square}$	$(\mathbf{1}, \mathbf{3})$

$$W_{\text{mag}} = h \text{Tr} \varphi \Phi \tilde{\varphi} - \mu^2 \text{Tr} \Phi.$$

The usual rank condition breaks $SU(3)_F \rightarrow SU(2)_F$

$$\mu_{ij} = \begin{pmatrix} \mu & 0 & 0 \\ 0 & \mu & 0 \\ 0 & 0 & \mu \end{pmatrix} \quad \text{and} \quad \varphi^T = \tilde{\varphi} = \begin{pmatrix} \mu \\ \mu \\ 0 \end{pmatrix} \quad F_\Phi = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & h\mu^2 \end{pmatrix} \quad \text{such that} \quad V_{\text{min}} = |h^2 \mu^4|.$$

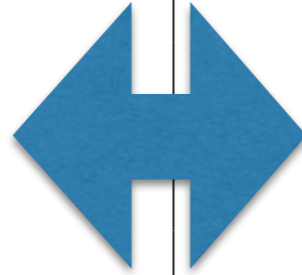
“Dynamical metastable flavour gauge mediation”

$$\delta m_{Q,U,D}^2 = -\frac{g_F^2}{16\pi^2} |h^2 \mu^2| \begin{pmatrix} \frac{8}{9} & 0 & 0 \\ 0 & \frac{8}{9} & 0 \\ 0 & 0 & \frac{20}{9} \end{pmatrix} + \dots$$

Perhaps we can explain Yukawas too!

Couple these fields together

Field	G_{SM}	$SU(3)_L \times SU(3)_R \rightarrow SU(3)_F$
\hat{Q}^f	$(\mathbf{2}, \frac{1}{6}, \mathbf{3})$	$(\bar{\mathbf{3}}, \mathbf{1})$
\hat{L}^f	$(\mathbf{2}, -\frac{1}{2}, \mathbf{1})$	$(\bar{\mathbf{3}}, \mathbf{1})$
\hat{H}_d	$(\mathbf{2}, -\frac{1}{2}, \mathbf{1})$	$(\mathbf{1}, \mathbf{1})$
\hat{H}_u	$(\mathbf{2}, \frac{1}{2}, \mathbf{1})$	$(\mathbf{1}, \mathbf{1})$
\hat{D}^f	$(\mathbf{1}, \frac{1}{3}, \bar{\mathbf{3}})$	$(\mathbf{1}, \mathbf{3})$
\hat{U}^f	$(\mathbf{1}, -\frac{2}{3}, \bar{\mathbf{3}})$	$(\mathbf{1}, \mathbf{3})$
\hat{E}^f	$(\mathbf{1}, \mathbf{1}, \mathbf{1})$	$(\mathbf{1}, \mathbf{3})$
$\hat{\nu}^f$	$(\mathbf{0}, \mathbf{1}, \mathbf{1})$	$(\mathbf{1}, \mathbf{3})$



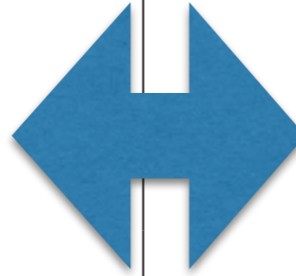
Field	$SU(\tilde{N})_{\text{mag}}$	$SU(3)_L \times SU(3)_R \rightarrow SU(3)_F$
Φ	1	$(\mathbf{3}, \bar{\mathbf{3}})$
φ	\square	$(\bar{\mathbf{3}}, \mathbf{1})$
$\tilde{\varphi}$	$\bar{\square}$	$(\mathbf{1}, \mathbf{3})$

leads to...
$$W = \frac{\lambda_u}{\Lambda} H_u Q \Phi U + \frac{\lambda_d}{\Lambda} H_d Q \Phi D$$

$$\Phi = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & \langle X \rangle \end{pmatrix} \text{ leads to } Y_u = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & Y_t \end{pmatrix}$$

Model 2

Field	G_{SM}	$SU(3)_L \times SU(3)_R \rightarrow SU(3)_F$
\hat{Q}^f	$(\mathbf{2}, \frac{1}{6}, \mathbf{3})$	$(\bar{\mathbf{3}}, \mathbf{1})$
\hat{L}^f	$(\mathbf{2}, -\frac{1}{2}, \mathbf{1})$	$(\bar{\mathbf{3}}, \mathbf{1})$
\hat{H}_d	$(\mathbf{2}, -\frac{1}{2}, \mathbf{1})$	$(\mathbf{1}, \mathbf{1})$
\hat{H}_u	$(\mathbf{2}, \frac{1}{2}, \mathbf{1})$	$(\mathbf{1}, \mathbf{1})$
\hat{D}^f	$(\mathbf{1}, \frac{1}{3}, \bar{\mathbf{3}})$	$(\mathbf{1}, \mathbf{3})$
\hat{U}^f	$(\mathbf{1}, -\frac{2}{3}, \bar{\mathbf{3}})$	$(\mathbf{1}, \mathbf{3})$
\hat{E}^f	$(\mathbf{1}, \mathbf{1}, \mathbf{1})$	$(\mathbf{1}, \mathbf{3})$
$\hat{\nu}^f$	$(\mathbf{0}, \mathbf{1}, \mathbf{1})$	$(\mathbf{1}, \mathbf{3})$



Field	$SU(\tilde{N})_{\text{mag}}$	$SU(3)_L \times SU(3)_R \rightarrow SU(3)_F$
Φ	1	$(\mathbf{3}, \bar{\mathbf{3}})$
φ	\square	$(\bar{\mathbf{3}}, \mathbf{1})$
$\tilde{\varphi}$	$\bar{\square}$	$(\mathbf{1}, \mathbf{3})$

Rank 2

Field	$SU(\tilde{N})_{\text{mag}}$	$SU(3)_L \times SU(3)_R \rightarrow SU(3)_F$
M	1	$(\mathbf{3}, \bar{\mathbf{3}})$
ϕ	\square	$(\bar{\mathbf{3}}, \mathbf{1})$
$\tilde{\phi}$	$\bar{\square}$	$(\mathbf{1}, \mathbf{3})$

Rank 1

$$\varphi^T = \tilde{\varphi} = \begin{pmatrix} 0 \\ \mu \\ \mu \end{pmatrix} \quad \text{and} \quad \phi^T = \tilde{\phi} = \begin{pmatrix} 0 \\ 0 \\ \nu \end{pmatrix}$$

$$\frac{\phi}{\Lambda} \sim O(1) \quad \frac{\varphi}{\Lambda} \sim \epsilon \quad \text{leads to} \quad Y_u \sim \begin{pmatrix} 0 & 0 & 0 \\ 0 & \epsilon & \epsilon \\ 0 & \epsilon & 1 \end{pmatrix}$$

Non-Abelian Froggatt-Nielson

Many more model building avenues to explore further...

(S.Abel & MM) 1404.1318

“Large At Without the Desert”

A.Abdalgabar, A.Cornell, A.Deandrea, MM 1405:1038

$$\mathbf{a}_u \approx \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & a_t \end{pmatrix}, \quad \mathbf{a}_d \approx \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & a_b \end{pmatrix}, \quad \mathbf{a}_e \approx \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & a_\tau \end{pmatrix},$$

UV

In many models $A_t = 0$ in UV



A_t runs negative

IR

typically ends up negative a few 100 GeV

Not sufficient to get the correct Higgs mass....

Question: Can we accelerate its running?

.The Higgs mass 126 GeV

The MSSM at one-loop

$$m_h^2 \simeq m_z^2 \cos^2(2\beta) + \frac{3}{(4\pi)^2} \frac{m_t^4}{v_{ew}^2} \left[\log \frac{m_{\tilde{t}}^2}{m_t^2} + \frac{X_t^2}{m_{\tilde{t}}^2} \left(1 - \frac{X_t^2}{12m_{\tilde{t}}^2} \right) \right]$$

top mass

average stop mass

$$126^2 = 91^2 + 81^2$$

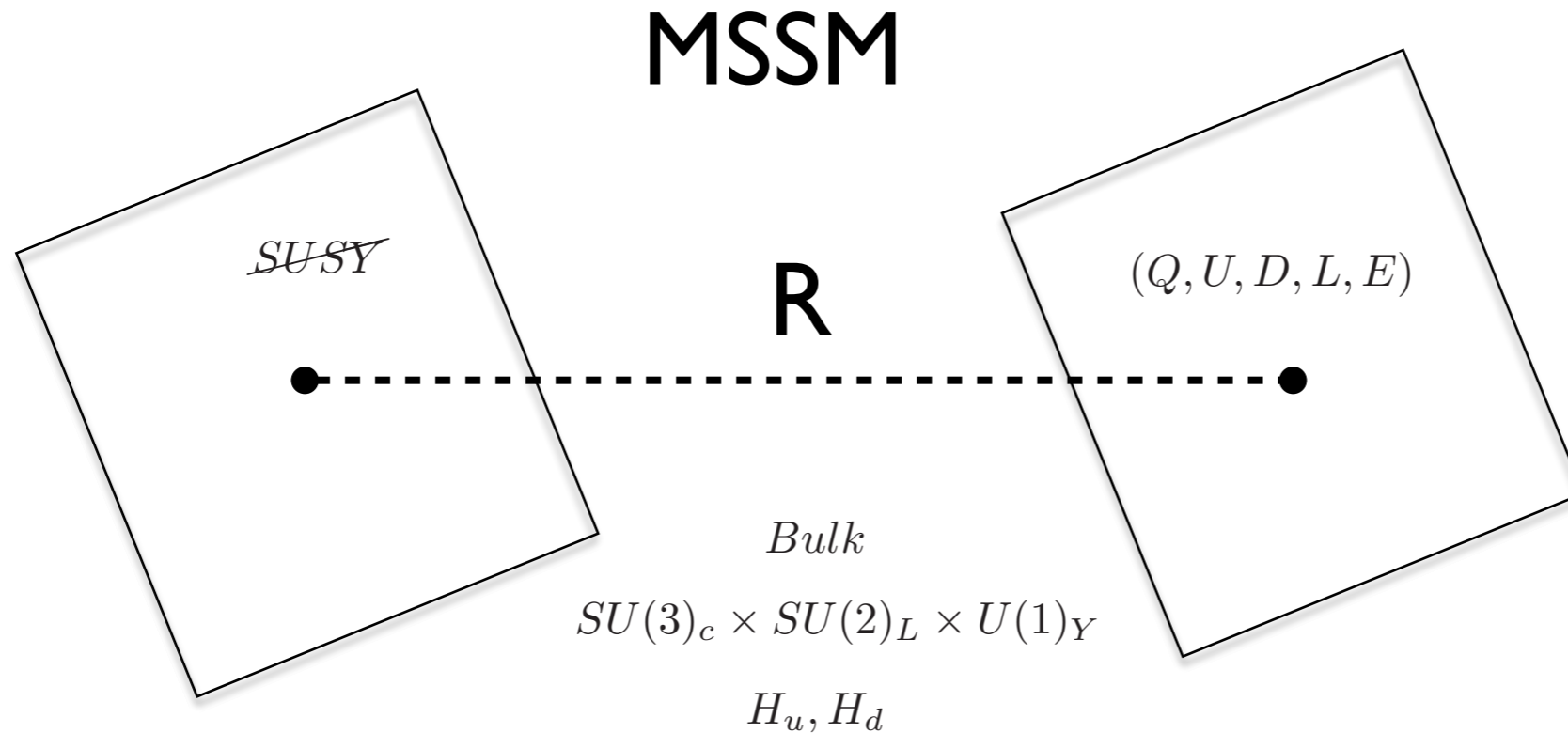
$$X_t = A_t - \mu \cot \beta$$

stop mixing

- Radiative corrections are same order as tree level piece
- corrections run logarithmically in SUSY
- MSSM case implies either heavy stops or large $X_t = A_t + \dots$

In 5D you can get large A_t !

“Power law running”



An extra dimension of radius R .

Additional Kaluza Klein modes enter RGEs @ $Q > 1/R$

Large A_t : Independent of the details of SUSY breaking

Split families: Locate different generations in brane or bulk

$$m_{(Q,U,D)3}^2 \ll m_{(Q,U,D)1,2}^2$$

Power law running

$$\alpha^{-1}(Q) = \alpha^{-1}(m_z) - \frac{b}{2\pi} \log \frac{Q}{m_z} + \frac{\tilde{b}}{2\pi} \log \frac{Q}{m_{KK}} - \frac{\tilde{b}}{2\pi} \left(\frac{Q^d}{m_{KK}} - 1 \right) c_d$$

(T.Taylor, G.Veneziano) [Phys. Lett. B212 \(1988\)](#)

(K.Dienes, E.Dudas, T. Gherghetta) [9803466](#)

(K.Dienes, E.Dudas, T. Gherghetta) [9806292](#)

“The finite power-law corrections to the Yukawa couplings have the right sign and magnitude to cancel the tree-level terms. This can help to explain the hierarchical structure of the fermion Yukawa couplings.”

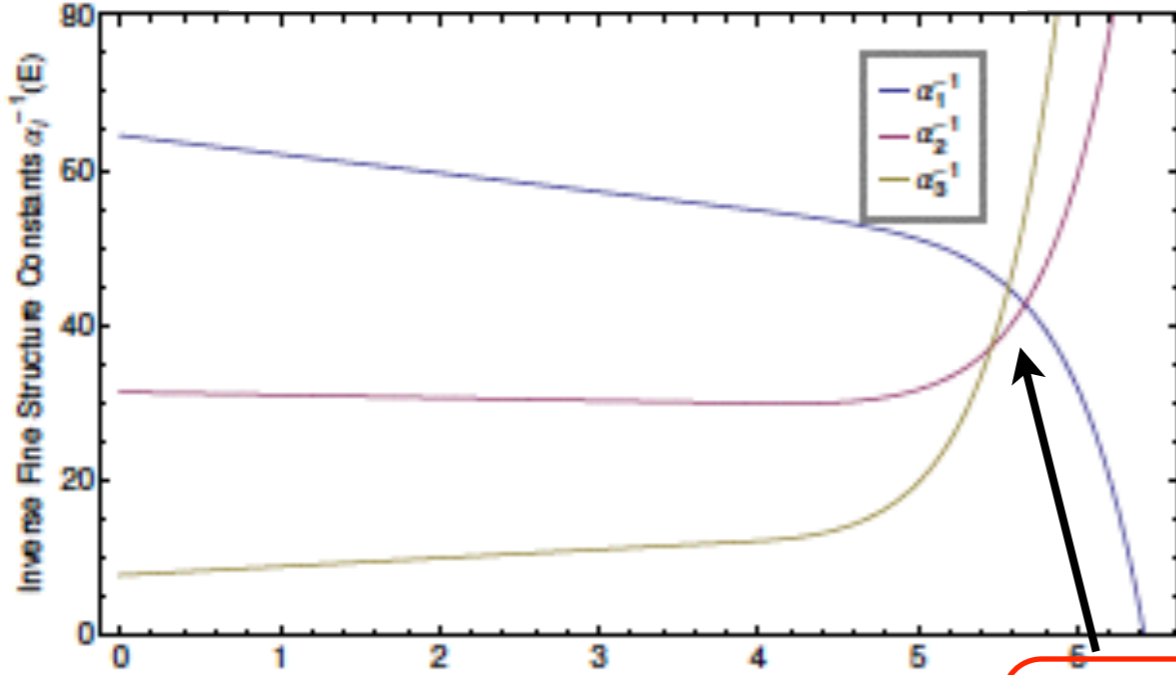
(A.Abdalagbar, A.Cornell, A.Deandrea, MM) [1405:1038](#)

“Perhaps we can use this to accelerate the value of A_t ?”

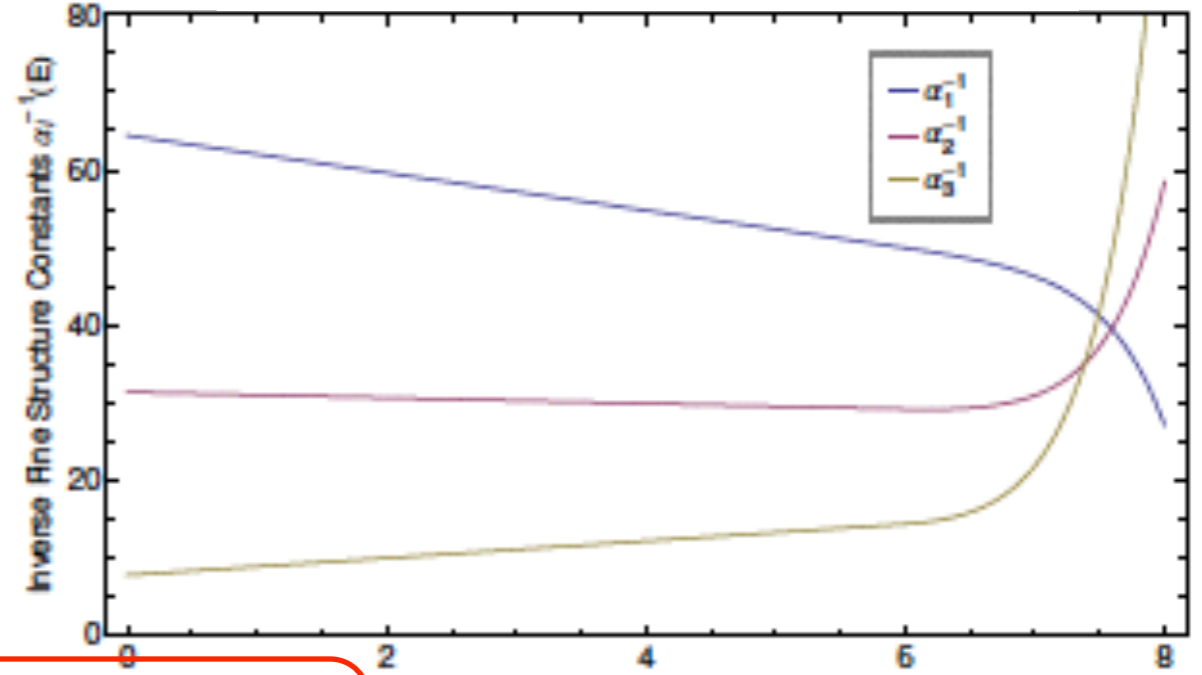
4+d dimensional MSSM

- ✓ Always unify
- ✓ No proton decay
- ✓ Explains flavour
- ✓ Large A_t

Compactification scale 10 TeV



Compactification scale 10³ TeV



Compactification scale 10⁵ TeV Unification @ 10⁶ GeV Compactification scale 10¹² TeV

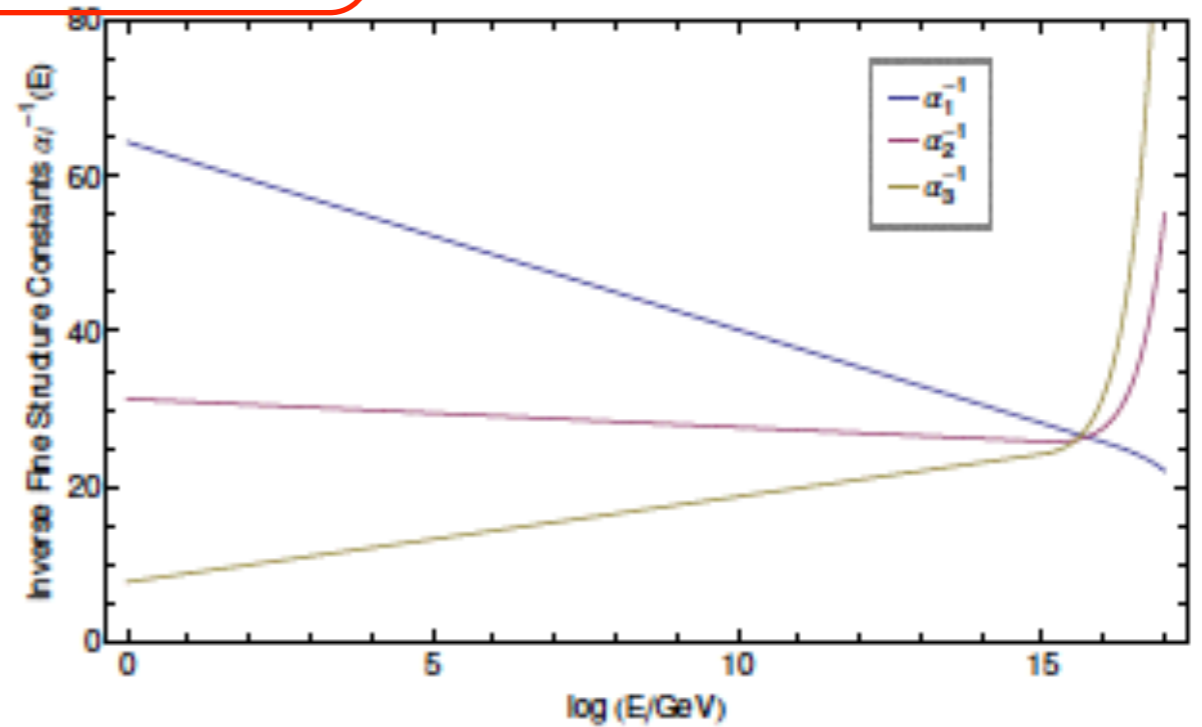
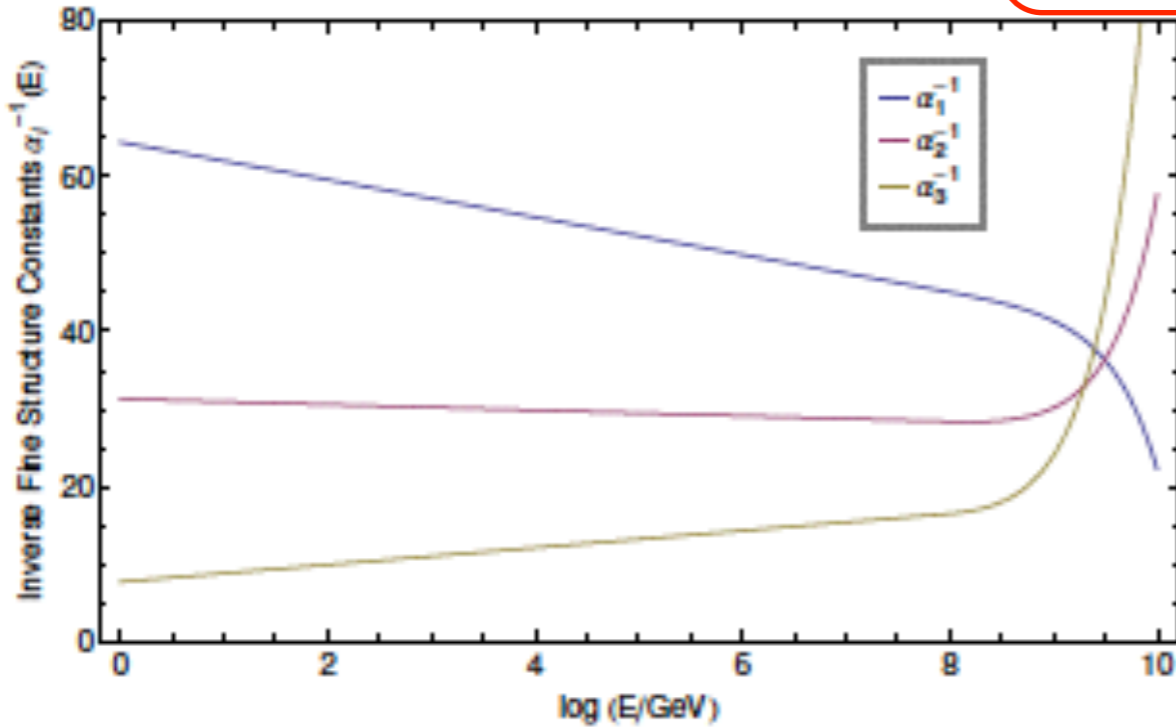
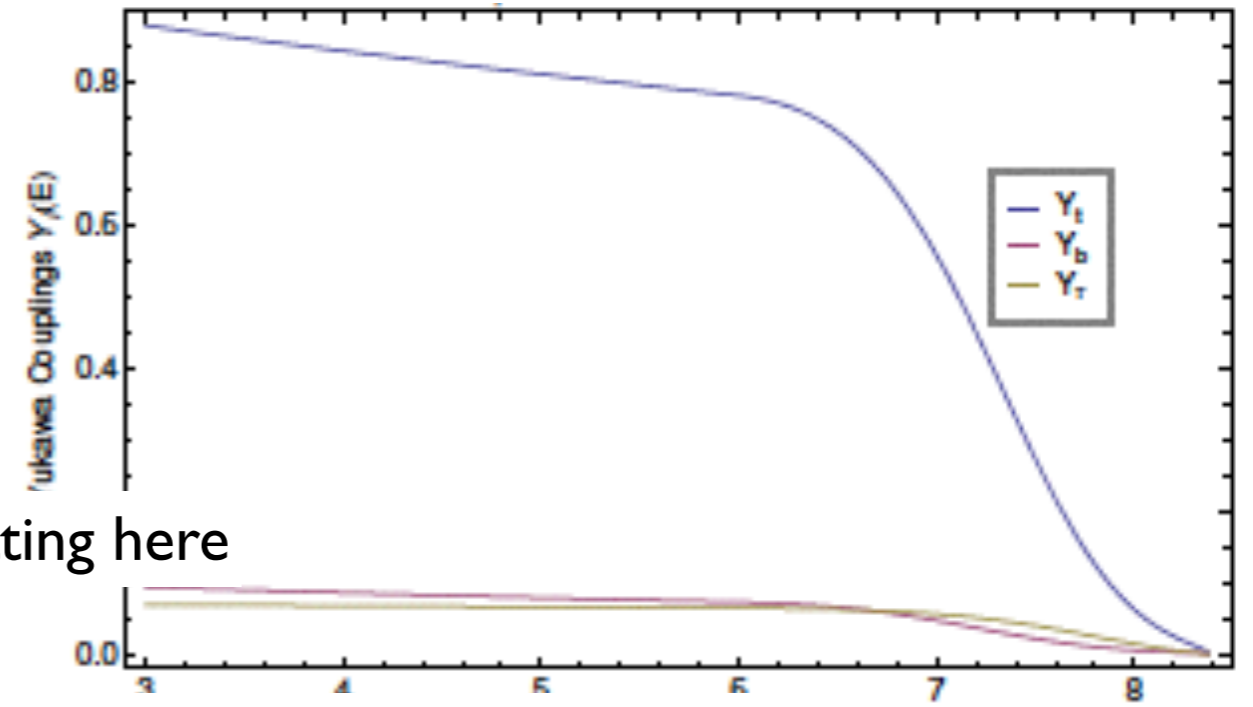
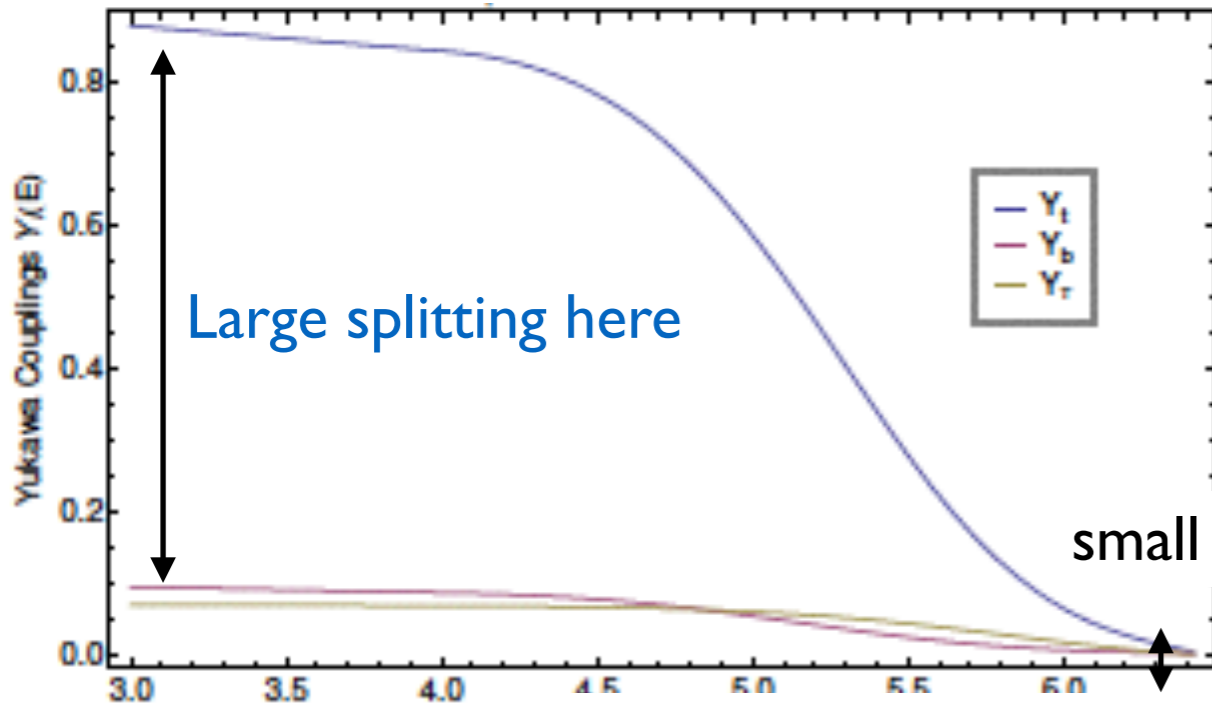


Figure 1. Running of the inverse fine structure constants $\alpha^{-1}(E)$, for three different values of the compactification scales 10 TeV (top left panel), 10³ TeV (top right), 10⁵ TeV (bottom left) and 10¹² TeV (bottom right), with M_3 of 1.7 TeV, as a function of $\log(E/\text{GeV})$.

Compactification scale 10 TeV

Compactification scale 10^3 TeV



Flavour hierarchy just an RGE effect?

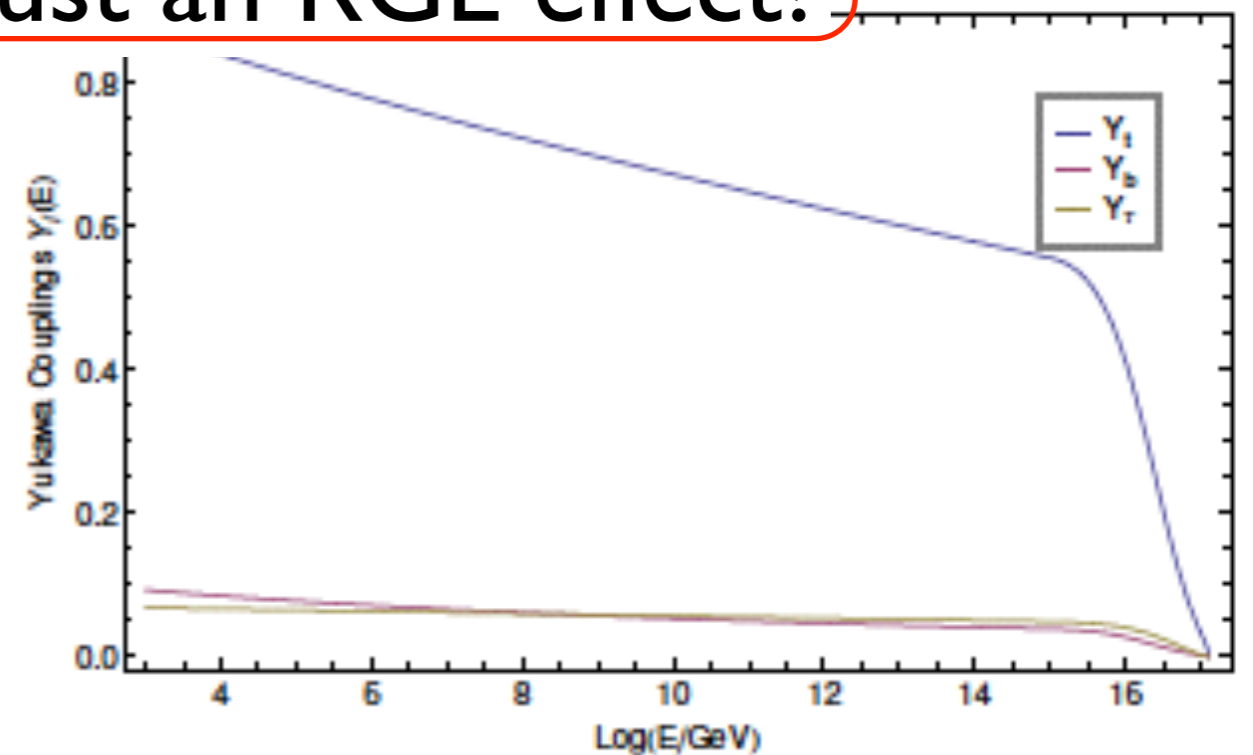
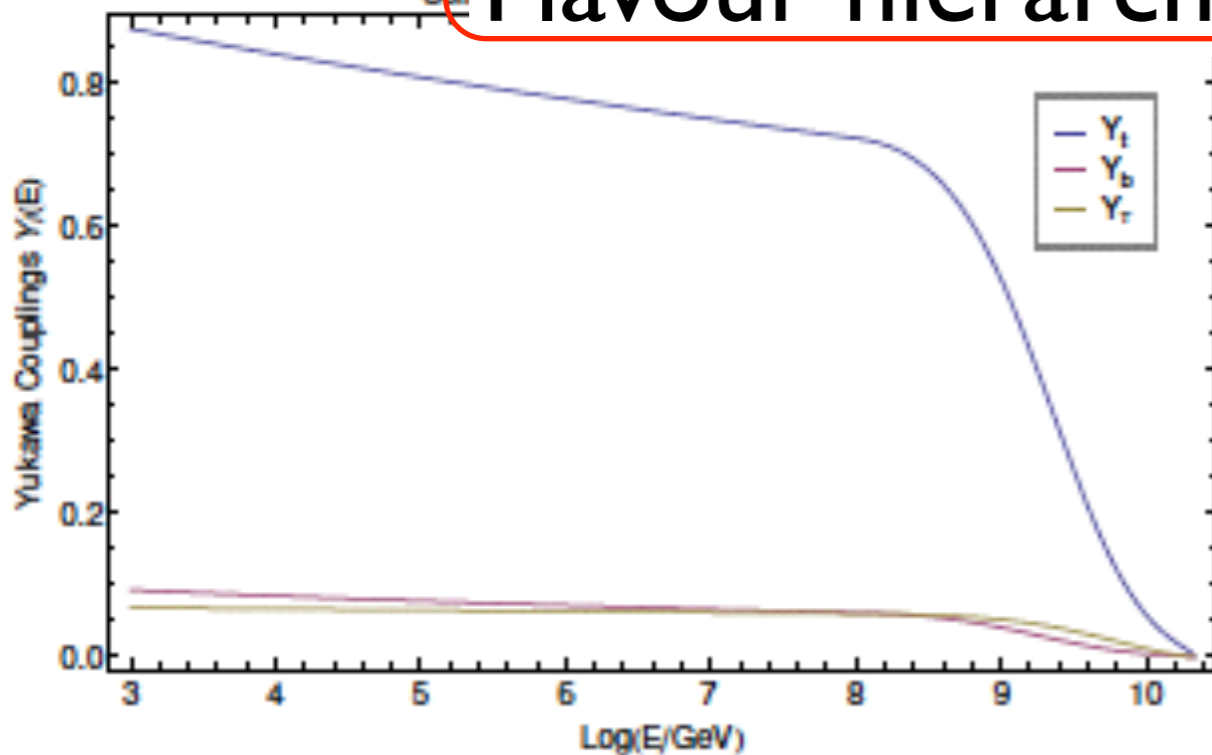
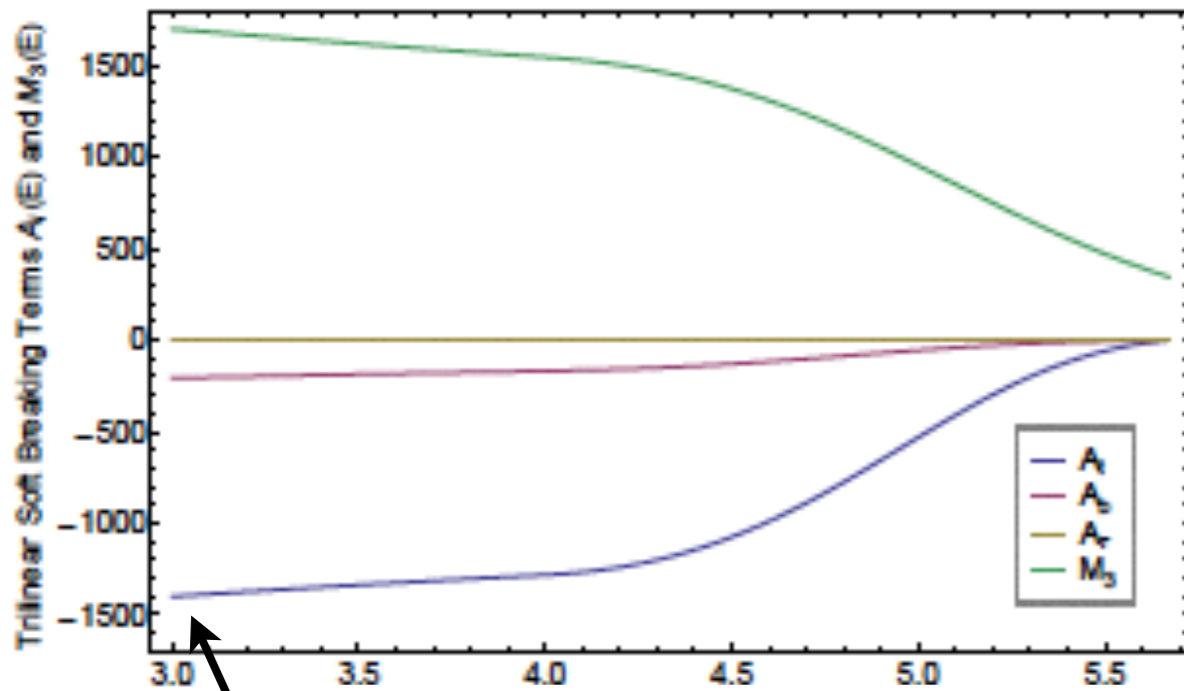
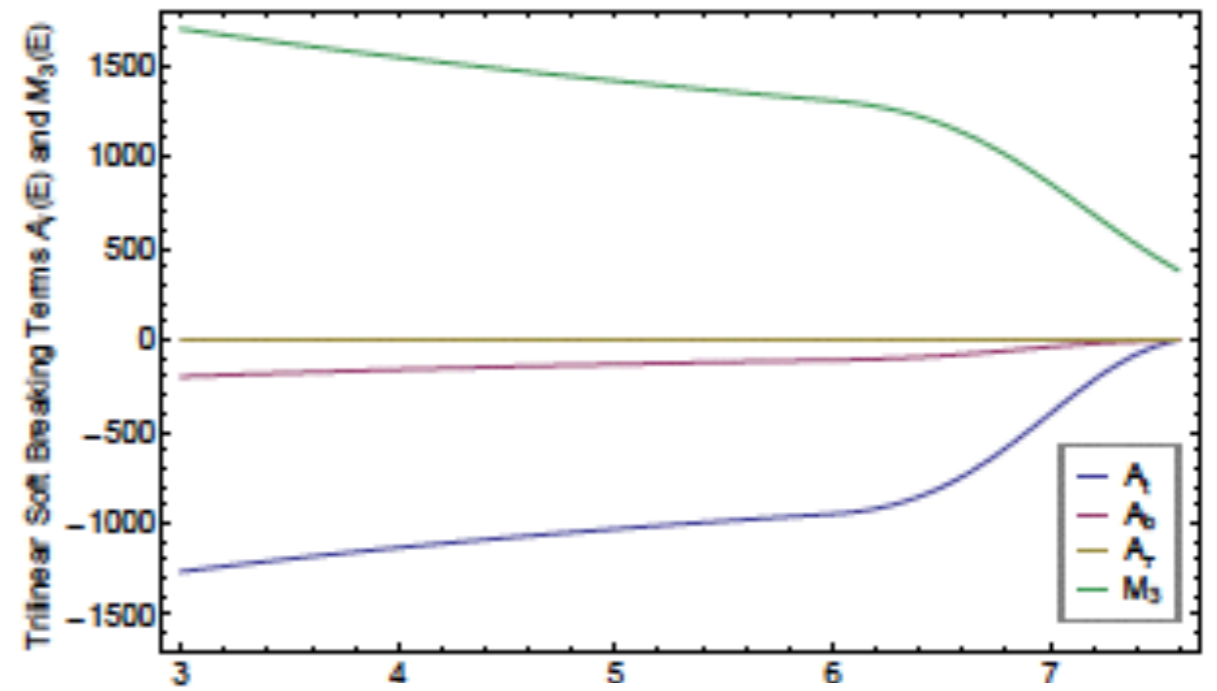


Figure 2. Running of Yukawa couplings Y_i , for three different values of the compactification scales: 10 TeV (top left panel), 10^3 TeV (top right), 10^5 TeV (bottom left) and 10^{12} TeV (bottom right), with $M_3[10^3]$ of 1.7 TeV, as a function of $\log(E/GeV)$.

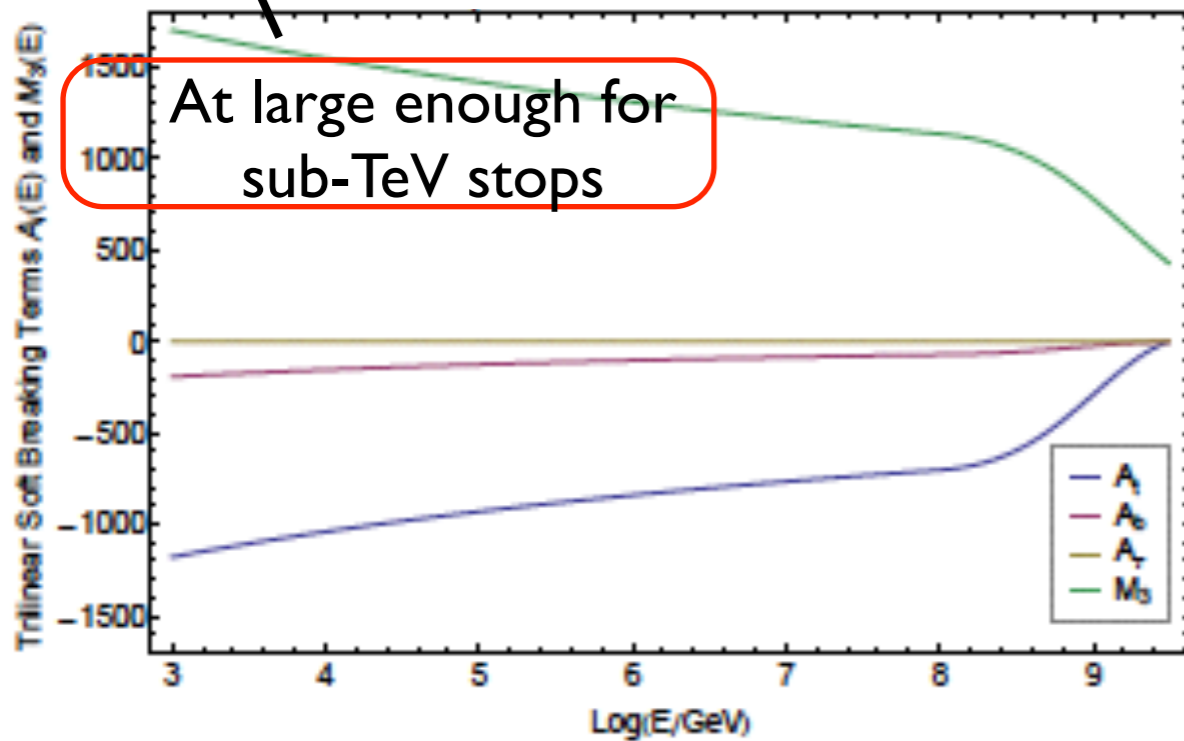
Compactification scale 10 TeV



Compactification scale 10^3 TeV



Compactification scale 10^5 TeV



Compactification scale 10^{12} TeV

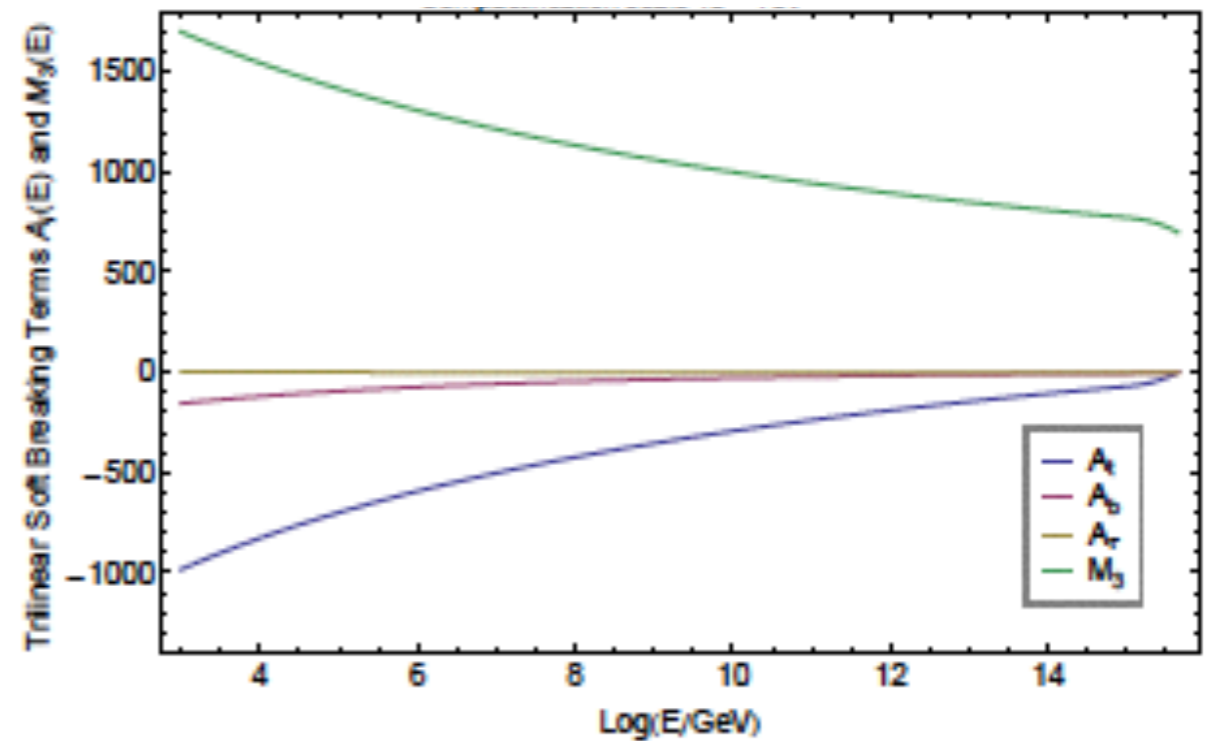
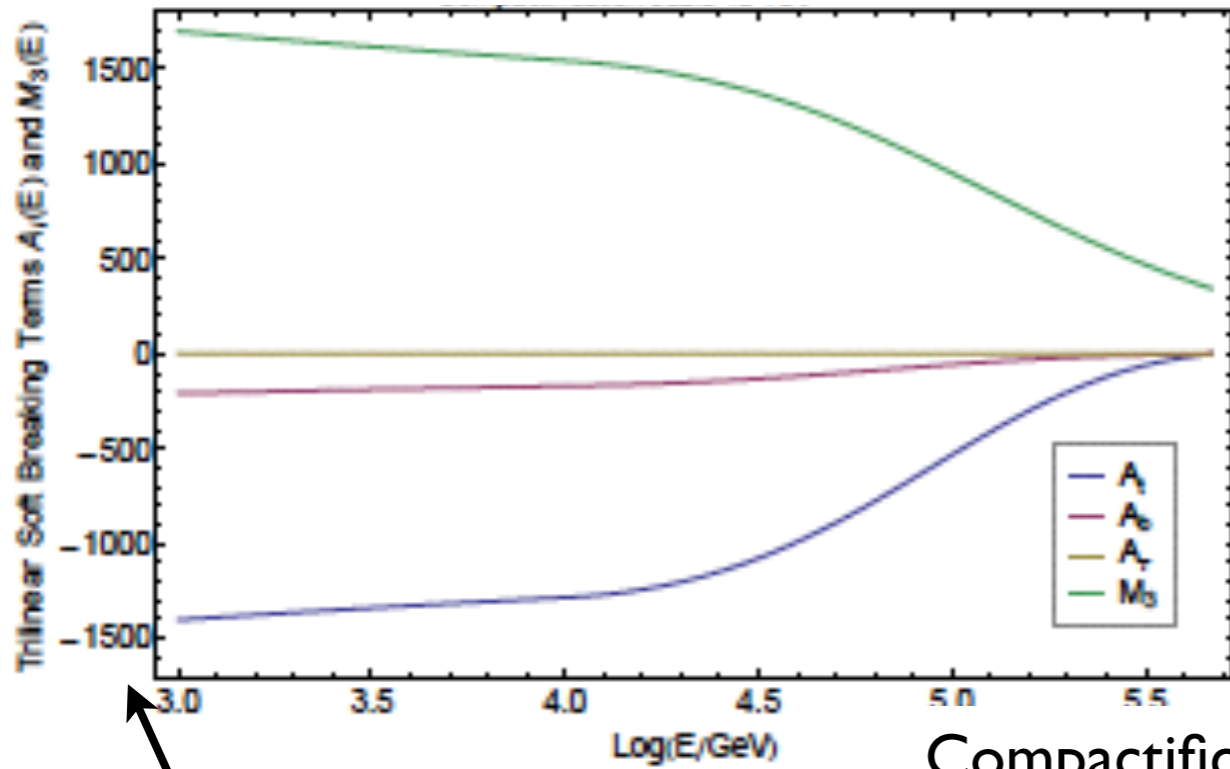
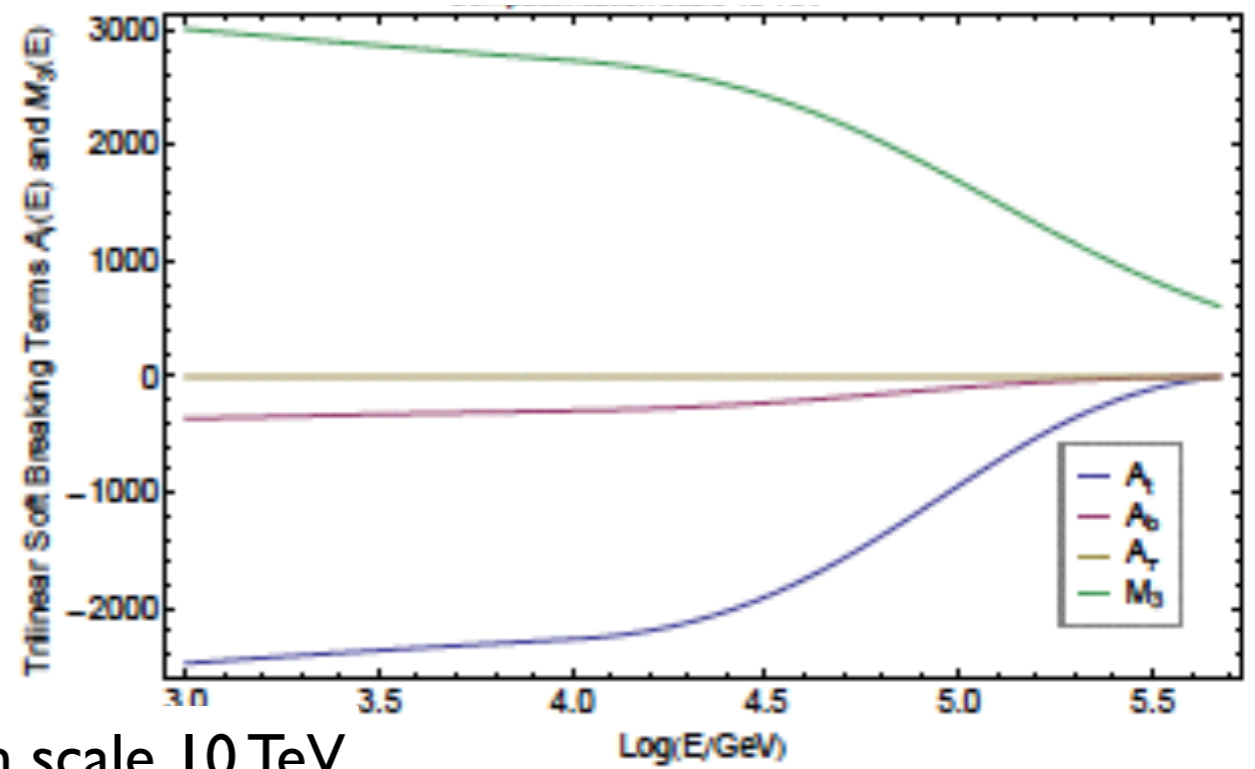


Figure 3. Running of trilinear soft terms $A_i(3,3)(E)$, for three different values of the compactification scales 10 TeV (top left panel), 10^3 TeV (top right), 10^5 TeV (bottom left) and 10^{12} TeV (bottom right), with $M_3[10^3]$ of 1.7 TeV, as a function of $\log(E/\text{GeV})$.

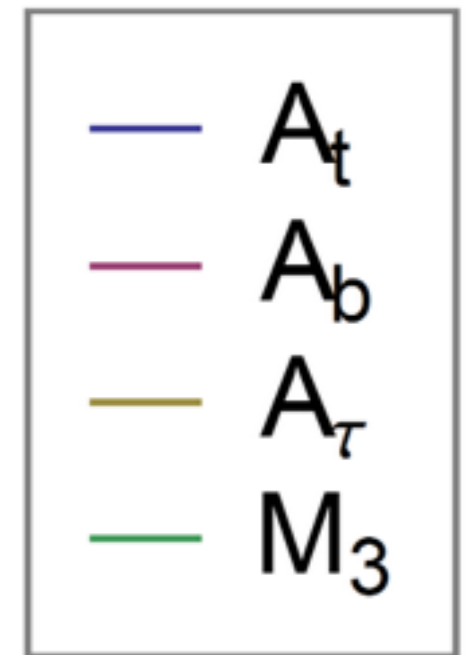
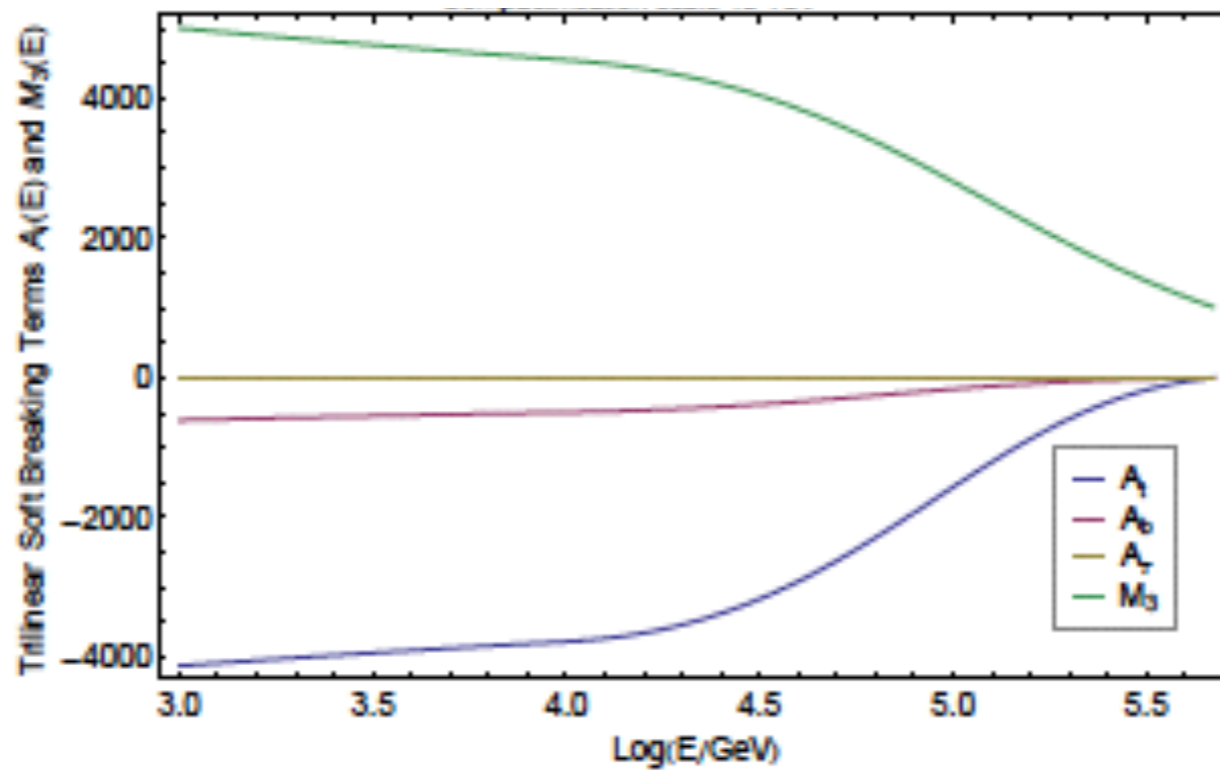
Compactification scale 10 TeV



Compactification scale 10 TeV



Compactification scale 10 TeV



At large enough for sub-TeV stops

Larger gluino gives larger A_t

Conclusions

- Traditional models are in bad shape
- Perhaps it is time to panic?
- Natural SUSY is motivated from bottom up
- These can have exciting top-down motivations too
- It does mean sacrificing minimality!

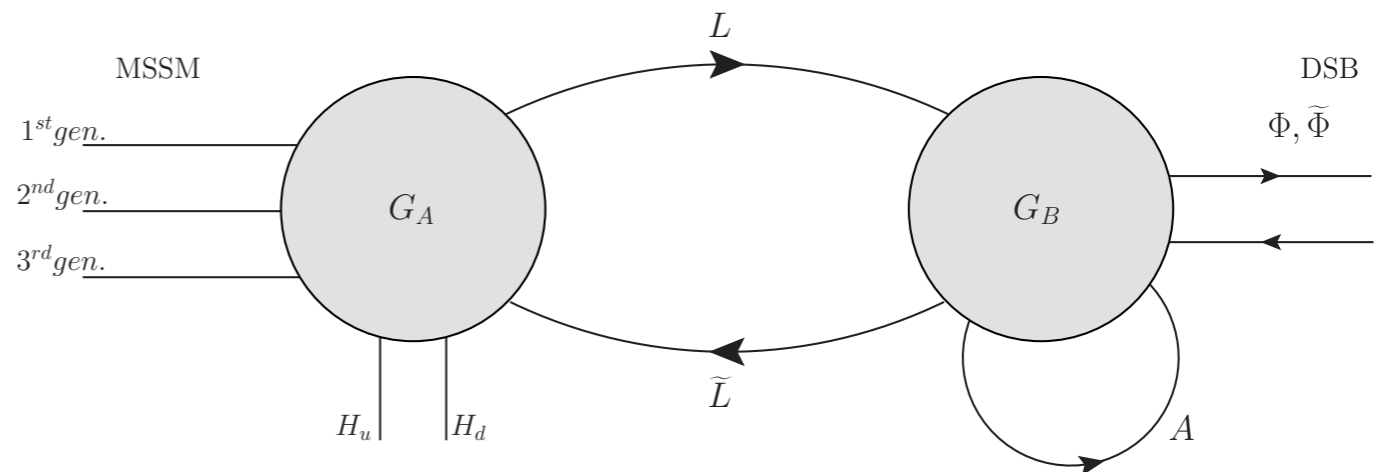
Back up slides

Non decoupled D-terms

(Aoife Bharucha, Andreas Goudelis & MM) 1310.4500

A quiver model: motivation

- non decoupled D-terms: lifts the Higgs
(sometimes substantially)
Batra, Delgado, Kaplan, Tait 0309149
- extra adjoints of SU(2), SU(3): lifts the Higgs
- More natural than NMSSM?
- embeds into magnetic SQCD
- Deconstructs an extra dimension
- “Split families”: Batra, Kaplan, Tait, Delgado 0404251/0409073



$$m_h^2 \simeq m_z^2 \cos^2(2\beta) + \frac{3}{(4\pi)^2} \frac{m_t^4}{v_{ew}^2} \left[\log \frac{m_{\tilde{t}}^2}{m_t^2} + \frac{X_t^2}{m_{\tilde{t}}^2} \left(1 - \frac{X_t^2}{12m_{\tilde{t}}^2} \right) \right] \quad \Delta = \left(\frac{g_A^2}{g_B^2} \right) \frac{2m_L^2}{m_v^2 + 2m_L^2}$$

Related works:

Csaki, Erlich, Grojean, Kribs 0106044

Medina, Shah, Wagner 0904.1625

“GGM and Deconstruction”

M.M. 1009.0012 and 1101.5158

Auzzi, Giveon, Gudnason, Shacham

1009.1714

1011.1664

easyDiracGauginos

Abel, Goodsell

Bharucha, Goudelis, M.M. 1310.4500

$$\delta\mathcal{L} = -g_1^2 \Delta_1 (H_u^\dagger H_u - H_d^\dagger H_d)^2 - g_2^2 \Delta_2 \sum_a (H_u^\dagger \sigma^a H_u + H_d^\dagger \sigma^a H_d)^2$$

$$m_z^2 \rightarrow m_z^2 + \left(\frac{g_1^2 \Delta_1 + g_2^2 \Delta_2}{2} \right) v_{ew}^2$$

D-terms Vs NMSSM

$$m_h^2 \simeq m_z^2 \cos^2(2\beta) + \frac{3}{(4\pi)^2} \frac{m_t^4}{v_{ew}^2} \left[\log \frac{m_{\tilde{t}}^2}{m_t^2} + \frac{X_t^2}{m_{\tilde{t}}^2} \left(1 - \frac{X_t^2}{12m_{\tilde{t}}^2}\right) \right]$$

$$\Delta = \left(\frac{g_A^2}{g_B^2} \right) \frac{2m_L^2}{m_v^2 + 2m_L^2}$$

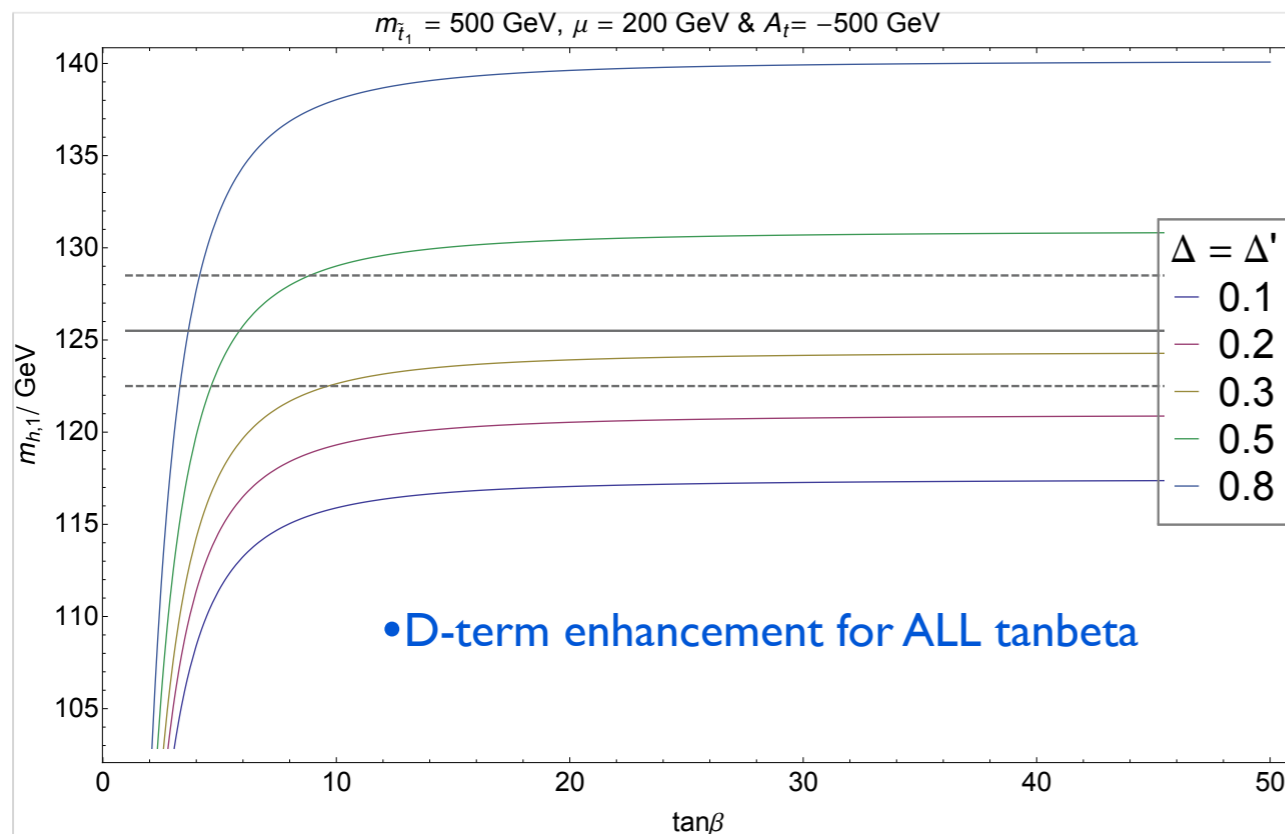
$$\delta\mathcal{L} = -g_1^2 \Delta_1 (H_u^\dagger H_u - H_d^\dagger H_d)^2 - g_2^2 \Delta_2 \sum_a (H_u^\dagger \sigma^a H_u + H_d^\dagger \sigma^a H_d)^2$$

$$m_z^2 \rightarrow m_z^2 + \left(\frac{g_1^2 \Delta_1 + g_2^2 \Delta_2}{2} \right) v_{ew}^2$$

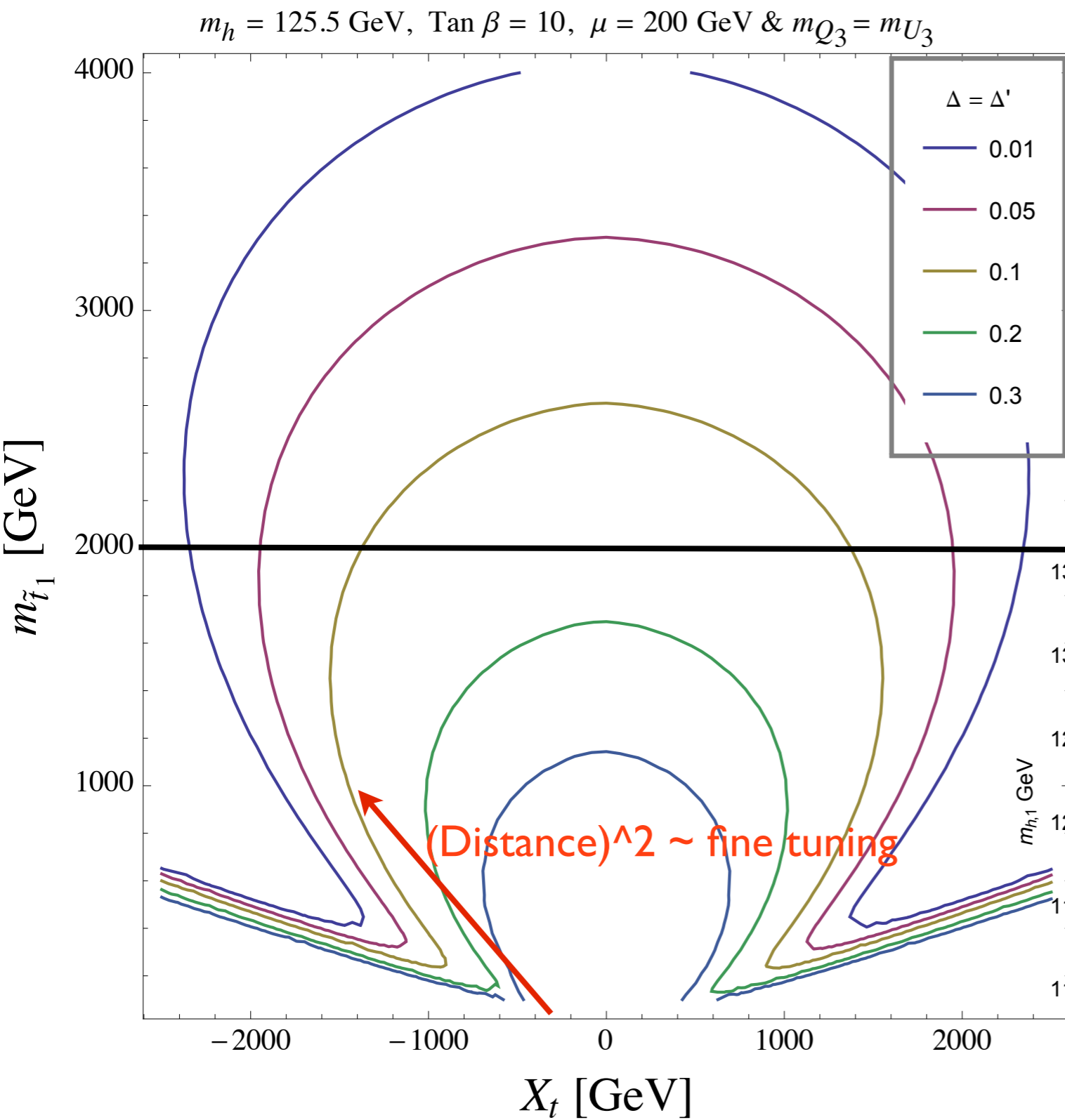
$$W_{NMSSM} \supset \lambda S H_u H_d$$

$$V(\phi's) \supset \lambda^2 |H_u H_d|^2$$

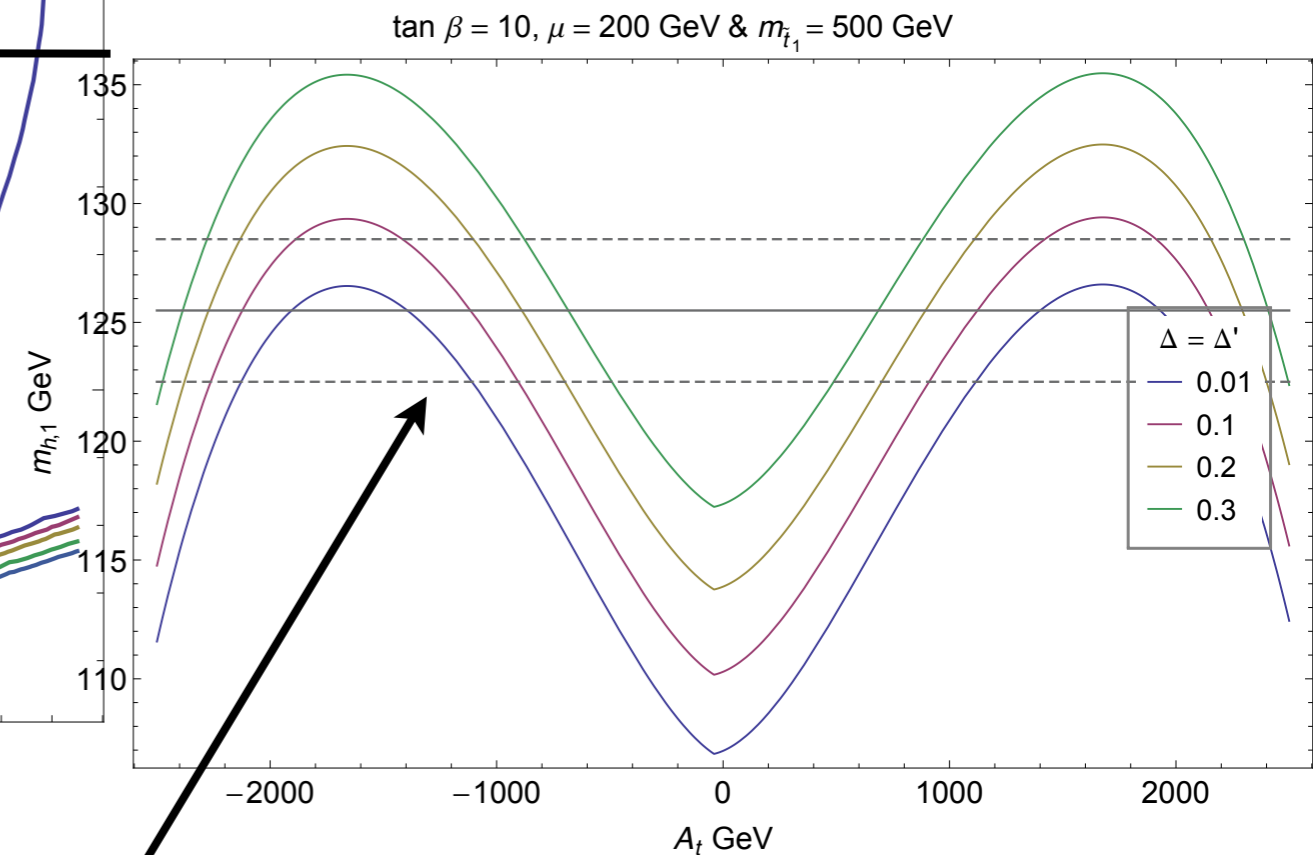
$$m_{h_0}^2 = m_z^2 \cos(2\beta) + \lambda^2 v_{ew}^2 \sin(2\beta)$$



• F-term enhancement only for small tanbeta



**Sub 2 TeV stops
for $\Delta \geq 0.1$**



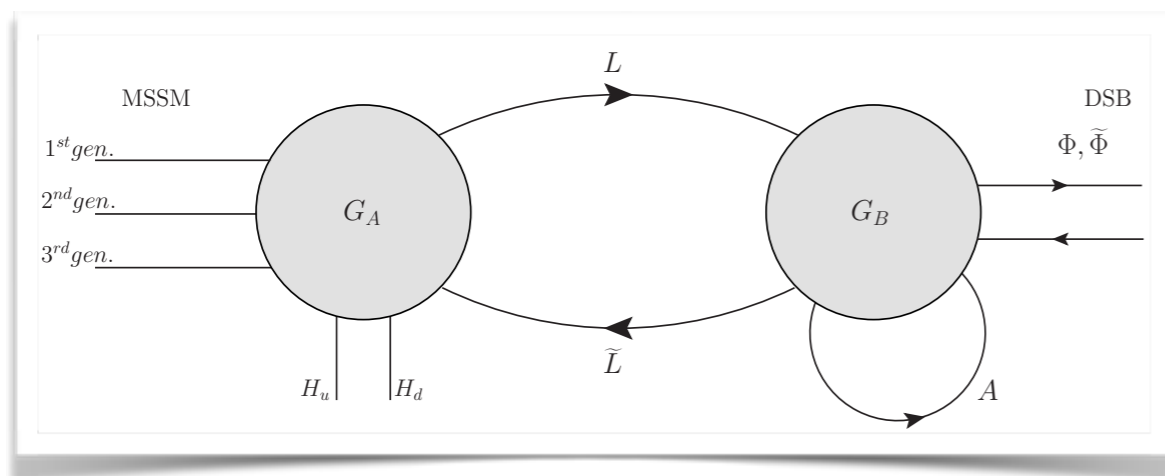
Combination of medium size A_t and Deltas can do the trick! (GMSB back in the game?)

So far most studies of D-terms have been at tree-level and bottom-up

A meta model

SF	Spin 0	Spin $\frac{1}{2}$	Generations	$(U(1)_A, SU(2)_B, SU(3)_c, U(1)_B, SU(2)_A)$	R-Parity
\hat{q}	\tilde{q}	q	3	$(\frac{1}{6}, 1, 3, 0, 2)$	-1
\hat{l}	\tilde{l}	l	3	$(-\frac{1}{2}, 1, 1, 0, 2)$	-1
\hat{H}_d	H_d	\tilde{H}_d	1	$(-\frac{1}{2}, 1, 1, 0, 2)$	+1
\hat{H}_u	H_u	\tilde{H}_u	1	$(\frac{1}{2}, 1, 1, 0, 2)$	+1
\hat{d}	\tilde{d}_R^*	d_R^*	3	$(\frac{1}{3}, 1, \bar{3}, 0, 1)$	-1
\hat{u}	\tilde{u}_R^*	u_R^*	3	$(-\frac{2}{3}, 1, \bar{3}, 0, 1)$	-1
\hat{e}	\tilde{e}_R^*	e_R^*	3	$(1, 1, 1, 0, 1)$	-1
\hat{L}	L	ψ_L	1	$(-\frac{1}{2}, \bar{2}, 1, \frac{1}{2}, 2)$	+1
$\hat{\tilde{L}}$	\tilde{L}	$\psi_{\tilde{L}}$	1	$(\frac{1}{2}, 2, 1, -\frac{1}{2}, \bar{2})$	+1
\hat{K}	K	ψ_K	1	$(0, 1, 1, 0, 1)$	+1
\hat{A}	A	ψ_A	1	$(0, 3, 1, 0, 1)$	+1

Table 2. Matter fields of the model.



$$W_{\text{SSM}} = Y_u \hat{u} \hat{q} \hat{H}_u - Y_d \hat{d} \hat{q} \hat{H}_d - Y_e \hat{e} \hat{l} \hat{H}_d + \mu \hat{H}_u \hat{H}_d$$

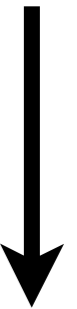
$$W_{\text{Quiver}} = \frac{Y_K}{2} \hat{K} (\hat{L} \hat{\tilde{L}} - V^2) + Y_A \hat{L} \hat{A} \hat{\tilde{L}}$$

The most sophisticated model so far implemented into a spectrum generator (SARAH/SPHENO)
 A meta-model i.e. *independent* of the type of supersymmetry breaking:
 AMSB, mSUGRA, GMSB, phenomenological, other?

Building a taylor made spectrum generator!

- We used SARAH (written by Florian Staub) mathematica package: “a spectrum generator *generator*” to write our own spectrum generator.
- We implemented 5 gauge groups with full 2-loop RGE’s and one loop self energies (soon 6 and 9 gauge groups!).
- Higgsing, and breaking to the diagonal 4 gauge groups, including all mixing matrices and assignment of Goldstones, Ghosts, RGEs of vevs, and Bmu at 2 loop.
- All 3 and 4 vertices of all fields computed, and self energies.
- All anomalous dimensions, tadpoles and running of all *additional soft terms and additional Yukawas, at 2 loop level.*
- finite shifts and threshold corrections also accounted for
- Can talk to FeynArts, FormCalc, CalcHep, HiggsSignals, HiggsBounds, WHIZARD, micrOMEGAS, Vevacious and more.

Quiver @
M messenger



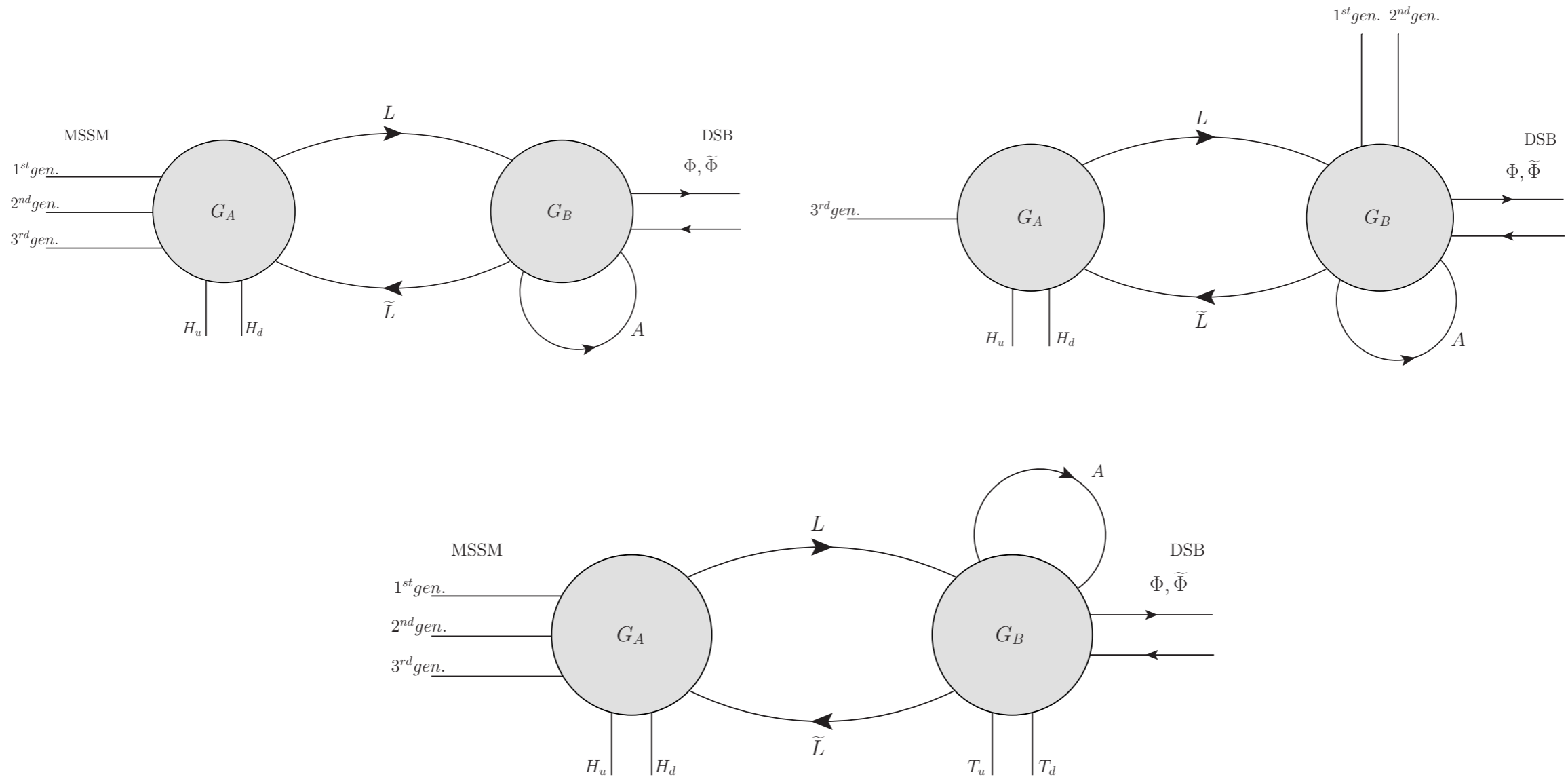
Threshold
scale:
MSSM



LHC

Same precision as SOFTSUSY, SPheno, SUSPECT

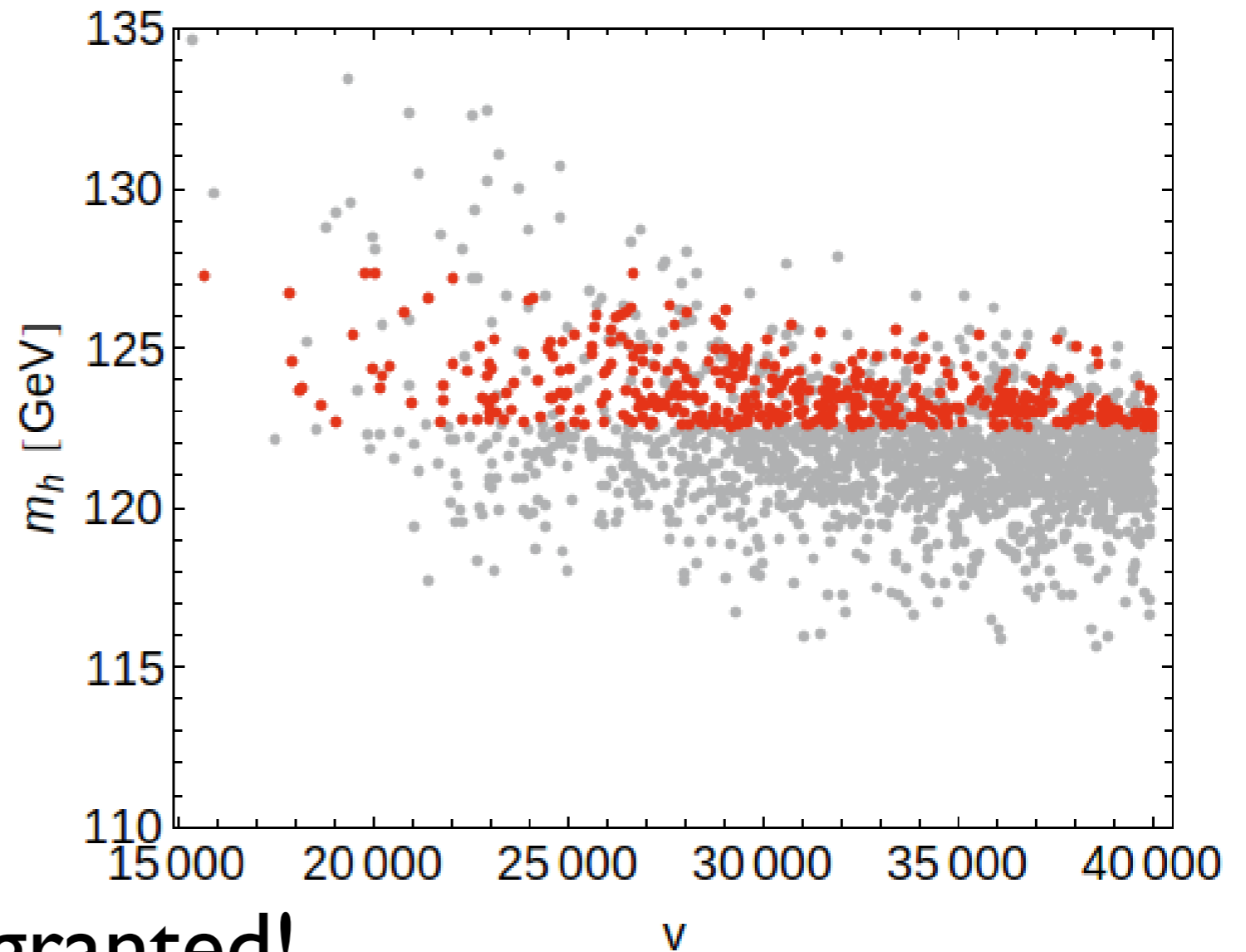
The Quiver Variations



Wish list

- $v < 10\text{TeV}$
 $m_L^2 > m_\nu^2$

We assumed GMSB
for soft terms!

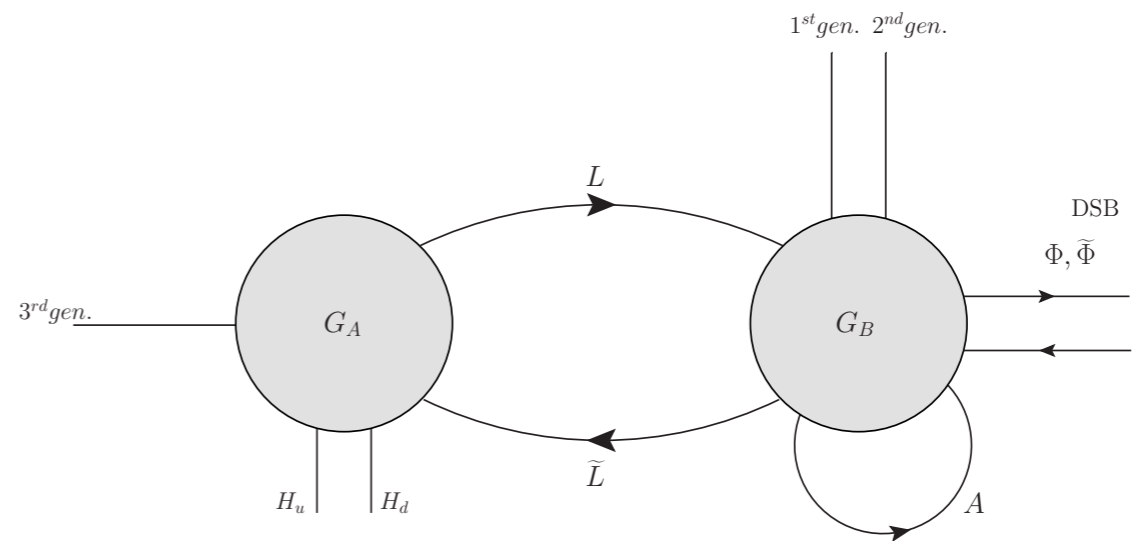
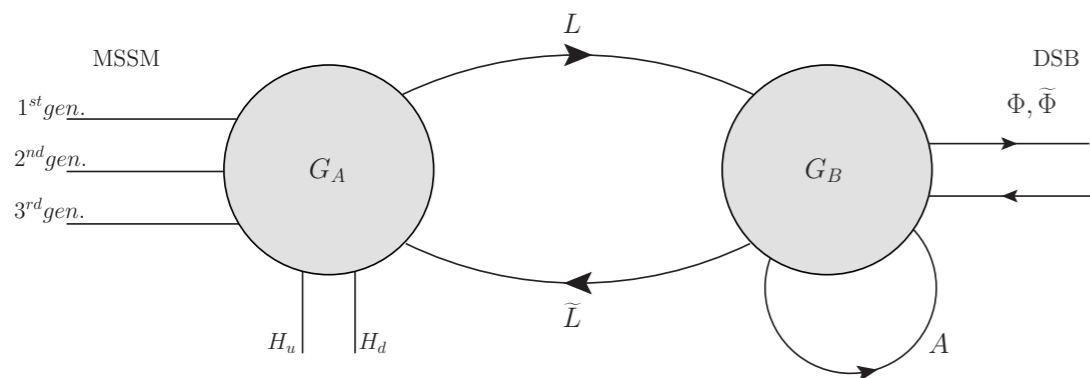
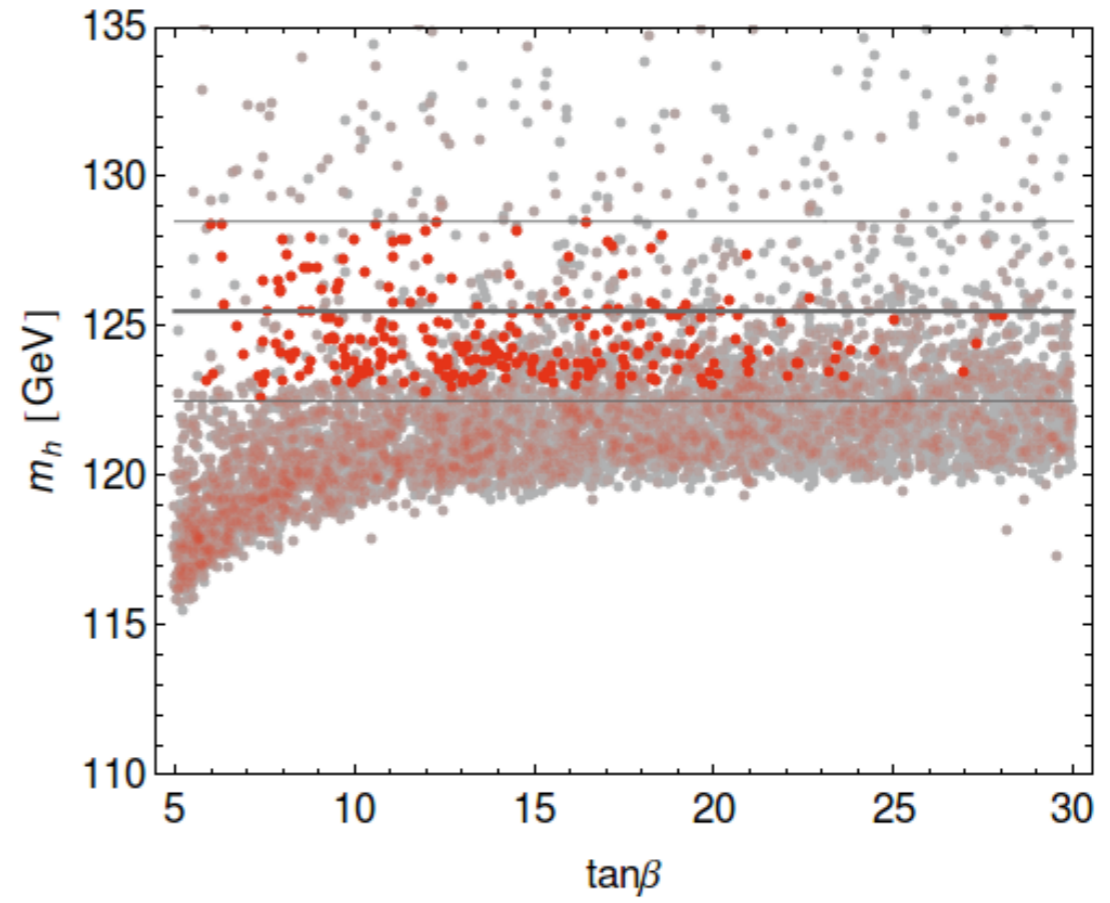
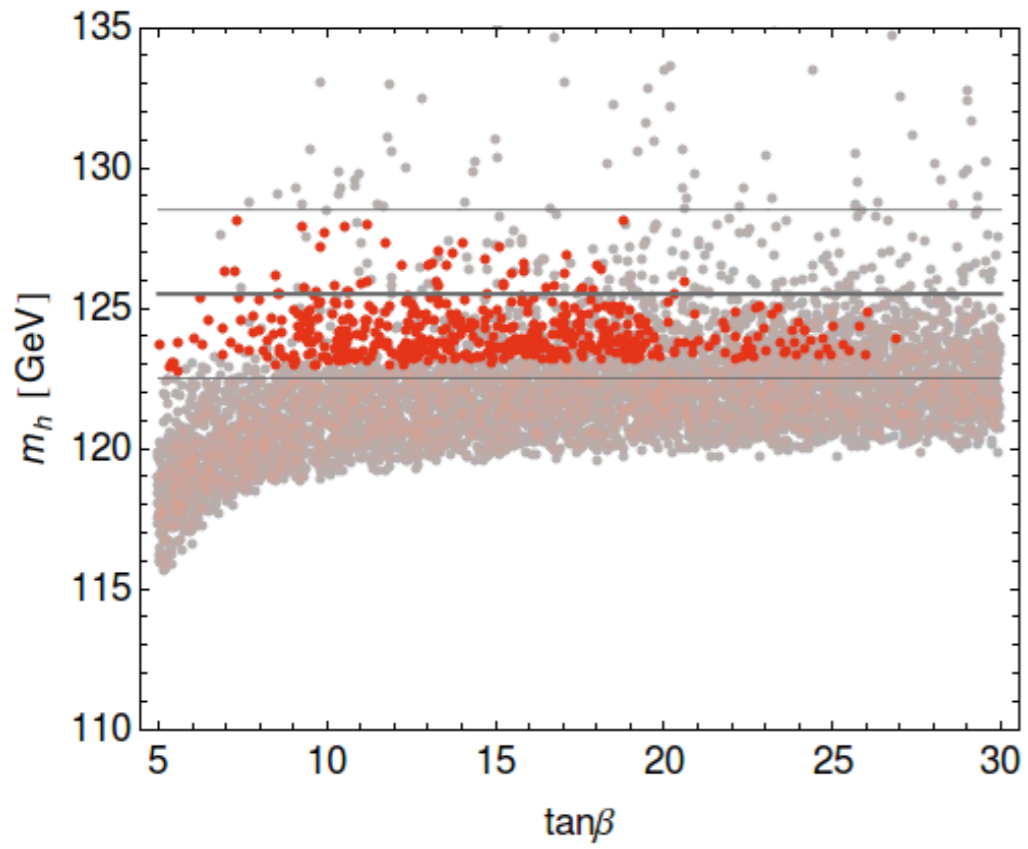


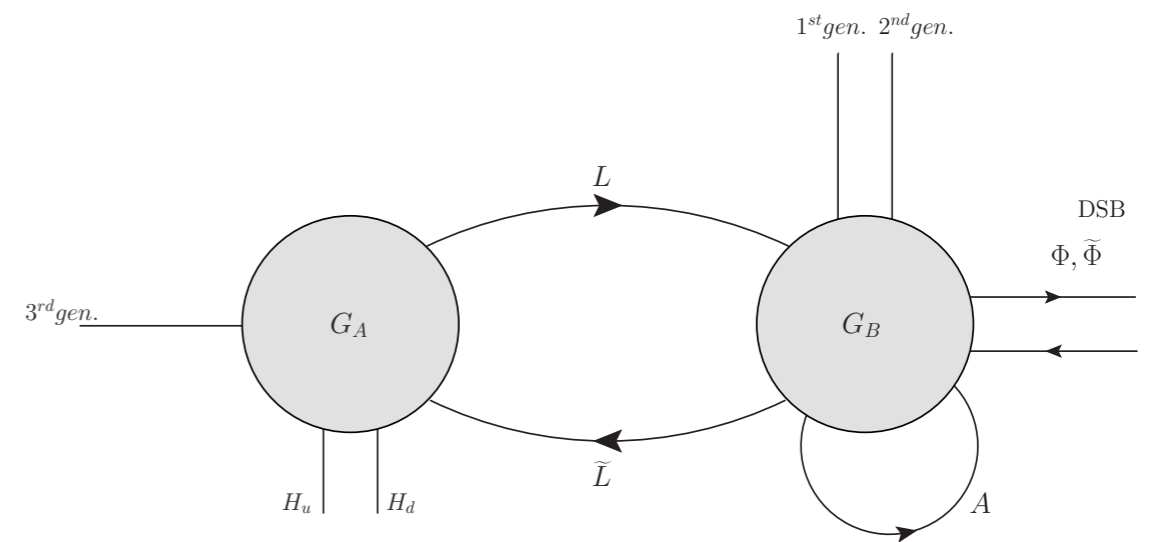
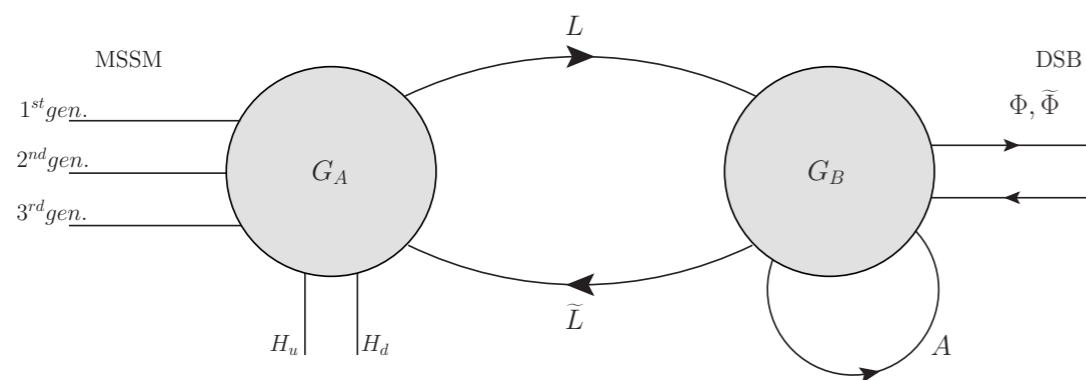
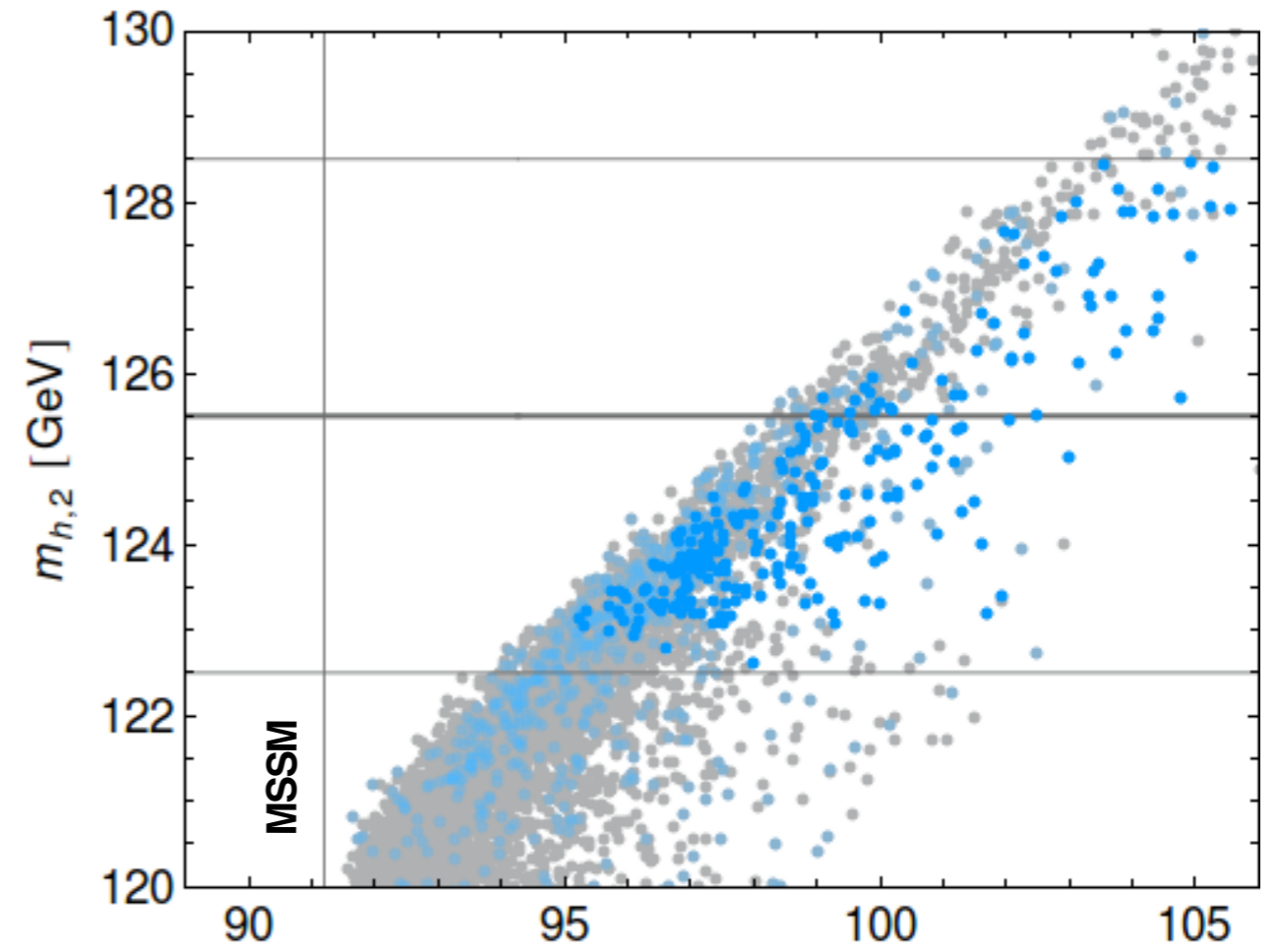
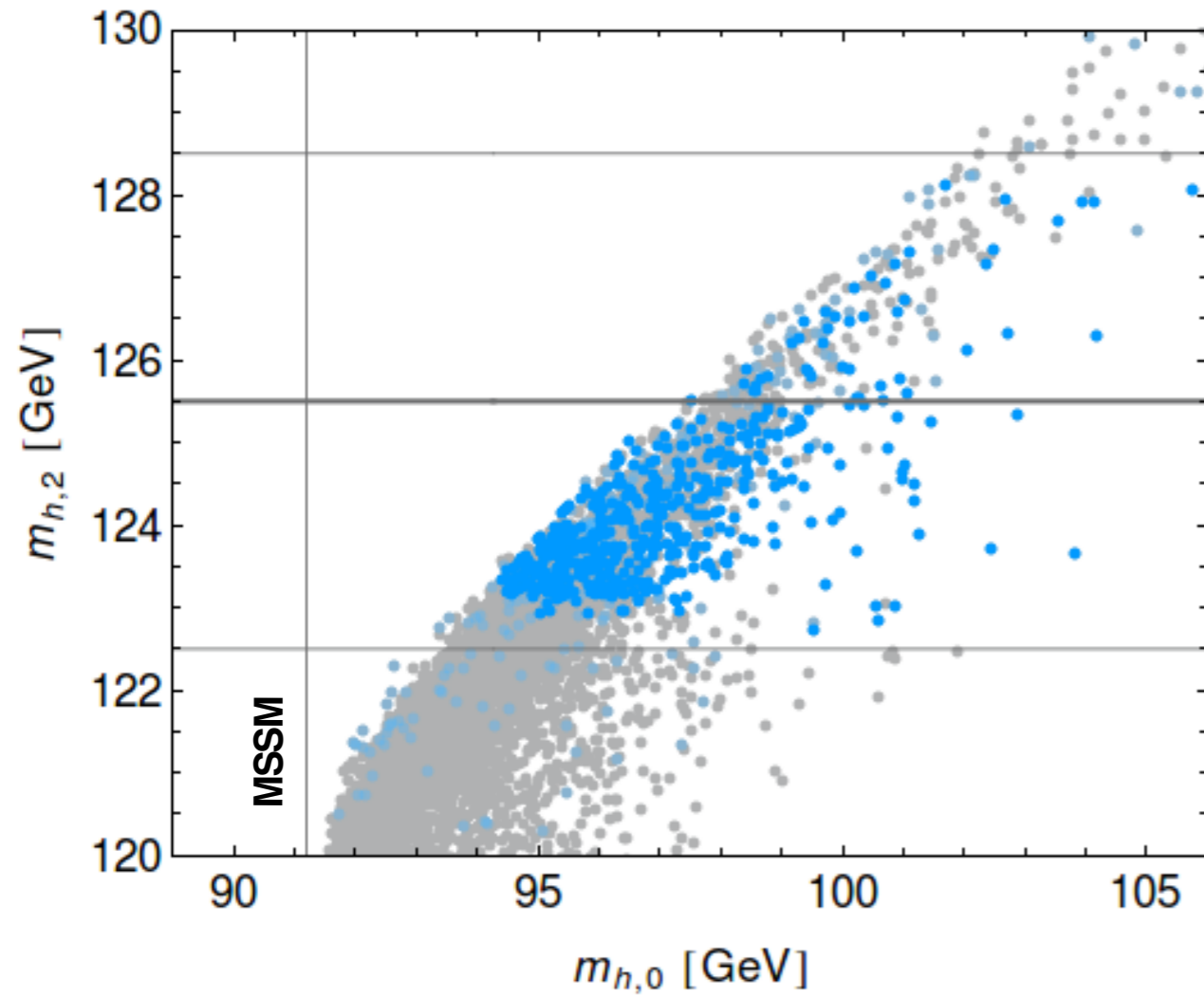
Our wishes were not granted!

we had to enlarge m_L^2 to
make it work

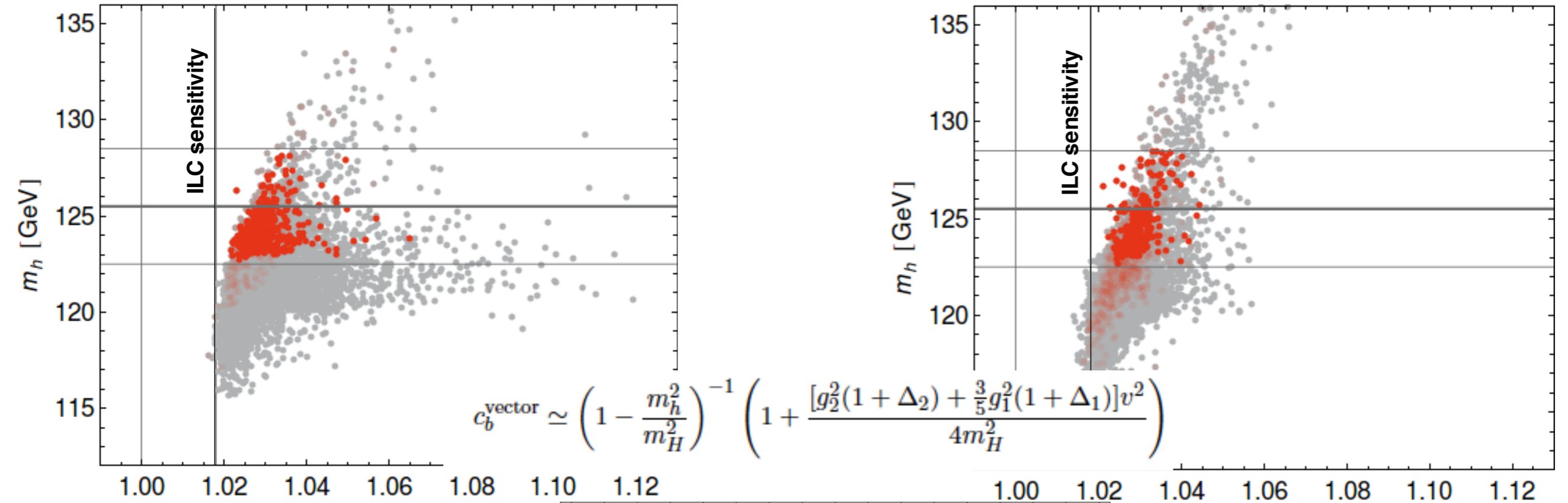
But perhaps this can be improved by
considering
different SUSY breaking scenarios

Ex. Applying mSUGRA here may get v down

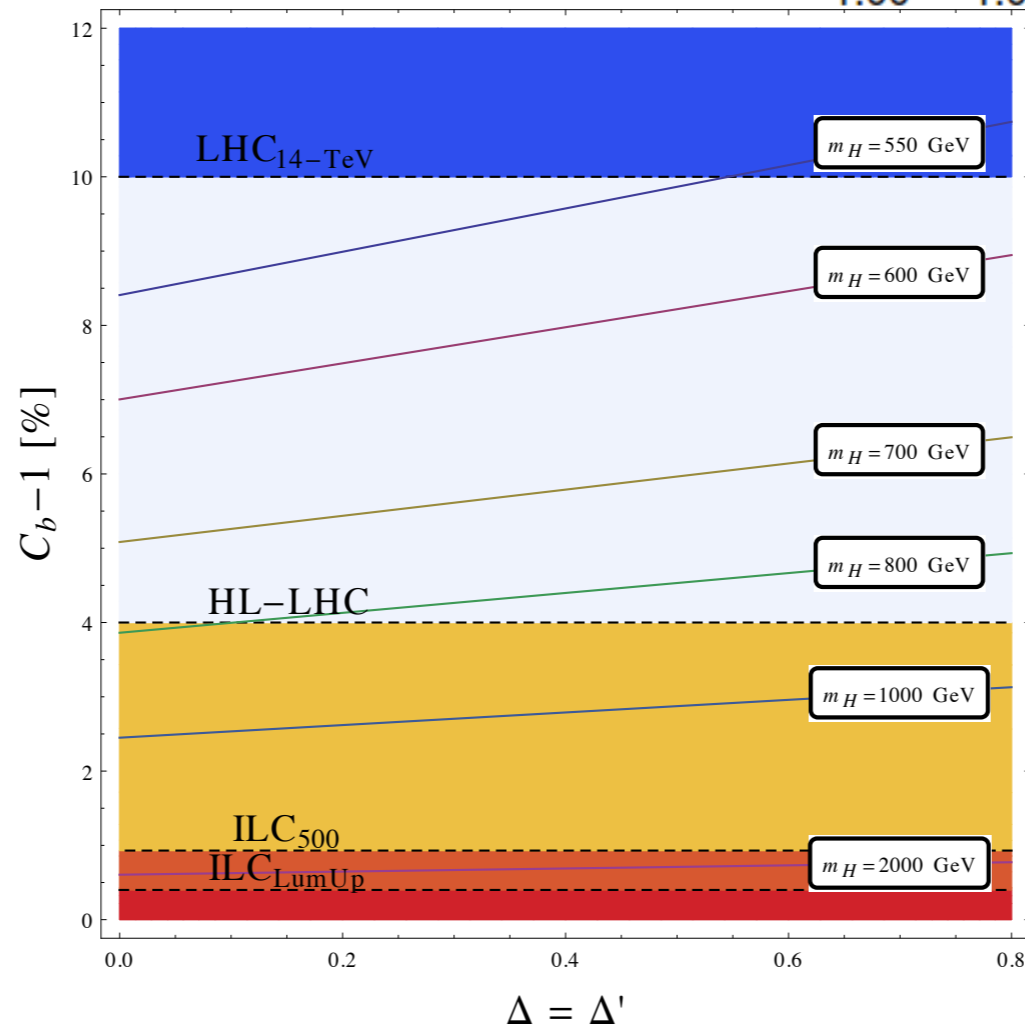




Testable at ILC!

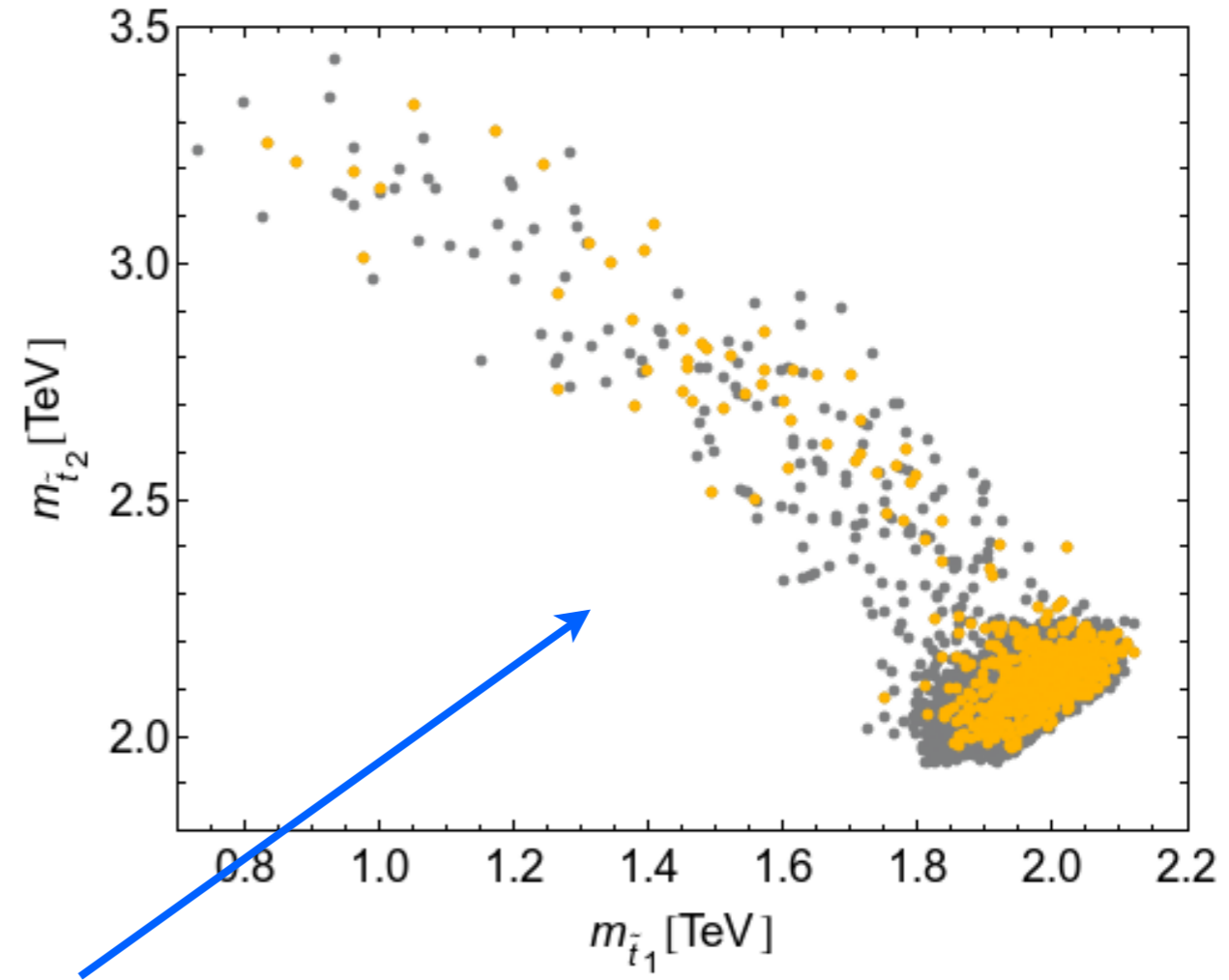
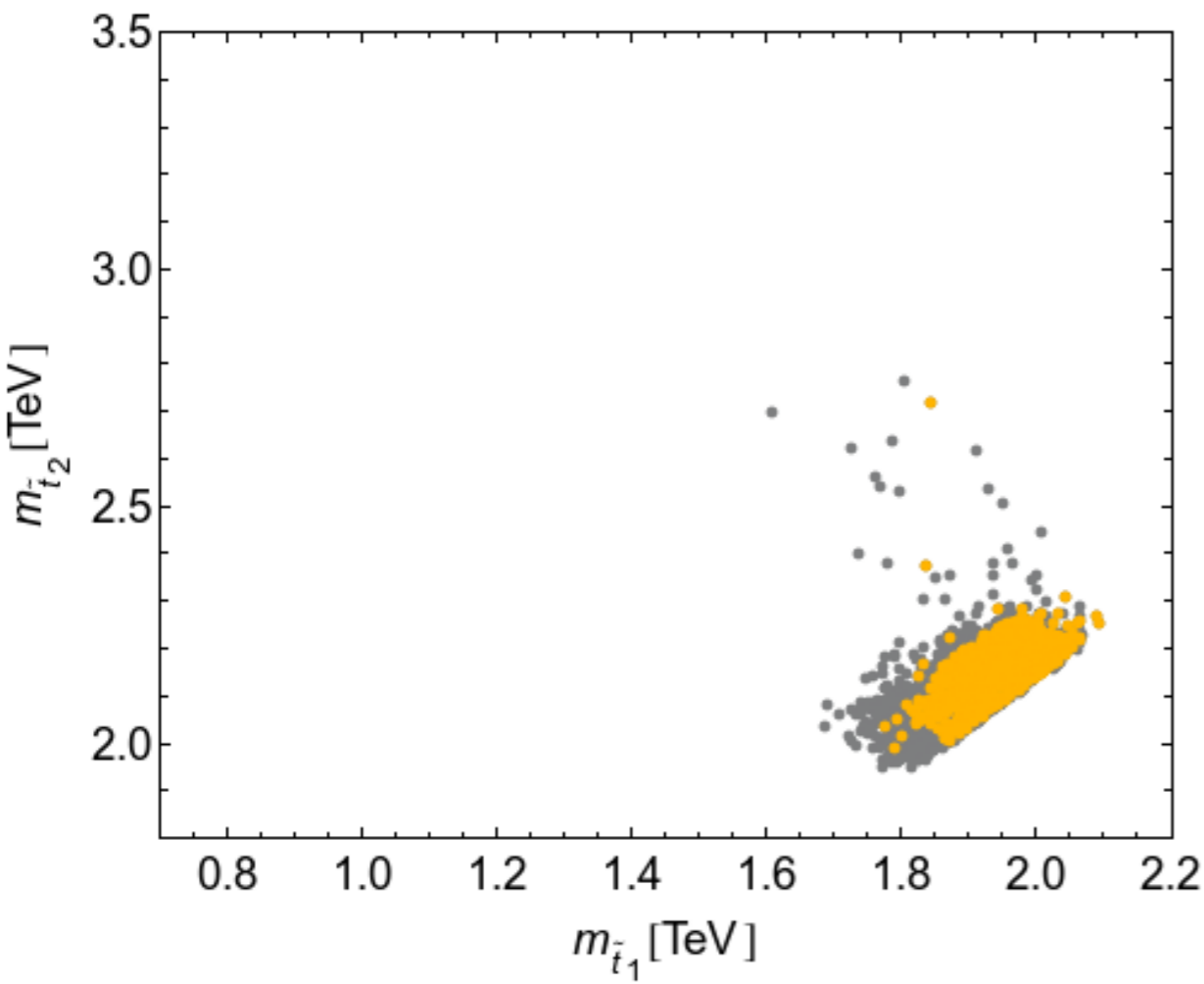


$$c_b^{\text{vector}} \simeq \left(1 - \frac{m_h^2}{m_H^2}\right)^{-1} \left(1 + \frac{[g_2^2(1 + \Delta_2) + \frac{3}{5}g_1^2(1 + \Delta_1)]v^2}{4m_H^2}\right)$$

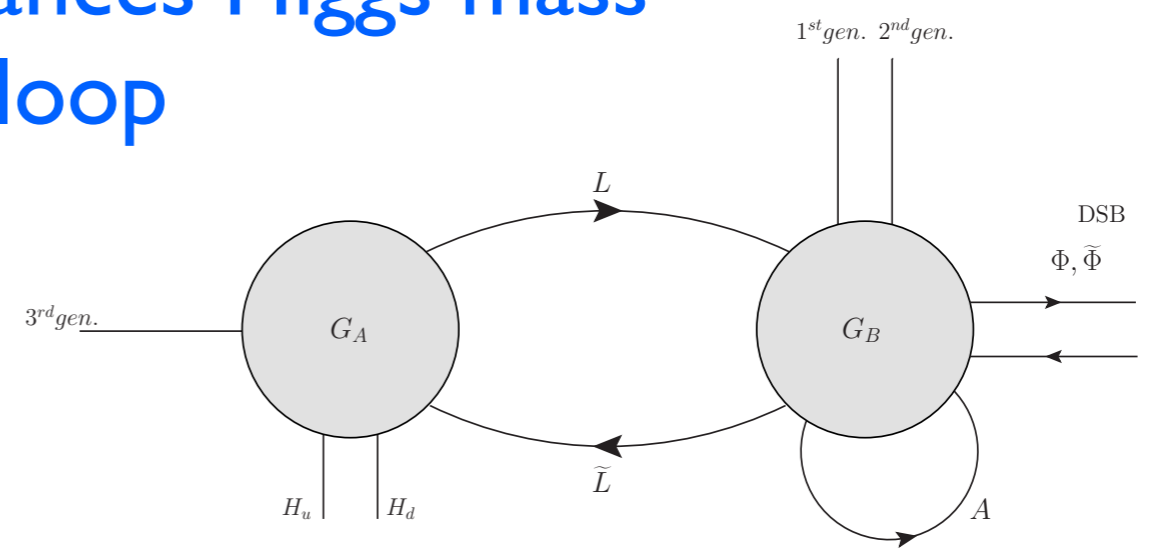
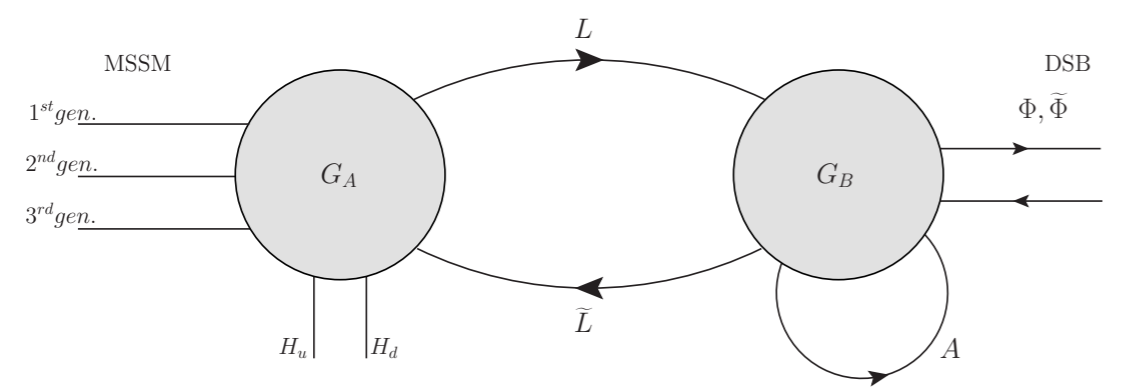


Testing D-terms
@ILC
with S.Porto, G. Moortgat-Pick (DESY)

$$m_h^2 \simeq m_z^2 \cos^2(2\beta) + \frac{3}{(4\pi)^2} \frac{m_t^4}{v_{ew}^2} \left[\log \frac{m_{\tilde{t}}^2}{m_t^2} + \frac{X_t^2}{m_{\tilde{t}}^2} \left(1 - \frac{X_t^2}{12m_{\tilde{t}}^2}\right) \right] + \Delta m_{h,1}^2 = \frac{3m_Z^2}{16\pi^2 v_{ew}^2} \left(1 - \frac{8}{3} \sin^2 \theta_W\right) \cos 2\beta m_t^2 \ln \left(\frac{m_{\tilde{q}_L^3}^2}{m_{\tilde{u}_R^3}^2} \right)$$



Stop splitting enhances Higgs mass @ 1-loop



	MI	MIa	MIb
Input values			
M	233 TeV	288 TeV	260 TeV
$\Lambda_{1,2}$	44.9 TeV	85.6 TeV	111 TeV
Λ_3	190 TeV	206 TeV	208 TeV
m_L^2	47.3 TeV ²	83.3 TeV ²	86.2 TeV ²
v	26.2 TeV	26.5 TeV	25.4 TeV
θ_1, θ_2	1.18, 1.13	1.09, 1.33	1.05, 1.04
$\tan \beta$	16	12	28
Squark sector			
$m_{\tilde{t}_1}$	1.84 TeV	1.99 TeV	409 GeV
$m_{\tilde{t}_2}$	1.98 TeV	2.06 TeV	3.49 TeV
A_t	-442 GeV	-146 GeV	-141 GeV
$m_{\tilde{b}_R}$	1.95 TeV	2.05 TeV	2.56 TeV
$m_{\tilde{q}_{12,L}}$	2.05 TeV	2.12 TeV	2.19 TeV
$m_{\tilde{q}_{12,R}}$	1.97 TeV	2.10 TeV	2.14 TeV
Slepton sector			
$m_{\tilde{l}_{12,L}}$	738 GeV	314 GeV	515 GeV
$m_{\tilde{l}_{3,L}}$	736 GeV	315 GeV	440 GeV
$m_{\tilde{l}_{12,R}}$	901 GeV	183 GeV	262 GeV
$m_{\tilde{l}_{3,R}}$	899 GeV	110 GeV	4.31 TeV
Gaugino sector			
$m_{\tilde{\chi}_1^0}$	53.2 GeV	116 GeV	154 GeV
$m_{\tilde{\chi}_2^0}$	99.3 GeV	242 GeV	306 GeV
$m_{\tilde{\chi}_3^0}$	187 GeV	750 GeV	818 GeV
$m_{\tilde{\chi}_4^0}$	222 GeV	755 GeV	823 GeV
$m_{\tilde{\chi}_1^\pm}$	96.8 GeV	242 GeV	306 GeV
$m_{\tilde{\chi}_2^\pm}$	225 GeV	756 GeV	823 GeV
$m_{\tilde{g}}$	1.62 TeV	1.66 TeV	1.75 TeV
Higgs sector			
m_{h_0}	125 GeV	127 GeV	125 GeV
m_{H_0}	720 GeV	792 GeV	885 GeV
m_{A_0}	721 GeV	796 GeV	894 GeV
m_{H_\pm}	726 GeV	799 GeV	893 GeV

Extensions:

- 6 gauge groups
- resolve issue of M_{Hu}^2 and V
- Other SUSY breaking parameterisations?
- Single regime spectrum generator
- Add the states to PDG etc....

A renormalisable way to model an extra dimension

**Ex. KK gluons, gluinos, Z' ,
KK W 's**

Can talk to FeynArts, Formcalc, CalcHep,
HiggsSignals, HiggsBounds,
WHIZARD, microOMEGA, Vevacious and more

“Deconstructed Holography for Gauge Mediation”

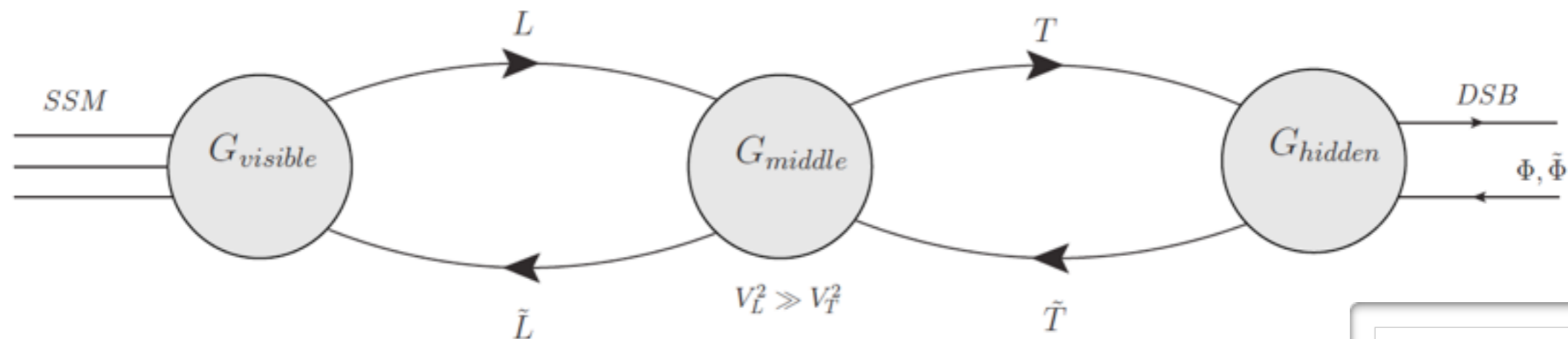
A holographic quiver

M.M. Rodolfo Russo [1004.3305](#)

M.M. Daniel C.Thompson [1009.4696](#)

M.M. [1210.4935](#)

- non decoupled D-terms
- extra adjoints of SU(2),SU(3)
- Interesting RGE's



4D: operator	Field	Δ	m^2
$\mathcal{O}_{L,R} = \phi^\dagger \phi_{L,R}$	$\rightarrow D(z, x)_{L,R}$	2	-4
$\mathcal{O}^\alpha(x)_{L,R} = -i\sqrt{2}\phi^\dagger q_{L,R}^\alpha$	$\rightarrow \lambda^\alpha(z, x)_{L,R}$	5/2	1/2
$\mathcal{O}^\mu(x)_{L,R} = \bar{q}\sigma^\mu q_{L,R} - i(\phi^\dagger \partial^\mu \phi - \partial^\mu \phi^\dagger \phi)_{L,R}$	$\rightarrow A^\mu(z, x)_{L,R}$	3	0

Table 1: Operators corresponding to the bulk fields of the model.

